

DOCUMENT RESUME

ED 286 721

SE 048 379

TITLE Quincy Market. [A Product of] the Regional Math Network: A Teacher Invigoration and Curriculum Development Project.

INSTITUTION Harvard Univ., Cambridge, Mass. Graduate School of Education.

SPONS AGENCY National Science Foundation, Washington, D.C.

PUB DATE Jun 87

GRANT NSF-MDR-84-70399

NOTE 205p.; For other products of the Regional Math Network, see SE 048 377-378.

AVAILABLE FROM Dale Seymour Publications, P.O. Box 10888, Palo Alto, CA 94303 (\$35.00; includes computer disk suitable for any Apple computer and game cards).

PUB TYPE Guides - Classroom Use - Guides (For Teachers) (052)
-- Guides - Classroom Use - Materials (For Learner) (051) -- Computer Programs (101)

EDRS PRICE MF01 Plus Postage. PC Not Available from EDRS.

DESCRIPTORS Area; *Economics; *Estimation (Mathematics); Map Skills; Mathematical Applications; Mathematical Concepts; *Mathematical Enrichment; Mathematics Education; *Mathematics Instruction; Mathematics Skills; Problem Solving; Ratios (Mathematics); Sampling; Secondary Education; *Secondary School Mathematics

IDENTIFIERS Massachusetts (Boston)

ABSTRACT

In this middle school mathematics unit two imaginary characters, Horatio and Portia, decide to make their fortune in Quincy Market (Boston, Massachusetts) running a Bull Market cart. In order to solve the problems that they encounter, they need to learn ratio and proportion, map reading, estimation, area and perimeter, population sampling, problem solving, and the collecting and processing of data. Teacher notes at the beginning of each section indicate the math objectives, materials, and whether the activity is a reinforcement or an extension of a math skill. The unit is divided into seven modules that can be used either independently or sequentially. These are: (1) an introduction to Quincy Market; (2) the use of the ruler; (3) map exploration; (4) ratio and proportion; (5) scale drawing; (6) perimeter and area; and (7) a simulation (in which the students run their business using the Bull Market Game or a computer simulation). Each module consists of two or three class activities and additional activities which can be used as extensions. The unit contains student worksheets, teacher notes, transparency masters, Bull Market Game cards, and a diskette to be used with the computer portion of the "simulation" module. (TW)

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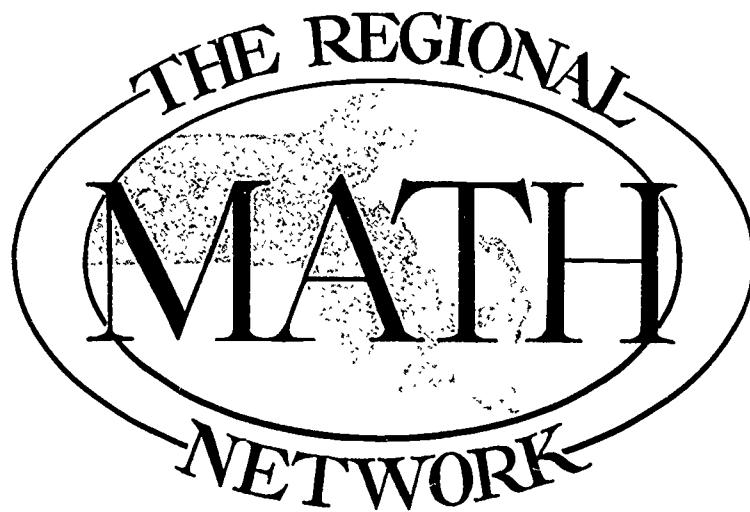
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QUINCY MARKET



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A Teacher Invigoration and Curriculum Development Project
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This material is based upon work supported by the National Science Foundation under Grant No. MDR-84-70399.

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Acknowledgements

We would like to acknowledge the contributions that several people have made to the development of these materials and to the overall implementation of the project.

For their presentations to the Teacher Fellows and project staff and for their helpful comments on the direction of The Regional Math Network activities, special gratitude is due to:

Stanley Bezuszka
Patricia Davidson
Carole Greenes
Michael Guillen

Peter Hilton
Alan Hoffer
Deborah Hughes-Hallett
Margaret Kenney

Steven Leinwand
Henry Pollak
Judah Schwartz
Harold Weymouth

The following individuals have given technical advice and contributed their expertise to various aspects of the project:

Aardvark Systems
Eric Arnold
John Chuang

Steve Codell
Lily Lee
Jeff Loeb

Blythe Olshan
Pamela Roth
Philip Sadler

Christopher Unger
Scott Wilder

Special appreciation to David Li, Boston Public School graduate, class of '86, who facilitated the creation of T-Stop Sales.

The Regional Math Network benefitted greatly from the untiring efforts of the Research Assistants and the MidCareer Math and Science Teacher Training Program Fellows. These individuals included:

John Bookston
Lisa Bonanno
John Burnette
Tom Czarny

Mary Eich
Matt Goggins
Randall Hancock
David Masunaga

Joy Moser
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Matt O'Connor
Eileen O'Sullivan

Joe Patuleia
Joel Poholsky
Jeff Sayah
Scott Smith

Randy Starr
Ted Stein
Jearld Waitkus

A special note of thanks is due to the Production Staff who typed, corrected and retyped the multiple drafts. Their willingness to work toward an improved final copy was impressive.

Steve Codell
Marianne Connolly
Brian Cranton

Scott Cranton
John Domilici
Charles Gerlach

Robert Hafer
Audrey Handelman
Ruskin Hunt

Stuart Klein
Lisa Oray
Robert Sporn

Loralyn Thompson

Particular recognition is given to Michael N. Smith of Laser Designs Corp. of Cambridge for his direction and organization during the final stages of production, and to Randy Hobbs of P&R Publications, who guided the printing process.

Finally, the Regional Math Network gratefully acknowledges the administrators, teachers, students, schools and districts within the region that participated in the development and evaluation of the project materials. The Regional Math Network would not have been possible without their cooperation.

FOREWORD

Mathematics is an increasingly important skill for understanding and appreciating the challenges in our society. Yet the learning of these concepts poses difficulties for many students, especially as they reach the junior high/middle school years. At the same time, mathematics teachers are leaving their profession at a rapid rate, tired of using materials that have not been revised to reflect changes in our society and its workforce. Clearly, a need exists to revitalize both the self-esteem and the teaching resources of those who have chosen this profession. The **Regional Math Network** aims to address these difficulties. The project, **funded by the National Science Foundation**, is sponsored by the Harvard Graduate School of Education.

The overall goal of the Regional Math Network is to invigorate individual teachers and to enhance the quality of the materials and techniques of those in the mathematics teaching profession. To achieve this goal, the Regional Math Network provided 22 Teacher Fellows from eleven school systems with a structured opportunity to collaborate with local business professionals and university personnel in the development of innovative teaching materials and instructional strategies. The school systems represented in the project include Acton, the Archdiocese of Boston, Boston, Cambridge, Chelmsford, Hingham, Lexington, Somerville, Waltham, and the Carroll, the Tower, and the Buckingham, Brown & Nichols Schools.

The **Regional Math Network** also seeks to stimulate math teaching in the greater Boston area. Toward that end, the Network sponsors seminars, receptions and meetings for math teachers and other interested professionals and students. The **Regional Math Network** serves as a model of collaboration on several levels: among different schools in the region, between schools and local businesses, and between these parties and the University, which primarily serves as a facilitator and resource.

A fundamental objective is to produce supplemental materials that are engaging for early adolescents and to improve their interest and ability in problem solving. The Teacher Fellows were organized into four project teams, each with a team leader and graduate research assistants. After conducting a needs and interest assessment within many regional schools and districts, each project team selected a specific context that provided the basis for the consideration of a major mathematical topic traditionally covered in the middle school curriculum. These contexts include an ice cream factory, local sporting events, the solar and space shuttle systems and Quincy Market, a local tourist and commercial area. To better understand the context, teams conferred with members of the local business community and worked with students from Harvard's MidCareer Math & Science Program, former business professionals studying to become mathematics teachers.

Each of these four context areas is linked to specific mathematical topics. While this emphasis does not exclude other related topics, teachers seeking materials on a particular topic may choose to work with a specific unit. The topics of emphasis include:

Ice Cream - Fractions

Math/Space Mission - Estimation, Geometry and Relational Concepts

Quincy Market - Ratio and Proportion

Sports Shorts - Decimals and Percents

All four of the units include a common emphasis on problem posing and problem solving. Many of the activities are open ended, encouraging students to pose their own problems for solving. Other themes and topics common to all of the units stress skills of estimation, graphing, polling, reading and interpreting charts, calculators and computer application and mental arithmetic. All of the materials stress realistic, mathematical applications that are accessible and motivating to middle school students.

Each of the units contains a variety of teacher and student resources. These include teacher notes and teaching suggestions, student pages, answers, activity cards, transparency masters, manipulative materials and classroom games. Additionally, the Quincy Market unit contains a computer disk suitable for any Apple computer.

These materials were written by teachers for other teachers to use. Hence, the materials and format are designed with a teacher's needs and constraints in mind. Comments about these materials are welcomed and may be made by writing to Professor Katherine K. Merseth, The Regional Math Network, Harvard Graduate School of Education, Cambridge, MA 02138.



NOTES TO TEACHERS

Regional Math Network • Harvard Graduate School of Education • Harvard University

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HORATIO AND PORTIA

A Mathematical Adventure

Introduction

Welcome to the world of Horatio and Portia, two imaginary characters who hear about Quincy Market and decide to make their fortune running a Bull Market cart. They have all sorts of adventures and mis-adventures in the process as they use maps to find out how to get to Quincy Market, take surveys to determine what to sell, and finally, run their cart.

Horatio and Portia constantly need math skills to solve their problems. They learn ratio and proportion, map reading, estimation, area and perimeter, population sampling, problem solving, and the collecting and processing of data.

Students who have used this unit in its pilot form have found it both fun and challenging, and we expect that your students will, too. They will use math because they need it to solve interesting and real problems that spark their imagination.

To make this unit easy to use by teachers who have many demands on their time, we have provided a variety of already prepared or easy to prepare materials. The Teacher Notes at the beginning of each section indicate the math objectives, materials needed, and whether the activity is a reinforcement or extension of a math skill.

We have divided the unit into seven modules. Each can be used independently, but the story line and the mathematical ideas flow best when they are used sequentially. The modules are:

1. Introduction to Quincy Market
2. Ruler
3. Map Exploration
4. Ratio and Proportion
5. Scale Drawing
6. Perimeter and Area
7. Simulation

Each module consists of 2-3 class activities and additional activities which can be used to reinforce or extend the topics presented in class. Every effort has been made to present material in a variety of ways and on a variety of levels. You will find individual, group and class activities. Material is presented concretely, visually, verbally, and numerically.

Teachers who have access to a computer for class use will find that the unit provides excellent opportunities for introducing students to real-life computer applications. The data which Horatio and Portia gather can be organized using a data base. In addition, their cart's inventory and financial reports are perfect for spreadsheet applications. We have included a computer game developed for this project, T-Stop Sales, which simulates the Bull Market cart business. The program will run on any Apple II computer.

OVERVIEW OF THE UNITS

Introduction to Quincy Market: This unit, which introduces the student to Quincy Market, provides a variety of alternatives to the teacher. A field trip (guidelines included), or a poster of Quincy Market which can be colored and displayed to stimulate class discussion can "set the scene".

Students are introduced to Horatio and Portia, who have just found a flyer announcing a sales opportunity at Quincy Market. Students read and study the flyer and accompanying scale drawings to glean facts about the market and to make decisions about potential sales opportunities.

Ruler: Students construct their own rulers and then use Quincy Market Bull Cart information to solve puzzles which require careful measurements. A map of a section of downtown Boston is also included which requires measurement and problem solving.

Map Exploration: Students use maps to explore metropolitan Boston. Students locate their own communities, Quincy Market, and other points of interest. They study scale coordinates, linear measurement, and distance within a circle of specific radius as they discover a wide variety of information about Eastern Massachusetts. The state map extends their map reading skills and knowledge of routes, distances and scale.

Ratio and Proportion: Horatio and Portia have to make important decisions about what to sell, how much to charge, and where to locate their cart. Students help Horatio and Portia to make predictions using actual figures from Quincy Market shops. They take their own survey to determine what they would sell. Teachers with access to a computer may have students record and analyze their information using a data base.

This unit incorporates many mathematical objectives including generating data from text and maps, population sampling, ratio, proportion, survey techniques, data collection and analysis, and problem solving.

Scale Drawing: Students use the scale drawing of Quincy Market to construct a classroom display. They then construct three dimensional models of the Bull Market carts and enlarge pictures of a crow and a grasshopper to include in the display.

In this unit, the students are using their knowledge of ratio and proportion, linear measure, scale drawing, and area and perimeter to solve real problems. Since this is a class project, students must depend upon one another for accuracy.

Perimeter and Area: Horatio and Portia need to know about perimeter and area to solve some of their problems. They develop an intuitive understanding of these topics as they explore Quincy Market. For example, they discover how many carts it would take to surround Quincy Market, how many people can fit into a small area, and project these answers onto larger areas.

In this unit students will use their knowledge of perimeter and area to make projections about Quincy Market.

Simulation: Students finally run their cart!! We have provided two methods of achieving this. In the "Bull Market Game", the class (or small groups) compete to make the greatest profit at the end of the week. The teacher who has access to one or more Apple computers can use the program specifically designed for this unit, "T-Stop Sales". In this program, students try to beat Sloppy Joe, a lazy business person who also runs a tee shirt cart. They can beat him only if they order carefully and price wisely. Both options require problem solving strategies and provide a review of basic math skills.

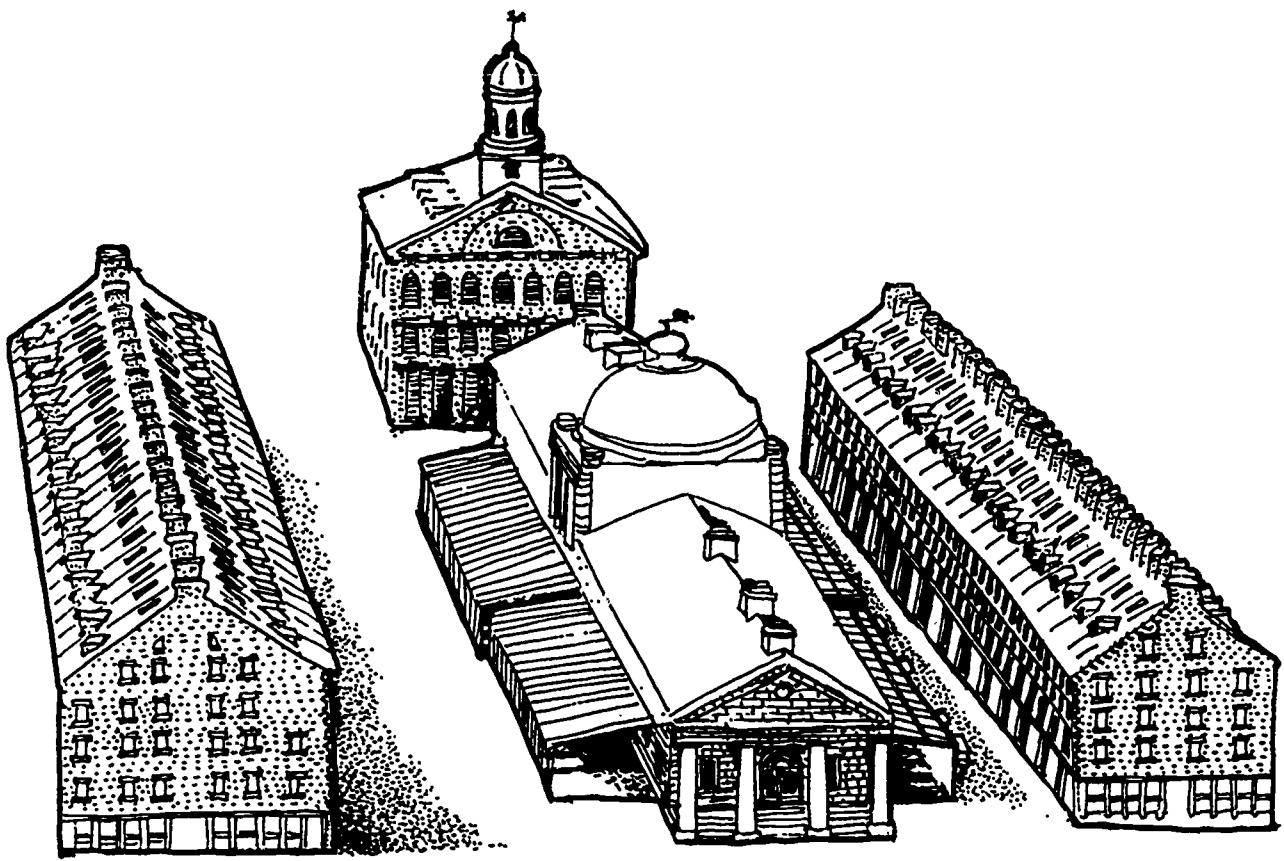
Students also learn to keep business records either by hand or using a computer spreadsheet application. They complete the project by finishing Portia and Horatio's Story.

ACTIVITY GRID & CONTENTS

	Ratio & Proportion	Perimeter & Area Measurement	Additional Topics	Activity Coding
Page Number	Meaning of Ratios Solving Proportions Rate Problems Scales	Measuring Skills Perimeter Area Naming Figures Circle Concepts Converting Units	Interdisciplinary Mental Arithmetic Estimation Graphing Understanding Charts Prediction Geometry	Reading Maps and Scale Drawings Problem Solving Collecting and Analyzing Data Problem Posing
Intro				
Getting the Facts	9			
QM Field Trip	11			
Ruler				
Follow the Ruler	19	●	●	
Code to Portia	23	●		
Where's My Cart?	24	●		
Take the Bull by the Horns	28	●		
Line Up	30	●		
As the Grasshopper Hops	32	●		
Map Exploration				
Map Exploration	38	●	●	
Partial Map of Boston	39	●		
Boston + Vicinity	40	●	●	
Route from Boston	43	●		
Where does the Crow Land?	44	●	●	
Ratio and Proportion				
Your Ratios	51	●		
Portia Predicts	53	● ● ●		
One of the Crowd	55	● ●		
Crowd According to Portia	57	● ●	●	
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Tally-Ho	67		●	
Steve's Ice Cream Survey	69	● ●	●	

ACTIVITY GRID & CONTENTS

	Ratio & Proportion	Perimeter & Area Measurement	Additional Topics	Activity Coding
Page Number	Meaning of Ratios Solving Proportions Rate Problems Scales	Measuring Skills Perimeter Area Naming Figures Circle Concepts Converting Units	Interdisciplinary Mental Arithmetic Estimation Graphing Understanding Charts Prediction Geometry Reading Maps and Scale Drawings Problem Solving Collecting and Analyzing Data Problem Posing	Introductory Long Term Open-Ended Answers Provided Calculator / Computer Special Challenges
Scale Drawing				
Scale Drawing of Shops	72	● ● ● ●	● ● ● ● ● ●	● ● ● ● ● ●
Graph Hopper	85	● ● ● ●	● ● ● ● ●	● ● ● ●
Construct Bull Cart	87	● ● ● ●	● ● ● ● ●	● ● ● ●
Perimeter and Area				
Perimeter	91	● ● ● ●	● ● ● ●	● ● ● ●
I Counted My Hops	92	●	● ● ● ●	● ● ● ●
Hands Around School	93	● ● ● ●	● ● ● ●	● ● ● ●
QM We've Got You Surrounded	94	● ● ● ●	● ● ● ●	● ● ● ●
Portia's Dilemma	95	● ● ● ●	● ● ● ●	● ● ● ●
Area: Squares and Rectangles	96	● ● ● ●	● ● ● ●	● ● ● ●
How Many Visitors Fit in QM?	97	● ● ● ●	● ● ● ●	● ● ● ●
Bull Cart Storage	98	● ● ● ●	● ● ● ●	● ● ● ●
Spot on the Wheel	99	● ● ● ●	● ● ● ●	● ● ● ●
Pi for Horatio	102	● ● ● ●	● ● ● ●	● ● ● ●
How Many Rotations?	103	● ● ● ●	● ● ● ●	● ● ● ●
Big Slice in Life of Horatio	104	● ● ● ●	● ● ● ●	● ● ● ●
Pizza Pi	106	● ● ● ●	● ● ● ●	● ● ● ●
Room Under the Umbrella	107	● ● ● ●	● ● ● ●	● ● ● ●
Summary				
Business Simulation	112	● ● ● ●	● ● ● ●	● ● ● ●
Grand Finale	116	● ● ● ●	● ● ● ●	● ● ● ●



INTRODUCTION TO QUINCY MARKET

GETTING THE FACTS

<u>Topic/Objective</u>	<u>Materials</u>
Generate data from written materials and maps	Quincy Market "business opportunity" flyer, storyline poster, scale drawings of Quincy Market

Before Class:

Prepare a bulletin board

Select appropriate bulletin board materials from the following introductory pages
(Note: A large poster of Quincy Market is included in your packet)

Schedule a field trip (optional)

Make overheads of scale drawings and cast of characters

During Class:

1. Introduce the history of Q.M. using "Hometown Boy Makes Good" information sheet.
2. Discuss the present day Q.M. using the scale drawings and "Move Over Mickey Mouse".
3. Introduce the cast of characters (Horatio, Portia, etc.).
(Note: These characters are essential to the story line in each unit.)

After Class

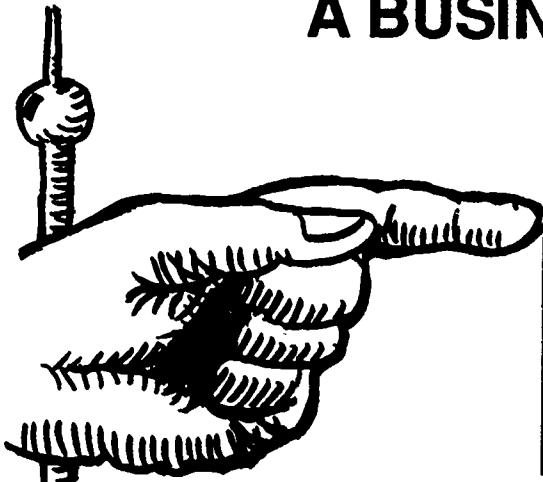
Ask students to write and solve five interesting math questions based on "Move Over Mickey Mouse."

Reinforcement

Make a poster illustrating an idea from "Hometown Boy Makes Good."

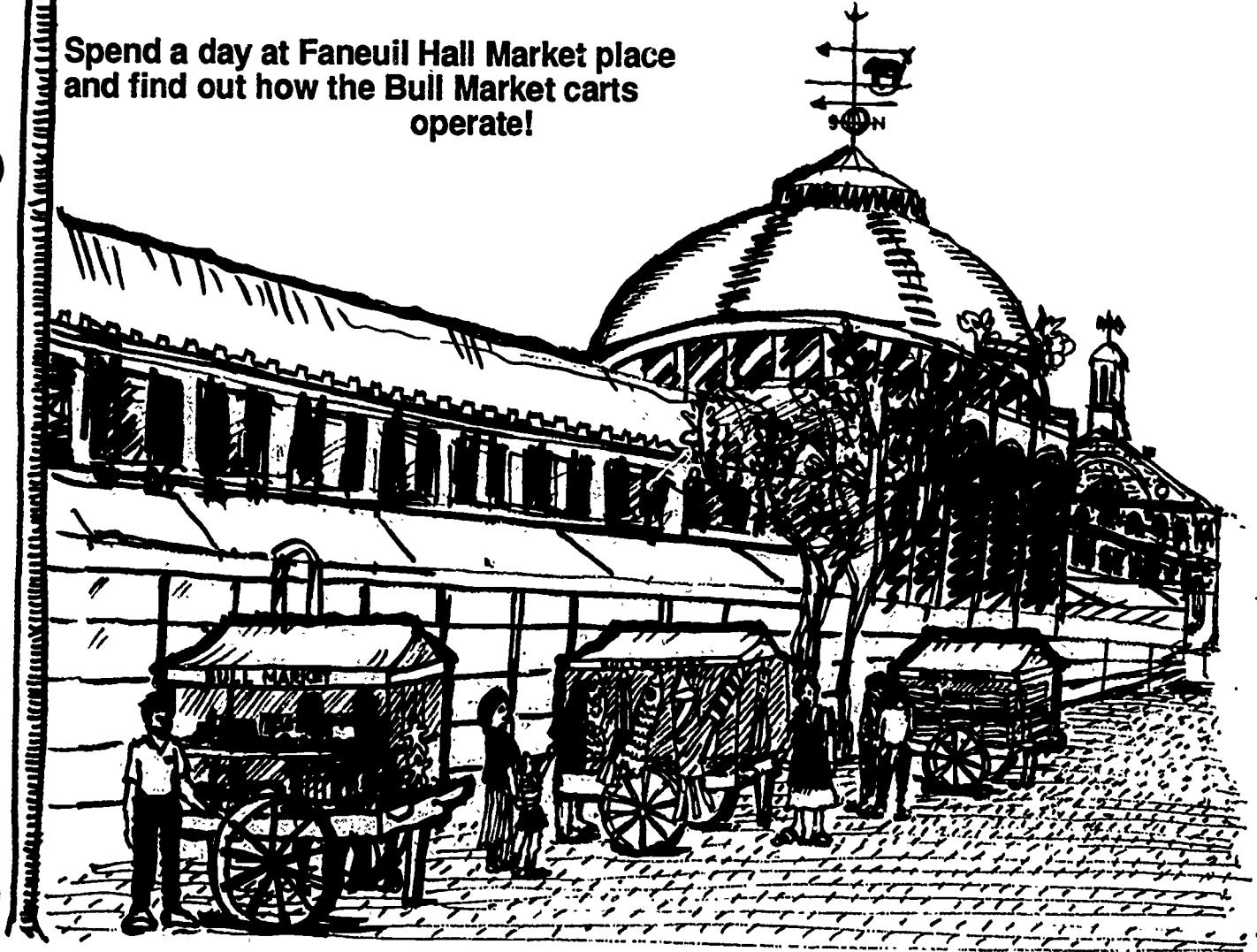
Reinforcement

Attention A BUSINESS OPPORTUNITY



**RUN YOUR OWN BULL MARKET
CART
AT
FANEUIL HALL MARKET PLACE
"FUN, FANTASY, FOOD, AND FROLIC"**

Spend a day at Faneuil Hall Market place
and find out how the Bull Market carts
operate!



QUINCY MARKET FIELD TRIP

A field trip to Quincy Market provides an excellent introduction to this unit. Students not only have an opportunity to "sample the flavor" of Quincy Market, they also have an opportunity to expand their knowledge of Boston history through a trip to Faneuil Hall and to learn how to do some real "data collection" as they gather information about Quincy Market. A trip must be carefully planned, however, so that students gain maximum benefit from it. Some important information to help you plan your trip is included below:

Best time to visit: October to May (least crowded)

Transportation: Nearest T-Stop is Haymarket. Parking is very limited.

Cost: None, other than food and transportation

Restrooms: In basement of rotunda, very limited.

Guided Tours: None of Quincy Market, but the National Park Service provides guided tours of Faneuil Hall

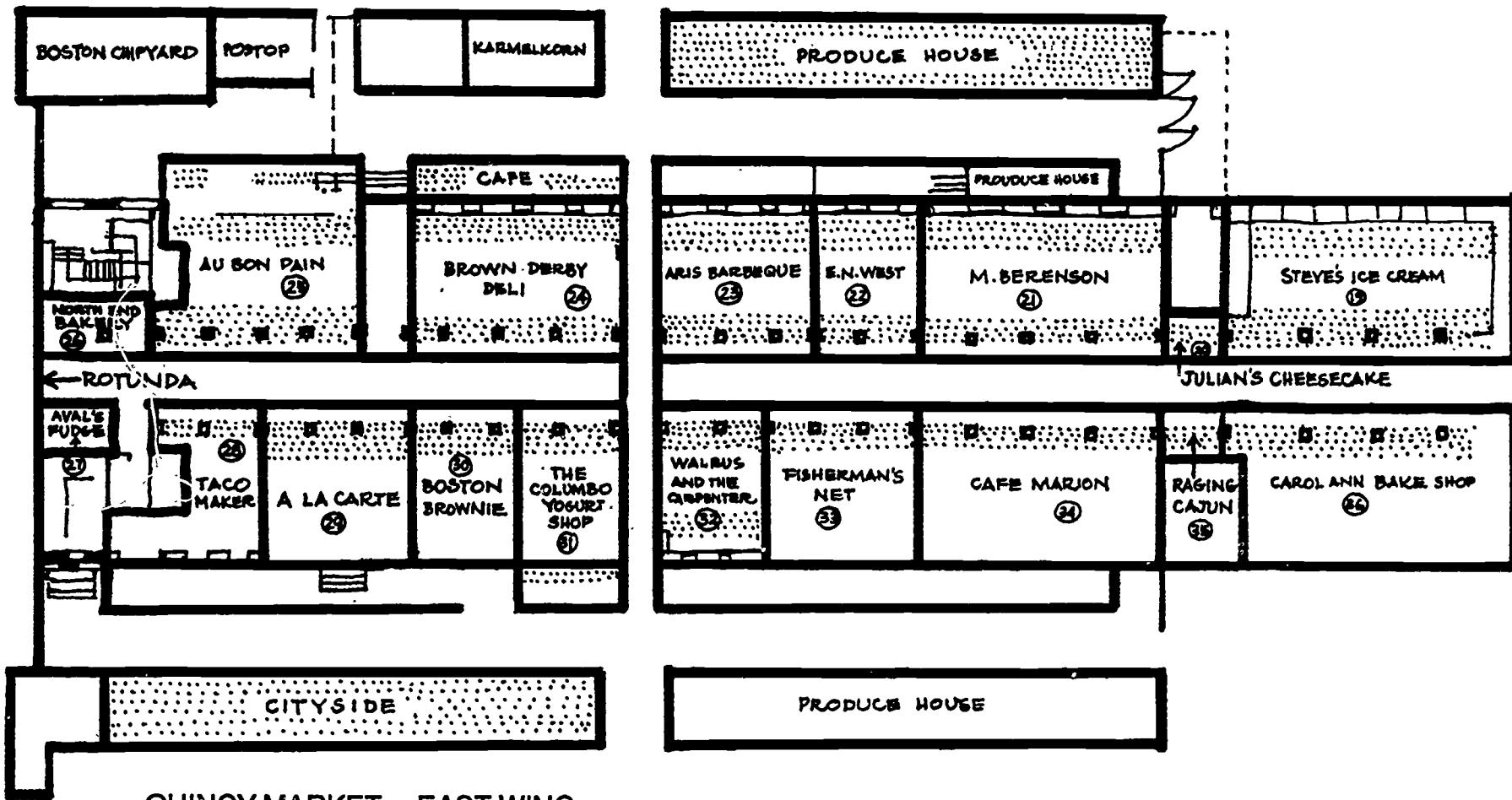
Chaperones: One for every 6 to 10 students if you plan to have students collect data

Pre-Field Trip Class Preparation:

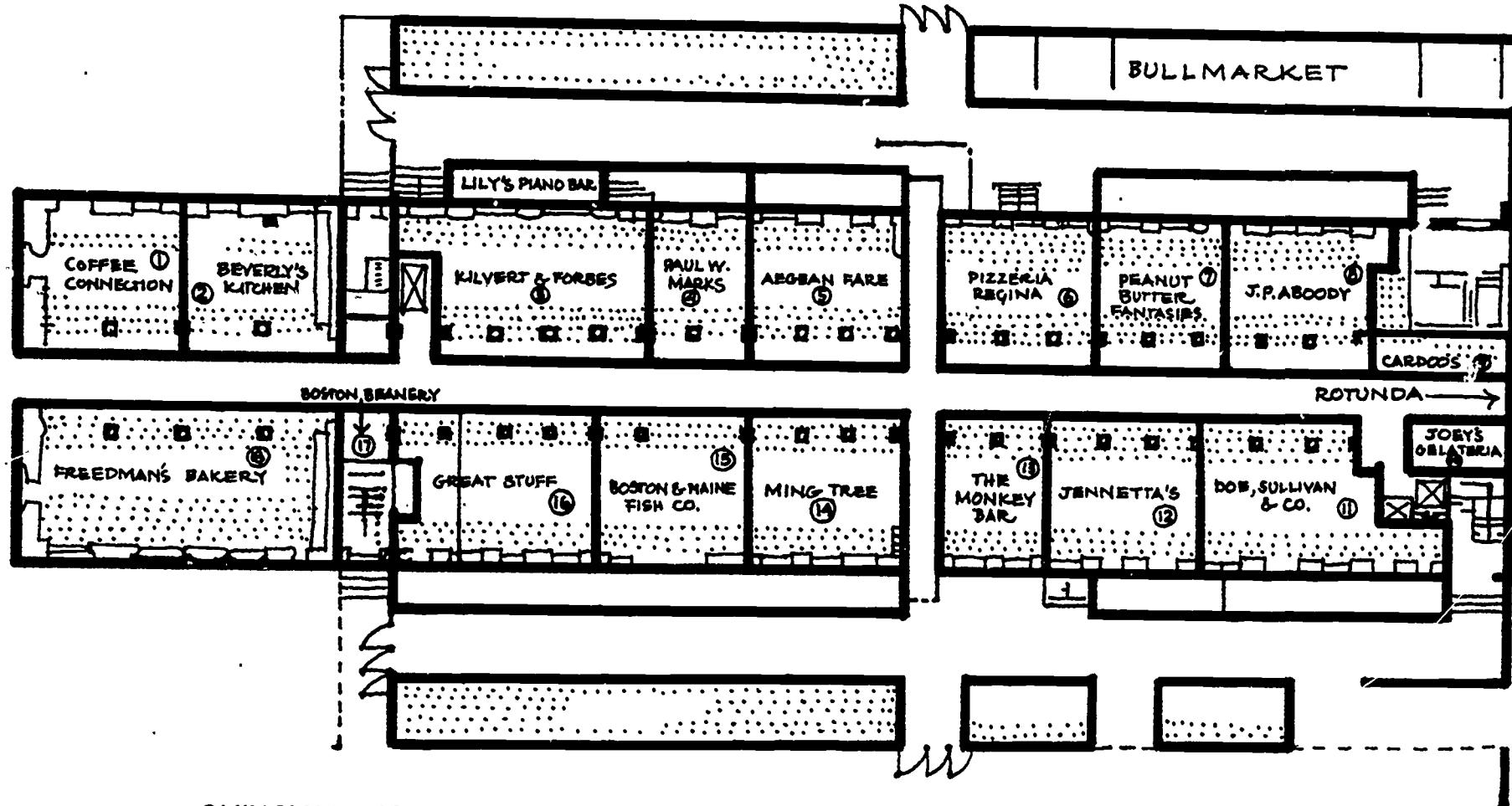
- Discuss Quincy Market and Faneuil Hall:
Their history (brief outline in appendix)
Location (use the T-Aid map)
Layout of shops—difference between stall, Bull Market, and store (use diagram)
- Brainstorm about what students should look for:
Location and type of food stalls
Location and type of Bull Market carts
Location of grasshopper (weathervane on Faneuil Hall)
Location of bull (weathervane on Quincy Market)
Number of salespeople at each stand
How weather affects sales
How many geometric shapes can students find
Which is the best location for a Bull Market cart
Which is the most popular cart, food stall
How do carts store their supplies
- Assign specific tasks to each group:
Make a list of all the food stalls
Make a list of all the Bull Market carts
Count the number of pieces of pizza sold in 5 minutes (specify which 5 minutes and compare to another 5 minute period at a different time during the day)
Count the number of ice cream cones sold in 5 minutes
Count the number of people who enter the west door in 5 minutes
Estimate the dimensions of Quincy Market

Follow-Up (homework, projects, etc.)

- Sketch a model of your favorite cart
- Draw a sketch of Quincy Market with the layout of stalls and carts from your notes
- Write an article on Quincy Market for your school or local newspaper



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FANEUIL HALL MARKETPLACE

HOMETOWN BOY MAKES GOOD!

Faneuil Hall was a gift to the city of Boston by Peter Faneuil in 1742 to mark his success and repay his hometown by building a hall for public use.

FIRE DESTROYS FANEUIL HALL!

Faneuil Hall burned down in 1761 and was rebuilt in 1763 with public funds.

THE CRADLE OF LIBERTY!

Faneuil Hall became famous as a meeting place and popular "rostrum." The first rumblings of the American Revolution took place here. Faneuil Hall continues to be a popular, national "rostrum" (have you looked this word up yet?) for many popular and unpopular ideas, causes, and organizations.

-The Hall 'below' became a 'market' for the exchange of goods.

-The Hall 'above' became a 'market' for the exchange of ideas.

GROWING PAINS FOR FANEUIL HALL!

Architect Charles Bullfinch enlarges it in 1806.

A NEW NEXT DOOR NEIGHBOR!

The Quincy Market Building was constructed in 1823. It was designed by architect Alexander Parish.

QUINCY MARKET TAKES NOTHING FOR GRANITE!

The Quincy Market Building is a two story granite market house. It is flanked by two 'harmonious' granite warehouses, one on North Market Street and the other on South Market Street.

...BUT THE WALLS START TUMBLIN' DOWN!

The markets remained in continuous use but by 1950 needed much repair.

REPAIRS, RENEWAL AND REBIRTH!

Redevelopment began in 1973 and was completed in 1978.

MOVE OVER, MICKEY MOUSE



Did you know that 12 to 14 million people visit Quincy Market every year! That's more people than visit Disney World! Not only do these people visit Quincy Market--they spend money too!

\$\$\$\$\$\$\$\$\$\$\$\$

The average visitor spends \$37, including \$10 at the Bull Market Carts. The average Bull Market Cart shopper is between 10 and 20 years old. These visitors give an ambitious young businessperson an excellent opportunity to get started.

Who Visits Faneuil Hall Marketplace?

Here are some important figures:

- 18% work in Boston
- 18% live within Route 128
- 7% live in Massachusetts outside Route 128
- 57% live outside New England

What Do People Eat?

Here are some statistics: (approximate)

- Pizzeria Regina sells 600 pizzas a day
- The Taco Maker sells 400 tacos and 250 burritos a day
- Boston Brownies sells 1000 brownies each day

Introducing.....

The Miscalculations of Horatio and Portia

THE CAST OF CHARACTERS

HORATIO



What's He Like?

A curious 13 year old--sometimes disorganized, sometimes illogical, sometimes impulsive, and sometimes.....

Favorite Expression:

"Oops! I miscalculated again!"

PORIA



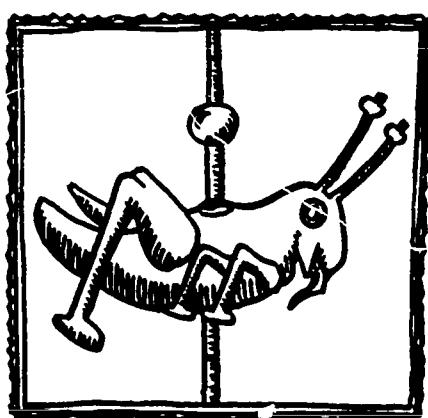
What's She Like?

A curious 13 year old-- sometimes organized, sometimes logical, often methodical, and often.....

Favorite Expression:

"It's perfectly obvious!"

THE GRASSHOPPER



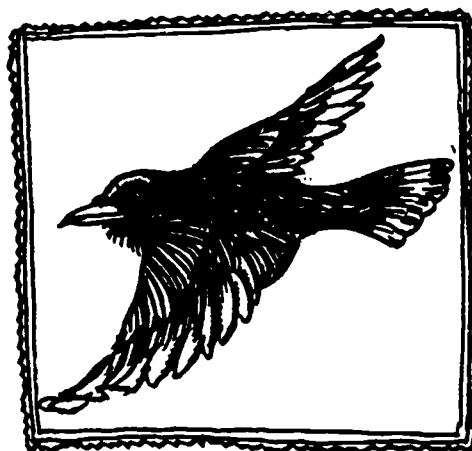
What's He Like?

He's the symbol of Faneuil Hall Market place and sits high atop Faneuil Hall on the weathervane. He's always 'happy-go-lucky'.

Favorite Expression:

"I never measure! I just count my hops!"

THE CROW



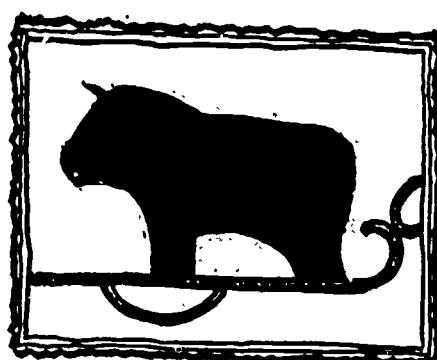
What's He Like ?

Very logical--all the time !

Favorite Expression:

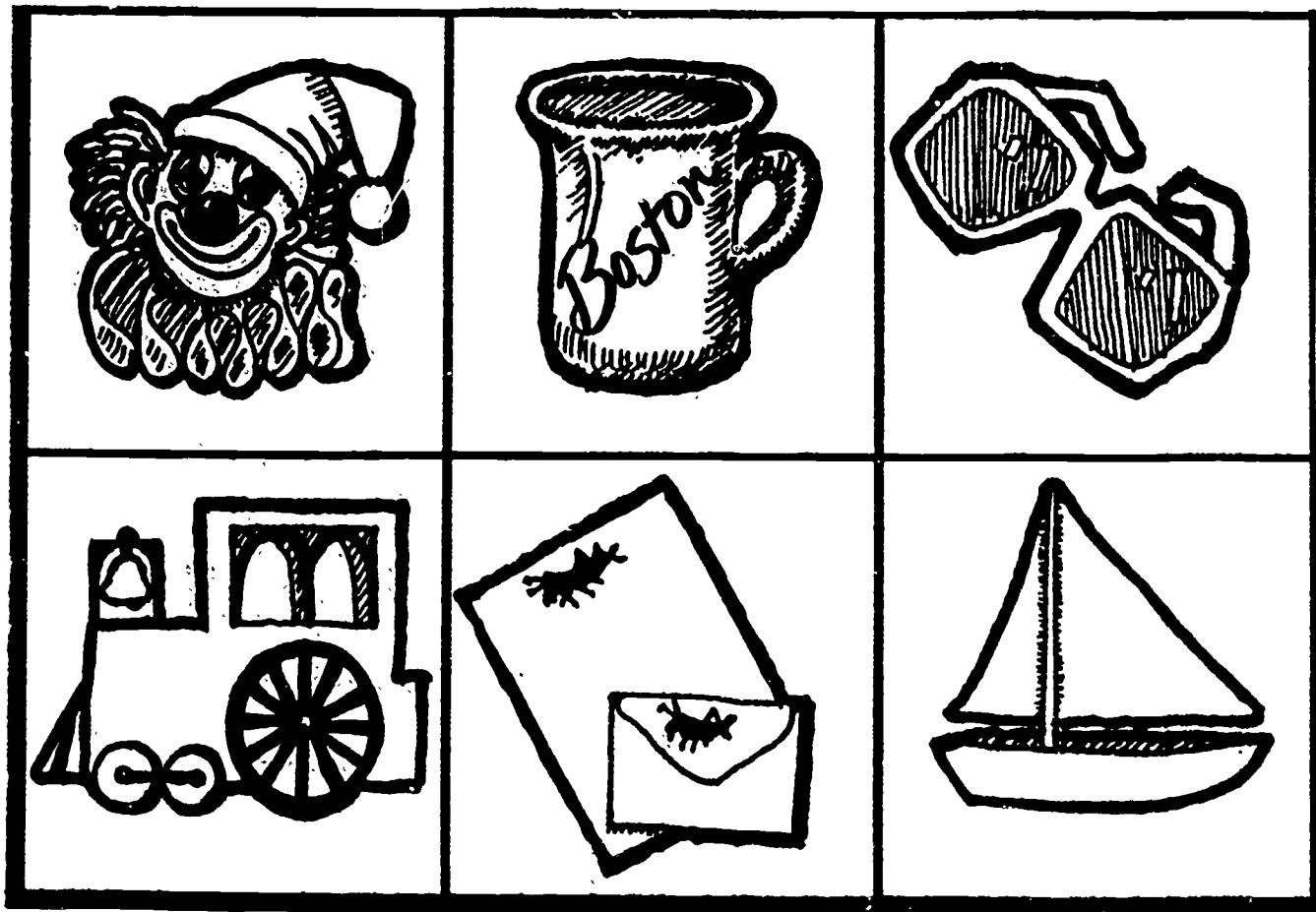
"The best way to get there is to fly in a straight line."

THE BULL



What's He Like?

He is the strong and proud symbol found atop the Quincy Market Building. He lends his name to the Bull Market pushcarts.



RULER

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FOLLOW THE RULER

<u>Topic/Objective</u>	<u>Materials</u>
Reading a Ruler Estimation Skills	Rulers Tape measure (optional)

During Class:

1. Using "Portia's Complaint" do the following: (overhead may be used to verify answers)
 - a. Introduce the ruler and discuss the divisions of an inch into $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$, $\frac{1}{16}$ inch segments.
 - b. Compare the divisions of an inch on the different rulers.
 - c. Ask students to mark various measurements on the rulers (e.g., find $2\frac{1}{2}$ and place an "A" there)
2. Have students estimate (do not allow rulers) and record their estimates on "Classroom Trivia" and/or "How do you Measure Up?"
3. Measure objects previously estimated and complete "Classroom Trivia" or "How do you Measure Up?" (Decide on appropriate degree of accuracy)

After Class

"Code to Portia"

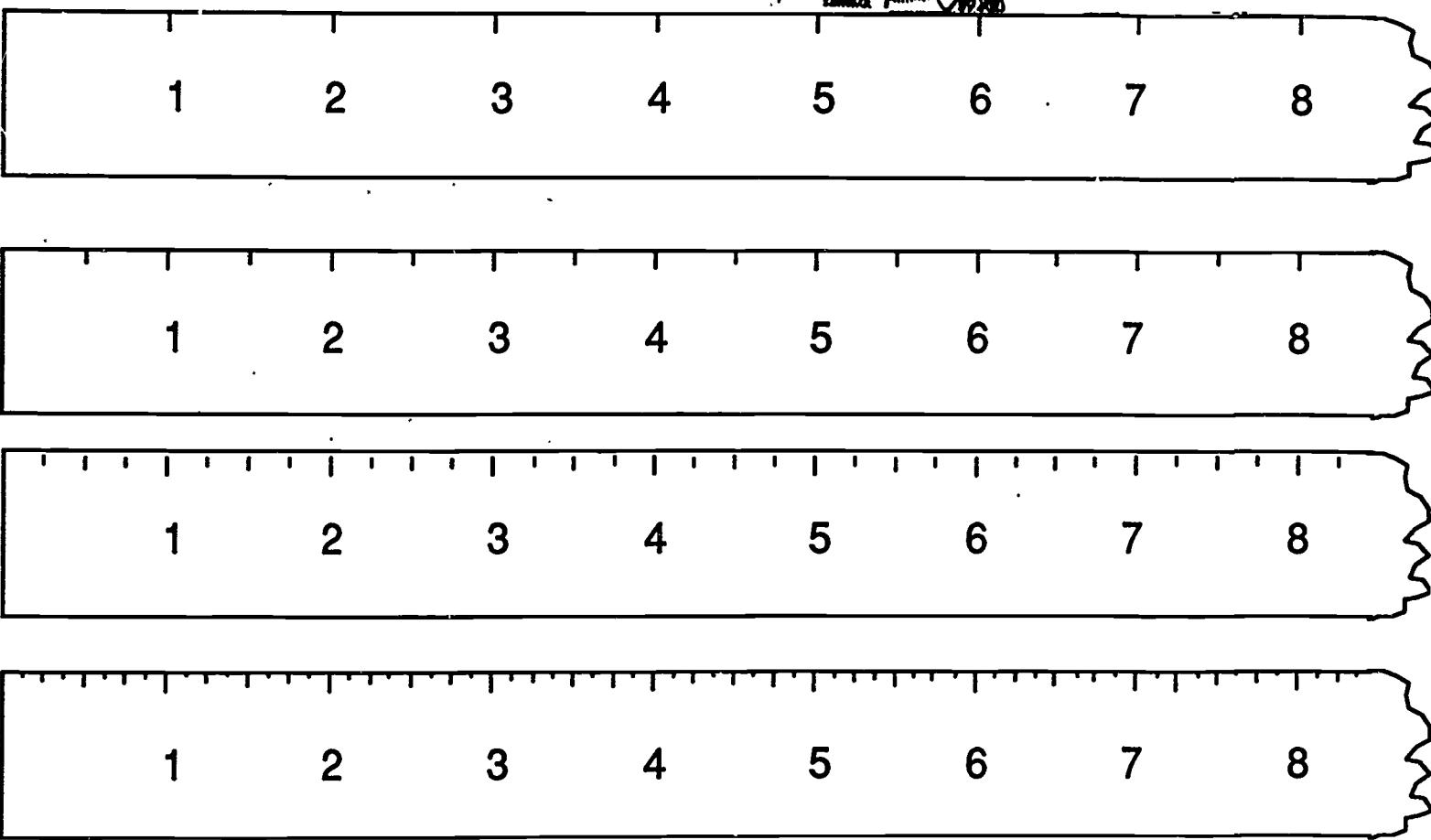
Reinforcement

Research the history of linear measurements and origins of specific units of measurement (e.g., inch, foot, yard)

Extension

PORTIA'S COMPLAINT

PORTIA: I was absent when you taught rulers. It's not my fault!



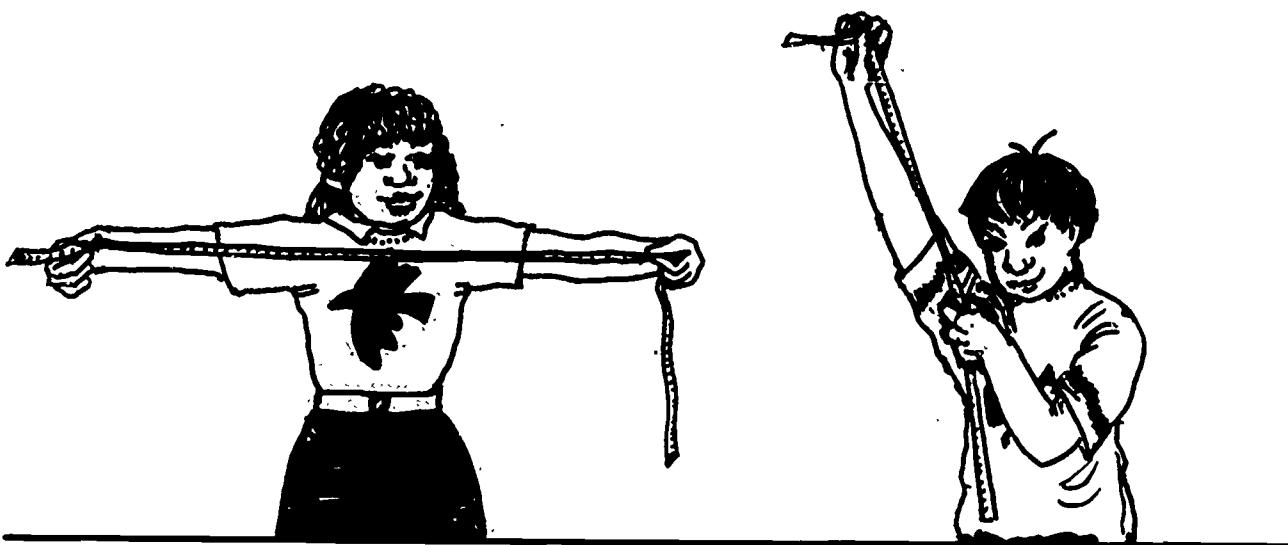
Class Activity

Class Activity



OBJECT	ESTIMATION	ACTUAL MEASUREMENT
Length of your desk		
Width of your desk		
Height of file cabinet		
Length of room		
Width of room		
Height of door		
Length of your book		
Thickness of desk top		
Diameter of clock		
Now think of your own (Less than 1")		
1)		
2)		
(Less than 1")		
1)		
2)		
(Less than 1 yard)		
1)		
2)		

HOW DO YOU MEASURE UP?



Object	Estimation	Actual Measurement (to nearest inch)
Height		
Arm span		
Hand span		
Head		
Foot		
Little finger		
Width across palm		
Width of thumb		
Length of smile		
Longest hair on your head		

Some interesting measurements!

Distance from nose to end of extended arm is approx. 36" (adult).
Span of hand is approx. 7 inches. Sheet of paper is 8 1/2" X 11".
Pens are approx. 6" long.

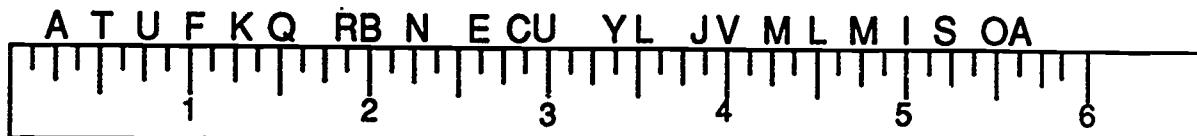
Now use the back of your paper to write 5 ratios comparing the lengths of various parts of your body.

CODE TO PORTIA

To help Portia with her ruler skills, Horatio has left her a secret message which she must decode by reading these rulers.

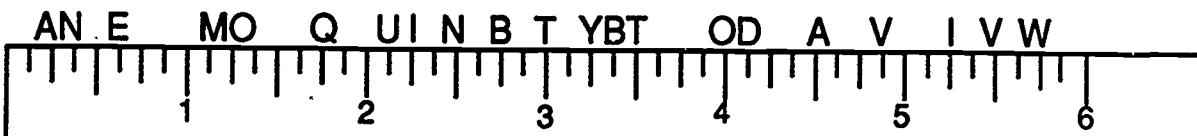
- I will meet you at

1 1/2, 3/4, 5, 2 1/4, 2 7/8, 3 3/8, 4 1/4, 5 5/8, 1 7/8, 1 1/4, 2 5/8, 1/2



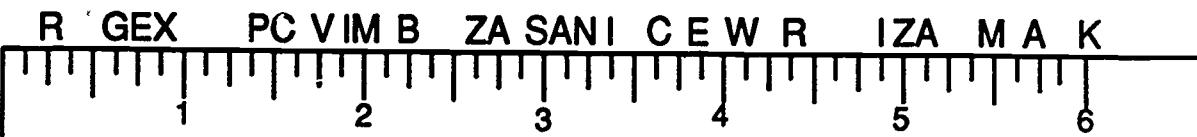
- around

2 1/2, 4, 1 1/4, 3/8, 3 1/2, 5 1/4, 1 1/8, 5/8



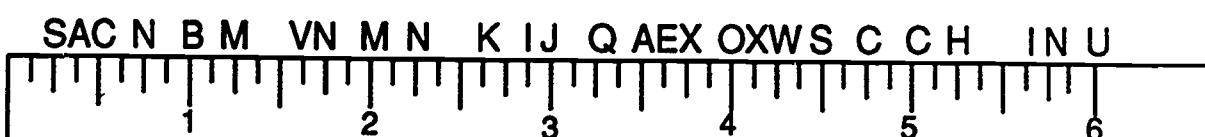
- We should plan to meet at

1 3/8, 3 3/8, 2 5/8, 5, 3 7/8, 4 3/8, 1 7/8, 5 3/4, 1/4, 6/8, 5/8, 4 7/8, 3 1/4, 2 3/4



- Do you want pepperoni, mushroom, onion pepper, or

?
3 1/2, 2 1/4, 4/8, 5 1/4, 4, 1 5/8, 2 7/8, 3 5/8, 4 1/2



WHERE'S MY CART?

<u>Topic/Objective</u>	<u>Materials Needed</u>
Reading a Ruler	Rulers
Estimating Skills	

During Class:

Use "The Name Game" and/or "The Match Game" to reinforce skills.

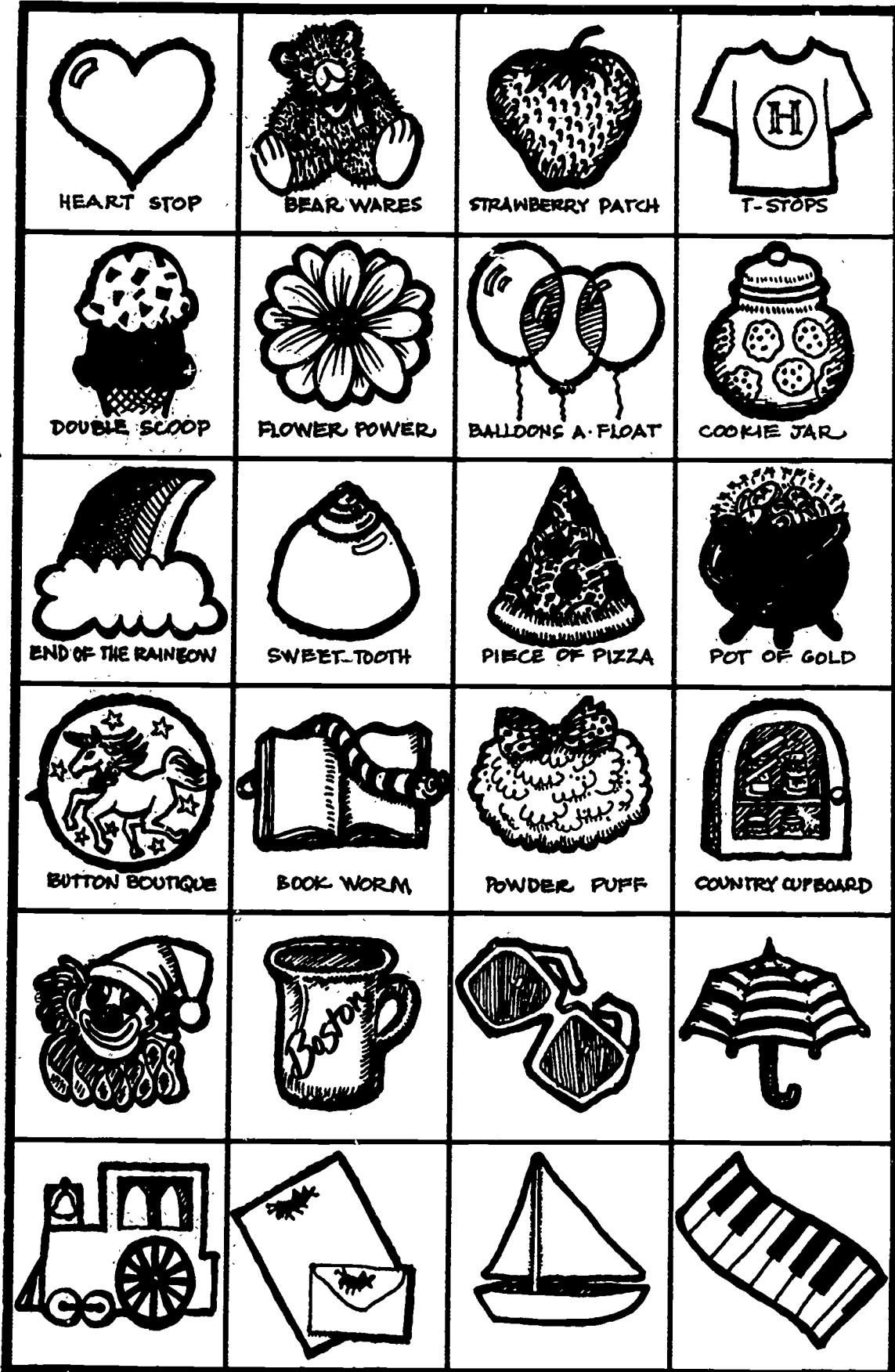
After Class

"Take the Bull by the Horns"

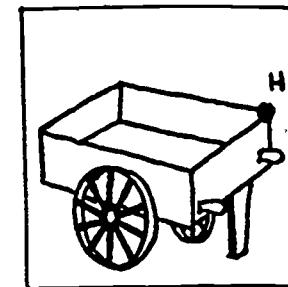
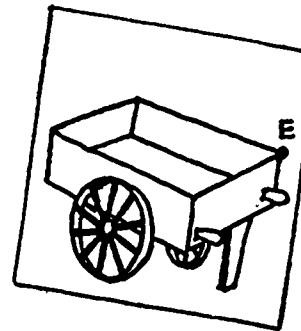
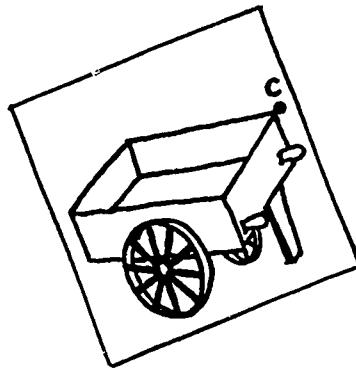
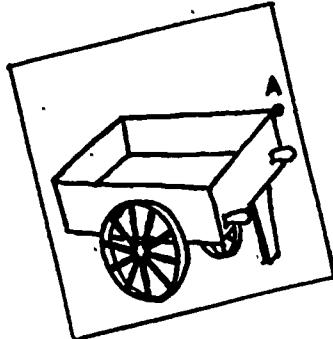
Extension

STICKER SHEET FOR BULLMARKET LESSONS

THE MATCH GAME
THE NAME GAME
TAKE THE BULL BY THE HORNS



THE MATCH GAME



GRASSHOPPER:

You know, I'm the symbol of Faneuil Hall Marketplace.

CROW:

Well, I'm the symbol of logic and common sense.

HORATIO:

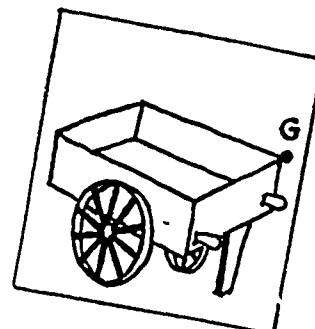
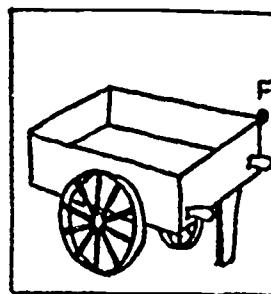
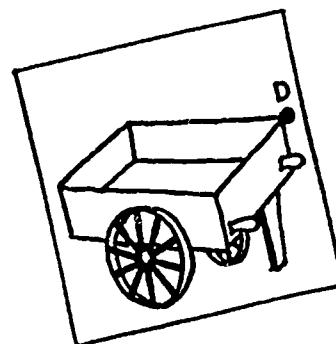
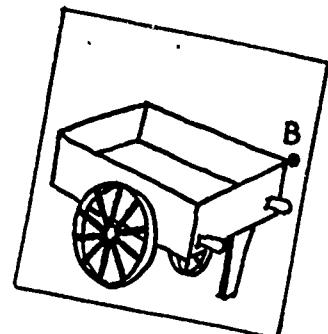
And I know how to match all the carts with their symbols.

GRASSHOPPER:

How can you do that?

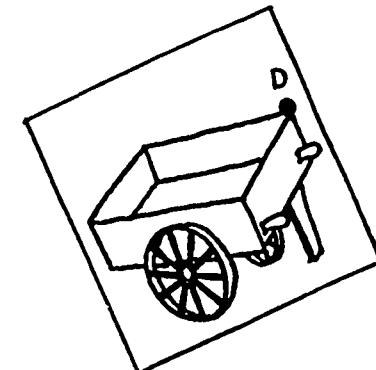
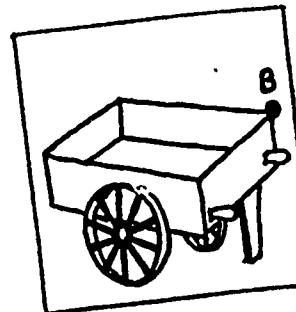
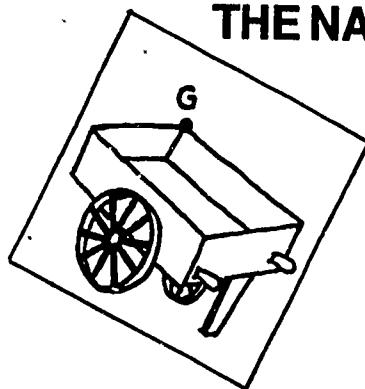
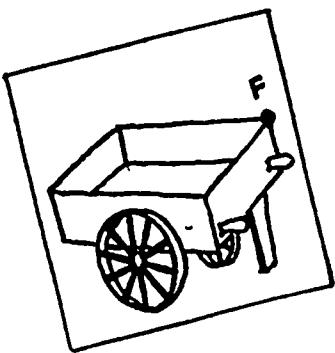
HORATIO:

I learned how to measure! I'll show you how!



Directions: Find each cart by measuring from dot to dot. Cut out the stickers from the sticker sheet for Bull Market Lessons and paste on each cart correctly.

1. From A to the Cookie Jar cart is $4\frac{1}{4}$ ".
2. From C to the Bear Wares cart is $2\frac{3}{4}$ ".
3. The Strawberry Patch is $2\frac{1}{4}$ " from the Cookie Jar.
4. The T-Stops cart is $3\frac{1}{4}$ " from C.
5. Heart Stop is $2\frac{1}{4}$ " away from The Strawberry Patch.
6. The Double Scoop is $6\frac{3}{4}$ " from D.
7. The Flower Power cart is $3\frac{1}{4}$ " from T-Stops.
8. $9\frac{1}{4}$ " from Bear Wares is Balloons-A-Float.



HORATIO: I'm not sure where all the carts are in the Bull Market.

PORTIA: It's perfectly obvious to me where they are!

CROW: O.K. then, Portia, where's **The Country Cupboard**?

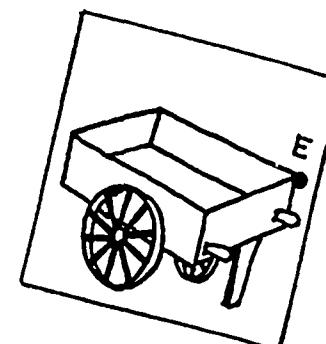
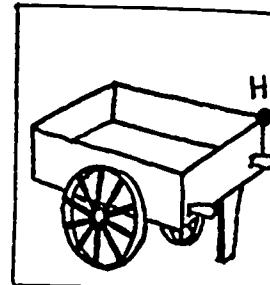
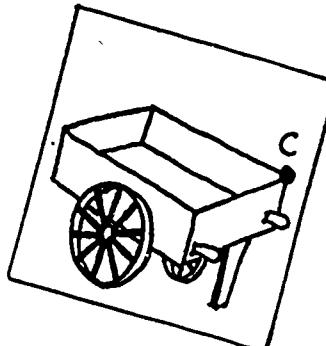
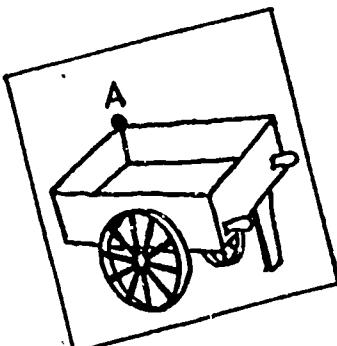
PORTIA: Well, it's, uh, um..., over there, near the, uh, um, or I think maybe it's near the ...

CROW: I think there's a way we can measure and figure out where they are!

THE NAME GAME

Directions: Find each Cart by measuring from dot to dot. Cut out the stickers from the sticker sheet for Bull Market Lessons and paste on each cart correctly.

1. From A to the **Sweet Tooth** is $7 \frac{1}{2}$ ".
2. **Piece of Pizza** cart is $3 \frac{1}{2}$ " from **End of the Rainbow**.
3. $2 \frac{1}{2}$ " from B is the **Pot of Gold** jewelry cart.
4. The **Button Boutique** is $5 \frac{1}{2}$ " from **Pot of Gold**.
5. The distance from **Button Boutique** to **Book Worm** is $9 \frac{1}{2}$ ".
6. The **Powder Puff** is 2" from **Book Worm**.
7. **The Country Cupboard** is $6 \frac{1}{2}$ " from cart G.
8. **End of the Rainbow** is $5 \frac{1}{4}$ " from **Sweet Tooth**.



TAKE THE BULL BY THE HORNS

DIRECTIONS:

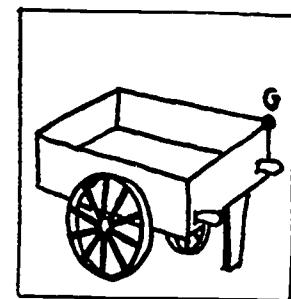
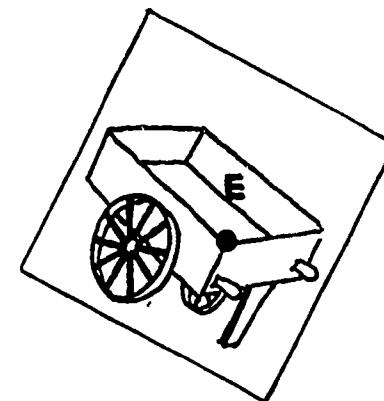
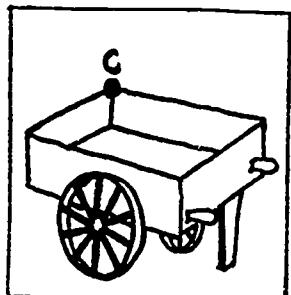
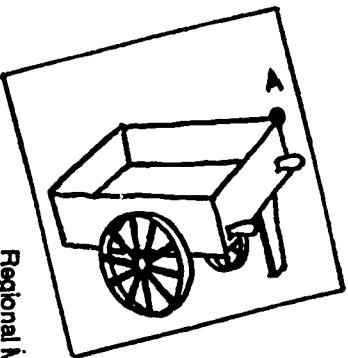
1. Name each cart. Use the "Take the Bull by the Horns" sheet. Put an appropriate symbol in each cart (or create your own). Save this as an answer sheet.
2. Write a set of directions for the points similar to the Bull Market Cart lessons.

PUZZLES BY _____ (YOUR NAME)

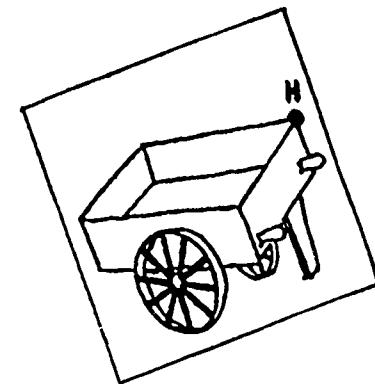
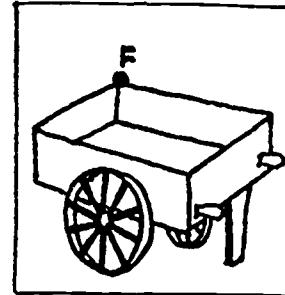
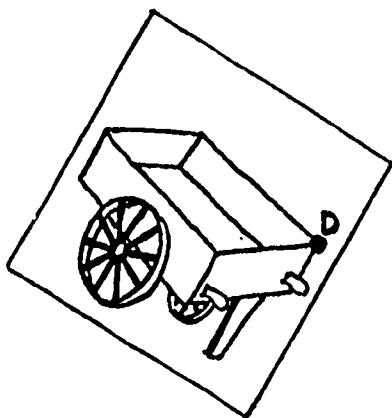
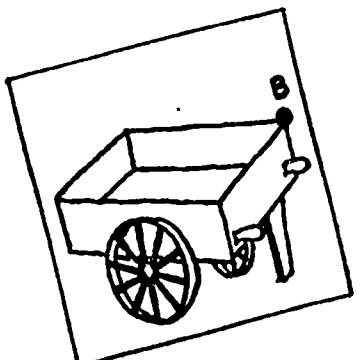
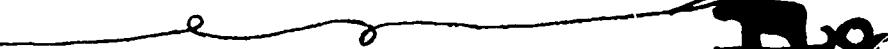
DIRECTIONS:

1. From point A to _____ measures _____.
 2. _____
 3. _____
 4. _____
 5. _____
 6. _____
 7. _____
 8. _____
 9. _____
 10. _____
 11. _____
 12. _____
-
-

Are you an expert game creator? Give your directions and a blank Bull Market Cart sheet to a classmate to solve.



Take the Bull by the Horns.



LINE UP

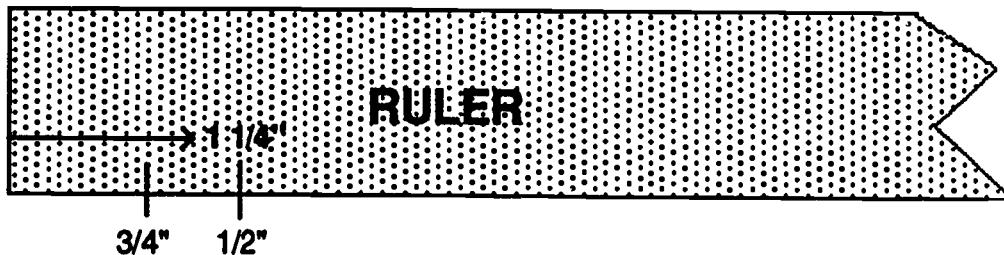
<u>Topic/Objective</u>	<u>Materials</u>
Measuring to nearest 1/8"	Rulers Adding Machine Tape or masking tape (1 yd. for every 2-3 students.) Length cards, cut a sufficient number for all groups and put each set in a container.

During Class:

Arrange class into groups of two or three students. Students take turns drawing a length card and marking off the lengths indicated on their tape. First group to complete the length of their tape wins. Groups check each other's work.

Example:

First student chooses $\frac{3}{4}$ " and marks that length on tape.
Next student chooses $\frac{1}{2}$ " so must mark $1\frac{1}{4}$ " on the tape.

**After Class**

"As the Grasshopper Hops"

Extension

LENGTH CARDS

7/8"	1 3/4"	3 7/8"	5"
5/8"	1 1/4"	3 3/4"	4 7/8"
3/8"	1 1/2"	3 1/2"	2 5/8"
1/8"	4"	2 7/8"	4 1/2"
3/4"	3"	2 3/8"	3 3/8"
1/4"	2"	2 1/8"	4 5/8"
1/2"	1"	2 1/2"	4 3/4"

AS THE GRASSHOPPER HOPS

Use the Boston Back Bay Map.

Measure all map lengths of streets to the nearest 1/4".

YOU MUST TRAVEL ONLY ON THE STREETS.

1. Measure the map length of Marlborough Street. _____ (Note
Marlborough Street runs from Massachusetts Avenue to Arlington
Street.)
2. Measure the map length of Gloucester Street. _____
3. Find the shortest distance from the corner of Fairfield Street and Beacon
Street to the corner of Dartmouth Street and Newbury Street.

Using different streets, find another route to reach the same destination.
Record the distance and explain your route. _____

4. Traveling from the corner of Boylston Street and Hereford Street to the
corner of Exeter Street and Newbury Street , how many different routes
can you find? _____
5. How many inches will the grasshopper travel on this map route:

Begin at the corner of Massachusetts Avenue and Beacon St.
Hop down Beacon St. and turn right on Hereford St.,
Hop down Hereford St. and turn left on Newbury St.,
Hop down Newbury St. and turn left on Dartmouth St.,
Hop down Dartmouth St. and turn right on Marlborough St.,
Hop to Berkeley St.

If 1 inch = 1/8 mile, approximately how many miles would the
grasshopper have traveled if he took the real trip?

6. If a three inch grasshopper can hop approximately twenty times his length,
how many hops will it take him to cover the route in question five?
This is tough! _____

AS THE GRASSHOPPER HOPS (II)

7. Find the spot:

Begin at the corner of Arlington St. and Newbury St. and go
1 1/2" down Newbury St.
Turn right and go 2 3/4".
Turn left and go 3 1/4".
Turn left and go 3 3/4"
Turn right and go 1 1/2"

Use street names to tell where you would be at the end of the trip.

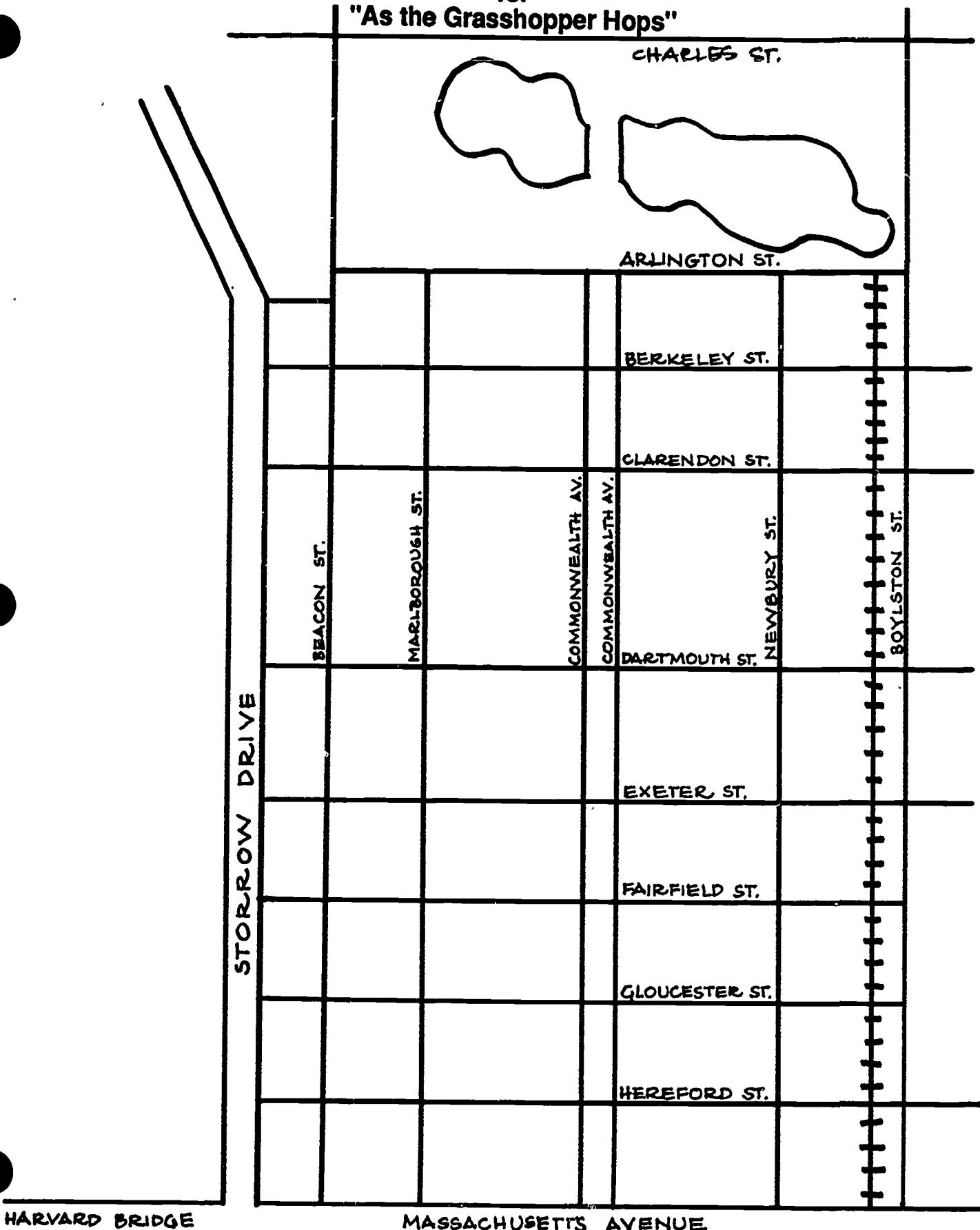
Approximately how many miles would this trip be if 1" = 1/8 mile?



Boston Back Bay Map

for
"As the Grasshopper Hops"

Extension



AS THE GRASSHOPPER HOPS

Extension

Use the Boston Back Bay Map.

Measure all map lengths of streets to the nearest 1/4".
YOU MUST TRAVEL ONLY ON THE STREETS.

1. Measure the map length of Marlborough Street. $7\frac{1}{4}$ " (Note Marlborough Street runs from Massachusetts Avenue to Arlington Street)

2. Measure the map length of Gloucester Street. 5"

3. Find the shortest distance from the corner of Fairfield Street and Beacon Street to the corner of Dartmouth Street and Newbury Street.
 $5\frac{1}{4}"$

Using different streets, find another route to reach the same destination. Record the distance and explain your route.

4. Traveling from the corner of Boylston Street and Hereford Street to the corner of Exeter Street and Newbury Street, how many different routes can you find? 4 ways of the shortest route.

5. How many inches will the grasshopper travel on this map route:

Begin at the corner of Massachusetts Avenue and Beacon St.
Hop down Beacon St. and turn right on Hereford St.,
Hop down Hereford St. and turn left on Newbury St.,
Hop down Newbury St. and turn left on Dartmouth St.,
Hop down Dartmouth St. and turn right on Marlborough St.,
Hop to Berkeley St.

$12\frac{1}{2}$ "

If 1 inch = 1/8 mile, approximately how many miles would the grasshopper have traveled if he took the real trip?

$1\frac{1}{2}$ miles

6. If a three inch grasshopper can hop approximately twenty times his length, how many hops will it take him to cover the route in question five?
This is tough! 1584 hops

AS THE GRASSHOPPER HOPS (II)

Extension

7. Find the spot:

Begin at the corner of Arlington St. and Newbury St. and go
1 1/2" down Newbury St.
Turn right and go 2 3/4".
Turn left and go 3 1/4".
Turn left and go 3 3/4".
Turn right and go 1 1/2"

Use street names to tell where you would be at the end of the trip.

The corner of Hereford St. and Boylston St.

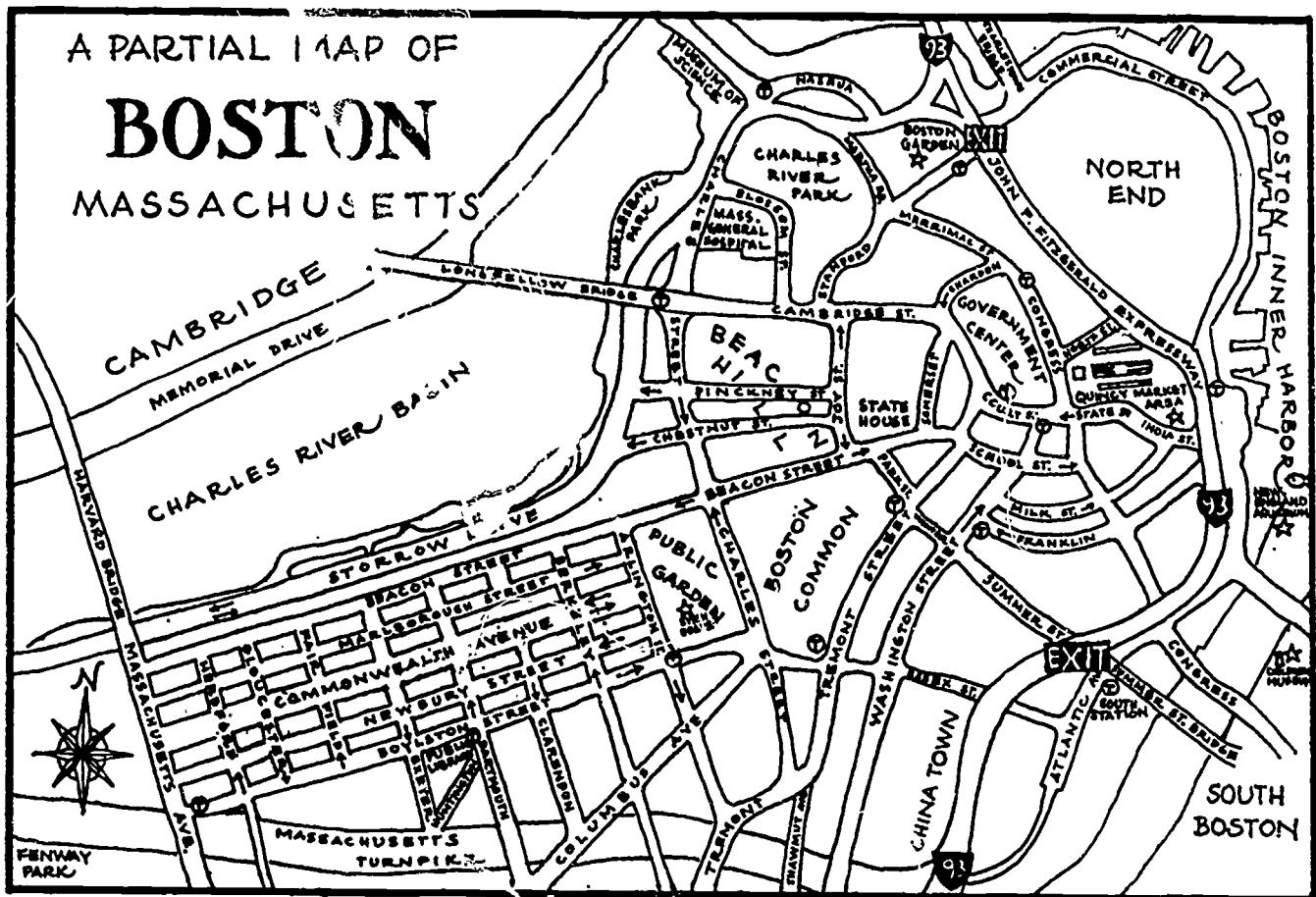
Approximately how many miles would this trip be if 1" = 1/8 mile?

$1\frac{5}{8}$ miles.



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map exploration

MAP EXPLORATION

<u>Topic/Objective</u>	<u>Materials</u>
Coordinate System, Scales, Ratio and Proportion Distances within a Specific Circle	Boston and Vicinity Map Review map and coordinates before class

During class:

1. Introduce the Boston and Vicinity Map.
 - a. Arrange students in groups and let them examine the map for 5 minutes.
Discuss and list some of the pertinent information.
 - b. Locate Quincy Market and your town. Discuss possible routes between them.
2. Discuss coordinates.
3. Play a game "I'm thinking of a town." (Student says "I'm thinking of a town in G-4.") Other students must identify that town (same idea as 20 questions). Questions must be ones requiring only a "yes" or "no" answer.

After Class

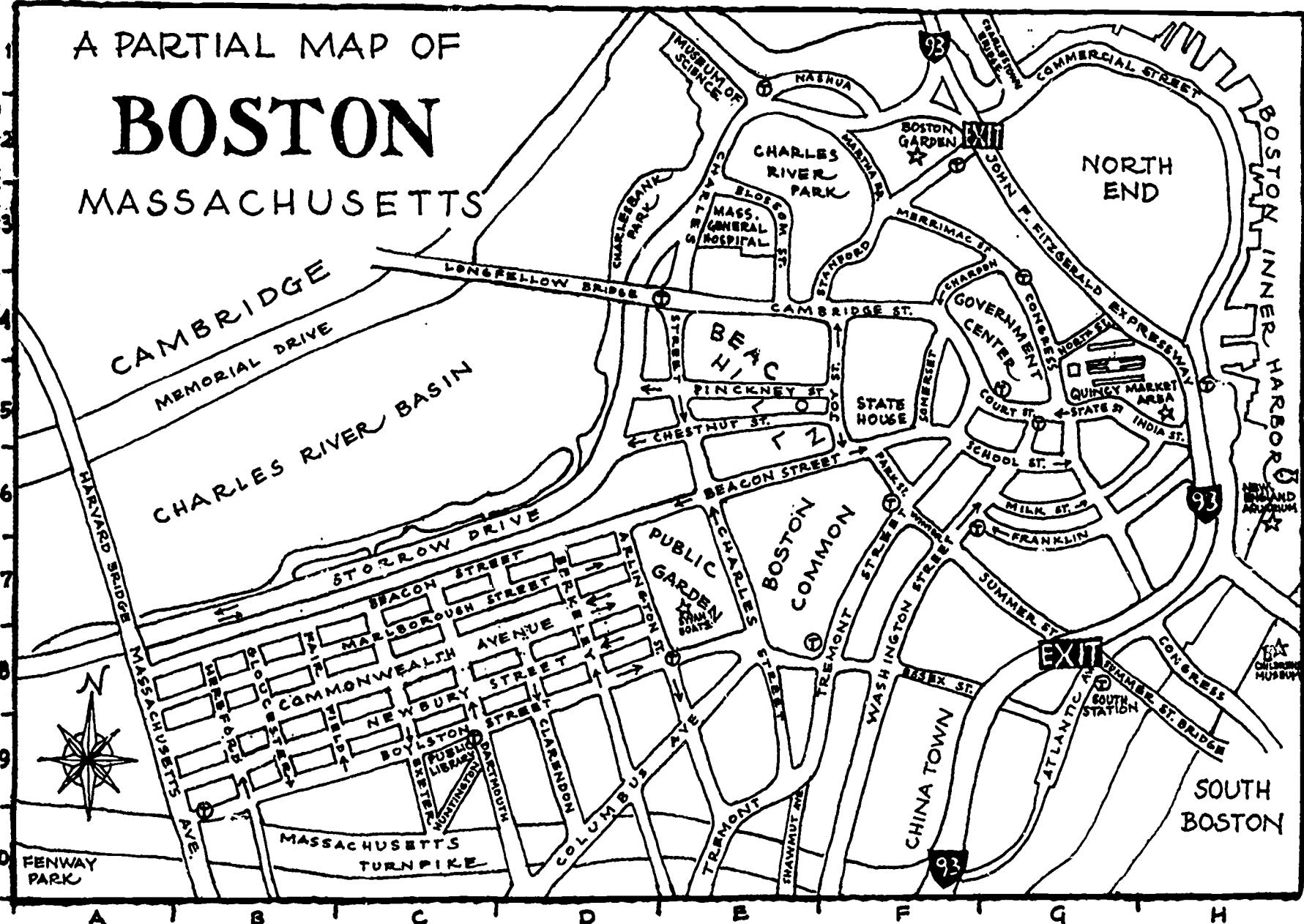
Partial Map of Boston

Extension

Have students generate questions about this map or write your own questions on the board. (e.g. Give the coordinates for Fenway Park or what town is found in A10?)

A PARTIAL MAP OF
BOSTON
MASSACHUSETTS

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BOSTON AND VICINITY

<u>Topic/Objective</u>	<u>Materials</u>
Scales - Ratio and Proportion Distances within a specific radius	Boston and Vicinity Map Rulers, String, Compass, or Circle transparencies (masters included)

During class:

1. Calculate distances using scale measure.

Have the student:

- a. Give the scale measure of the map ($1'' = 2$ miles).
- b. Measure approximate mileage between two towns by measuring from the first letter of one to the first letter of the other. Explain that we have chosen this method because it is well defined, but the method can be misleading. Is it really only one mile from Belmont to Arlington--should we measure from center of town to center of town? Can we tell the center of town from this map? Can anyone think of another accurate method?

- | | |
|--|--|
| 1. <u>Newton to Chelsea</u> (9 miles)
2. <u>Brookline to Medford</u> (7 1/2 miles)
3. <u>Lexington to Bedford</u> (4 miles)
4. <u>Boston to Newton</u> (8 miles)
5. <u>Holliston to Wellesley</u> (10 1/2 miles) | 6. <u>Dedham to Hingham</u> (14 miles)
7. <u>Acton to Natick</u> (15 1/2 miles)
8. <u>Peabody to Revere</u> (9 miles)
*9. Your town to other towns.
*10. Your town to Quincy Market. |
|--|--|

2. Determine distance using a radius and make a chart. (optional)

Review the meaning of the term radius and teach students how to determine towns within a specific circle using transparencies, string, or compass.

Have the student:

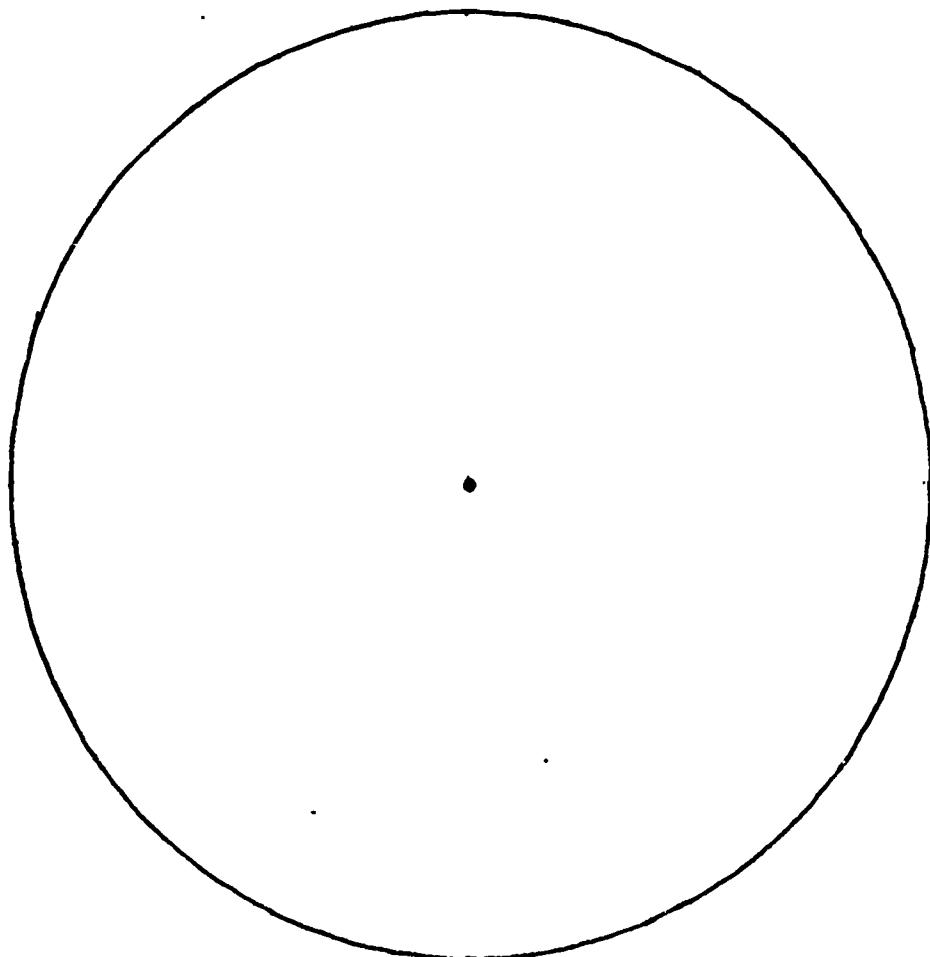
- a. List the towns within a 5 mile radius of Winchester and record.
(Lexington, Arlington, Belmont, Medford, Malden, Melrose, Stoneham, Woburn, Burlington)
- b. List the towns within a 6 mile radius of Watertown and record.
(Arlington, Medford, Somerville, Cambridge, Brookline, Newton, Waltham, Belmont)
- c. List those towns that are in both sets. (Arlington, Belmont, Medford)

After Class

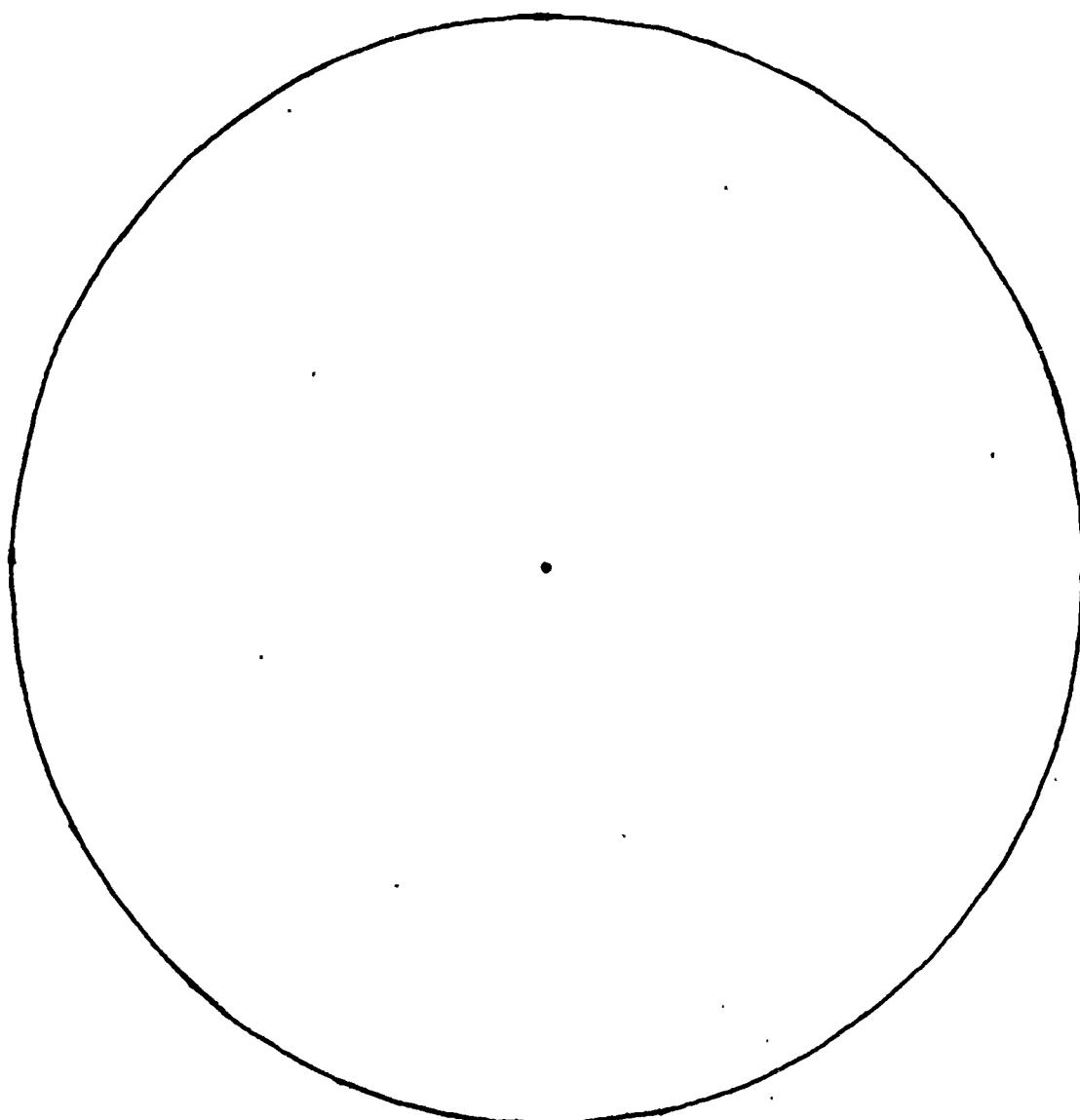
"Routes from Boston"

Extension

5" Circle Transparency

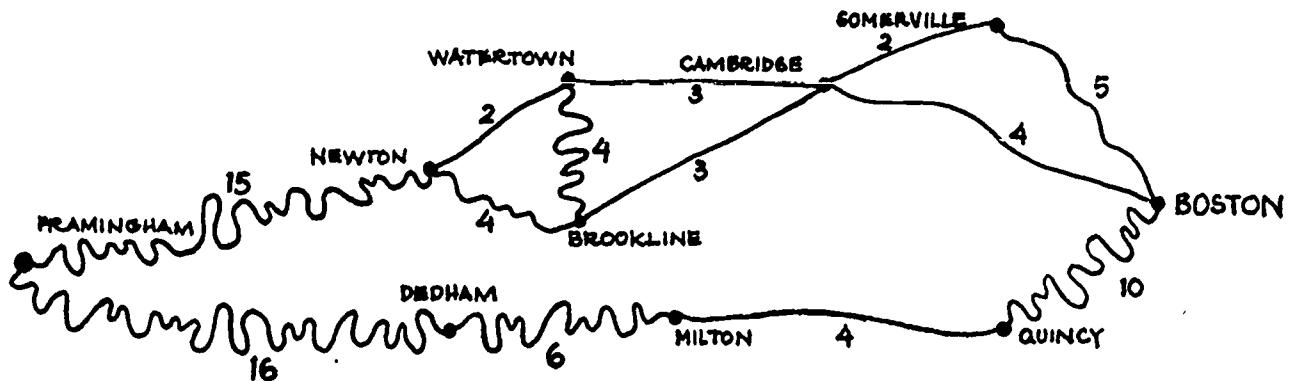


6" Circle Transparency



59

ROUTES FROM BOSTON



1. How many miles is it from Boston to Cambridge to Watertown to Newton?

 2. How many miles is it from Boston to Cambridge to Brookline to Newton?

 3. How much further is it from Boston to Newton if you go through Somerville than if you take the most direct route? _____
 4. Make a list of 2 different routes you can take from Boston to Framingham if you can't pass through the same city/town twice? Show the cities in order, using the first letter of each city name. Reminder: Use BO for Boston and BR for Brookline.

Example: ROUTE TOTAL NUMBER OF MILES
BO-C-W-N-F 20

Now find two other routes from Boston to Framingham.

5. What is the shortest route from Boston to Framingham?
How many miles? _____

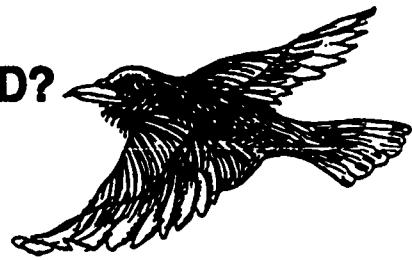
6. How many miles is the longest route from Boston to Framingham if you
can't pass through the same town/city twice? _____

7. Find a route which leaves Boston and visits every town/city just once and
ends back in Boston. _____

How many miles is it? _____

Is there more than one route? _____

WHERE DOES THE CROW LAND?



<u>Topic/Objective</u>	<u>Materials</u>
Scale Linear Measure	Massachusetts map Push pins or thumbtacks 1 set of Crow cards

During class:

1. Arrange students in groups of 4-5. Give each group a map. Note that now students will measure from the centers of towns, not from first letters of names.
2. Give each group the same crow card. The group decides using the map where the push pin should be placed.
3. Choose a group at random to place the push pin on the bulletin board map. That group assigns a member to go to the bulletin board.
4. The other groups verify that the push pin has been correctly placed. If the pin was incorrectly placed, another group may try. Points should be awarded for correct placement and subtracted for incorrect placement.

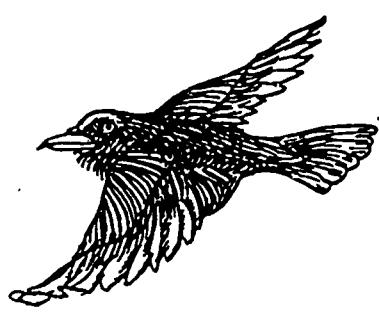
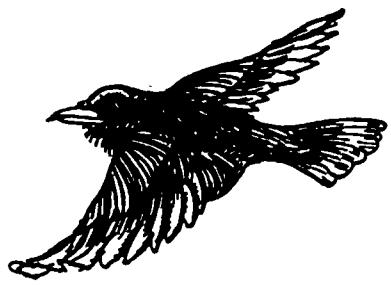
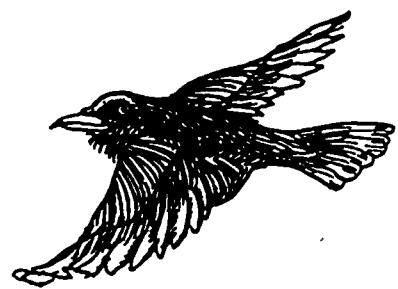
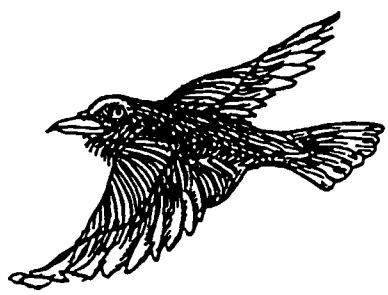
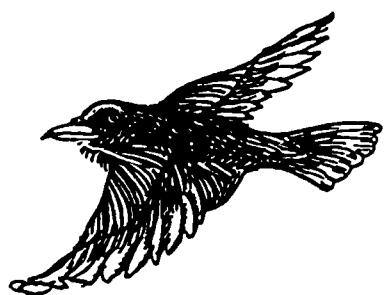
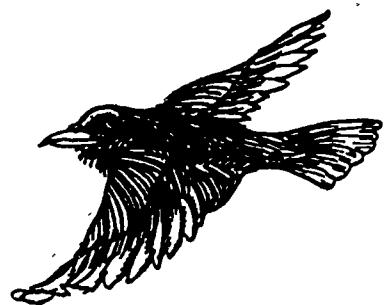
After Class

Have students write their own crow cards to add to the deck

Have students develop a system for noting which push pin matches each crow card.

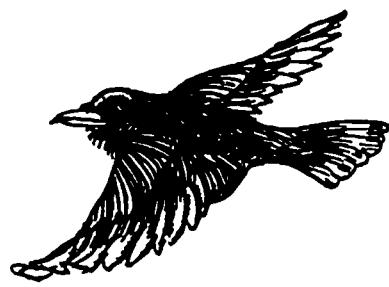
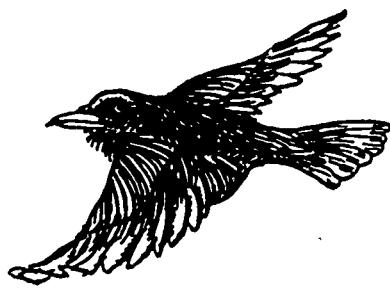
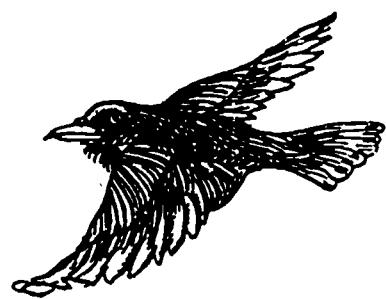
WHERE DOES THE CROW LAND?

# 1 The crow starts in Boston and flies 18 miles towards Lowell. Where does he land?	# 2 The crow starts in Lawrence and flies 21 miles toward Gloucester. Where does he land?	# 3 The crow starts in Chicopee and flies 33 miles toward Fitchburg. Where does he land?
# 4 The crow starts in Northhampton and flies 19.5 miles toward Fitchburg. Where does he land?	# 5 The crow starts in Chelmsford and flies 16.5 miles toward Needham. Where does he land?	# 6 The crow starts in Fall River and flies 43.5 miles toward Worcester. Where does he land?



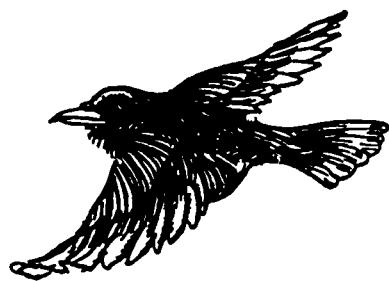
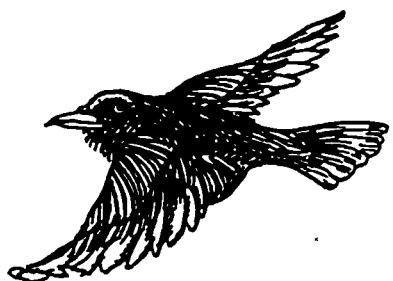
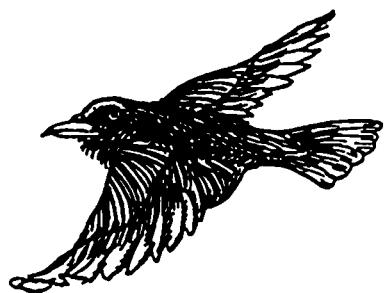
WHERE DOES THE CROW LAND?

# 7 The crow starts in Arlington and flies 19.5 miles toward Lunenberg. Where does he land?	# 8 The crow starts in Pittsfield and flies 51 miles toward Worcester. Where does he land?	# 9 The crow starts in Belmont and flies 45 miles toward Bourne. Where does he land?
# 10 The crow starts in New Bedford and flies 10.5 miles toward Nantucket State Forest. Where does he land?	# 11 The crow starts in Beverly and flies 26 miles toward Provincetown. Where does he land?	# 12 The crow starts in Lawrence and flies 4.5 miles toward Melrose. Where does he land?



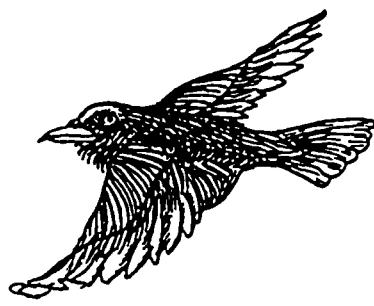
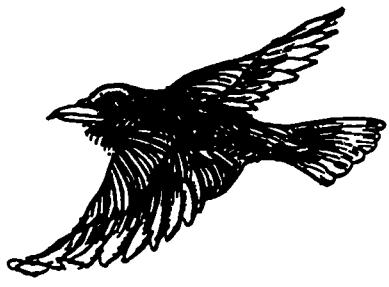
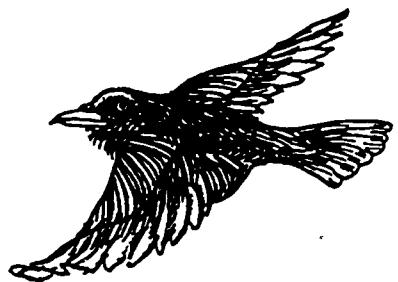
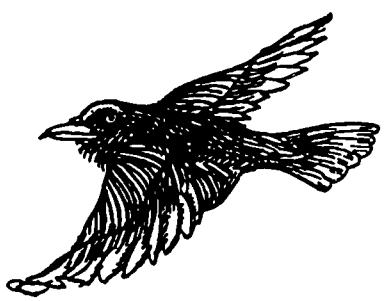
WHERE DOES THE CROW LAND?

# 13 The crow starts in Cambridge and flies 9 miles toward Sudbury. Where does he land?	# 14 The crow starts in Palmer and flies 16.5 miles toward Stockbridge. Where does he land?	# 15 The crow starts in Pittsfield and flies 60 miles towards Fitchburg. Where does he land?
# 16 The crow starts in Foxborough and flies 60 miles toward Amherst. Where does he land?	# 17 The crow starts in Holden and flies 6 miles toward Hudson. Where does he land?	# 18 The crow starts in Newburyport and flies 12 miles toward Peabody. Where does he land?



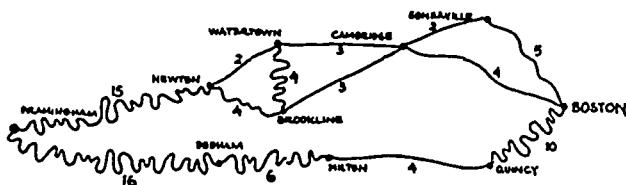
WHERE DOES THE CROW LAND?

# 19 The crow starts in Bridgewater and flies 42 miles toward Amesbury. Where does he land?	# 20 The crow starts in Westfield and flies 60 miles toward Groton. Where does he land?	# 21 The crow starts in Boston and flies 103 miles toward Pittsfield. Where does he land?
# 22 The crow starts in Framingham and flies 19.5 miles toward Brockton. Where does he land?	# 23 The crow starts in Palmer and flies 22.5 miles toward Ashburnham. Where does he land?	# 24 The crow starts in Lynn and flies 12 miles toward Gloucester. Where does he land?



ROUTES FROM BOSTON

Extension



- How many miles is it from Boston to Cambridge to Watertown to Newton? 9 miles
- How many miles is it from Boston to Cambridge to Brookline to Newton? 11 miles
- How much further is it from Boston to Newton if you go through Somerville than if you take the most direct route? 3 miles
- Make a list of 2 different routes you can take from Boston to Framingham if you can't pass through the same city/town twice? Show the cities in order, using the first letter of each city name. Reminder: Use BO for Boston and BR for Brookline.

Example: ROUTE TOTAL NUMBER OF MILES
BO-C-W-N-F 20

Now find two other routes from Boston to Framingham.

BO-C-B-N-F 26 miles

BO-Q-M-D-F 36 miles

- What is the shortest route from Boston to Framingham? BO-C-W-N-F How many miles? 24 miles
- How many miles is the longest route from Boston to Framingham if you can't pass through the same town/city twice? 36 miles
- Find a route which leaves Boston and visits every town/city just once and ends back in Boston. BO-Q-M-D-F-N-BR-W-C-S-BO

How many miles is it? 69 miles

Is there more than one route? yes

Answers for "Where Does the Crow Land?"

Start	Toward	Distance (miles)	Lands
1. Boston	Lowell	18	Billerica
2. Lawrence	Gloucester	21	Essex
3. Chicopee	Fitchburg	33	Barnie
4. Northampton	Fitchburg	19.5	Quabbin Reservoir
5. Chelmsford	Needham	16.5	Waltham
6. Fall River	Worcester	43.5	Northbridge
7. Arlington	Lunenburg	19.5	Littleton
8. Pittsfield	Worcester	51	Quabbin Reservoir
9. Belmont	Bourne	45	Myles Standish Park
10. New Bedford	Nantucket St. Forest	10.5	Buzzards Bay
11. Beverly	Provincetown	26	Massachusetts Bay (ocean)
12. Lawrence	Melrose	4.5	Andover
13. Cambridge	Sudbury	9	Waltham
14. Palmer	Stockbridge	16.5	Holyoke
15. Pittsfield	Fitchburg	60	Philipston
16. Foxborough	Amherst	60	Quabbin Reservoir
17. Holden	Hudson	6	Wachusett Reservoir
18. Newburyport	Peabody	12	Topsfield
19. Bridgewater	American	42	Danvers
20. Westfield	Groton	60	Leominster
21. Boston	Pittsfield	103	Peru
22. Framingham	Brookton	19.5	Stoughton
23. Palmer	Ashburnham	22.5	Barnie
24. Lynn	Gloucester	12	Manchester

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RATIO AND PROPORTION

YOUR RATIOS

<u>Topic/Objective</u>	<u>Materials</u>
Ratio	Total school population by grade and sex. See Appendix for other useful statistics.

During Class:

1. Introduce the concept of a ratio as a comparison of two quantities using the "Your Ratios" chart (2 out of 3, 2 to 3, 2:3, 2/3).

If class size is odd, you may choose to:

- add yourself
- add imaginary students
- use calculators

For school and town populations, you may choose to use rounded numbers.

2. Reduce ratios of larger numbers, if possible.

- The ratio of a vote of 140,000 to 200,000 is equivalent to the ratio of a vote of 7 to 10.
- If 400 out of 1000 people buy ginger ale, this ratio is equivalent to 2 out of 5 people buying ginger ale.

Simplify some examples from the chart.

3. Change some of these simplified ratios to percents.

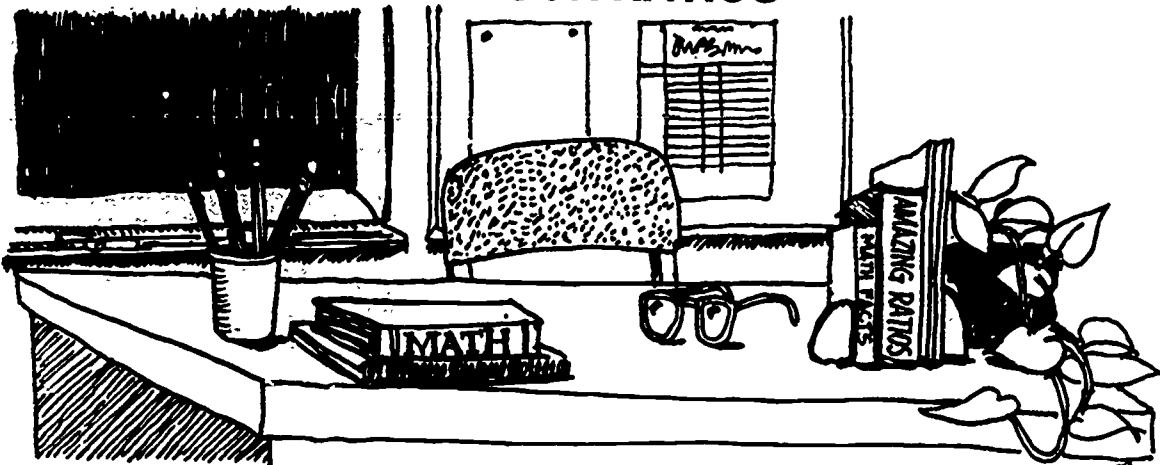
After Class

"Your Ratios"

Reinforcement

Add your own ratios and complete chart.

YOUR RATIOS



Your Classroom	Ratio	Simplified Ratio	Percent
Boys to total students			
Girls to total students			
Students to desks			
Blue-eyed students to total students			
Brown-eyed students to total students			
Left-handed students to total students			
Our class to total school population			
Population of seventh grade to town population			

Think of YOUR OWN RATIOS for the remaining spaces.

1.			
2.			
3.			
4.			

PORTIA PREDICTS

<u>Topic/Objective</u>	<u>Materials</u>
Proportions	"Your Ratios" completed for last night's homework

During Class:

1. Introduce the concept of proportion with examples on the board. A proportion is an equation that states that two ratios are equal.
 - A. Review from fractions:
Reducing: If 4 out of every 8 students will go on a field trip, and 47 students go on a field trip, how many students are there in all?

$$\frac{4}{8} = \frac{47}{?}$$

Expanding: If the ratio of boys to girls in your class is 4 to 5 and there are 15 girls in the class, how many boys are there in the class?

$$\frac{4}{5} = \frac{?}{15}$$

- B. Introduce cross multiplication:
 If I have a ratio of 2 candy bars for every 3 children, and I have 28 students, how many candy bars will I have?

$$\frac{\text{2 candy bars}}{\text{3 students}} = \frac{? \text{ candy bars}}{\text{28 students}}$$

2. Use "Your Ratios" to generate new examples and in particular to predict statistics for the school.

After Class:

"Portia Predicts"
 Textbook Examples of
 Cross Multiplication
 or Use QM data in Appendix
 to generate questions

Reinforcement

PORTIA PREDICTS

Portia watched what foods were being sold at Quincy Market. She learned some interesting things. Can you use her research to answer these questions?

Assume: Quincy Market is open 10 hours every day, 7 days a week.*

1. At the Taco Maker Horatio observed that 20 tacos were sold in 30 minutes.
At this rate, how many tacos would be sold in ...

<u> </u> tacos in 1 hour	<u> </u> tacos in 1 1/2 hours
<u> </u> tacos in 5 hours	<u> </u> tacos in 1 day
<u> </u> tacos in 1 week	<u> </u> tacos in 1 year

2. Portia was told the Pizzeria Regina sells an average of 600 pizzas per day.
At this rate, how many pizzas would be sold in ...

<u> </u> pizzas in 1 hour	<u> </u> pizzas in 5 hours
<u> </u> pizzas in 1 week	<u> </u> pizzas in 1 year

3. Horatio discovered the Boston Brownie sell 5 times as many brownies to adults as to young people, a 5 to 1 ratio. (Warning! This isn't a 1 to 5 ratio)

- 1) If they sell a total of 180 brownies in 1 hour, how many were sold to adults? _____ to young people? _____
- 2) How many brownies are sold in one day to adults? _____ to young people? _____
- 3) How many brownies are sold in one week to adults? _____ to young people? _____

* Actually, Quincy Market is only open 6 hours on Sunday but for this set of predictions assume it is open 10 hours on Sunday.

ONE OF THE CROWD

<u>Topic/Objective</u>	<u>Materials</u>
Ratio, Proportions, Estimation, Prediction	

During Class:

1. What is the ratio of the number of seventh graders in your home town to the number of visitors to Quincy Market?

Example:

In one year 14,000,000 people visited Quincy Market. If Cambridge seventh graders were the only visitors that year, how many times would each seventh grader have had to visit Quincy Market?

The ratio of Cambridge seventh graders to the number of visitors is:

$$\frac{500}{500 \text{ to } 14,000,000} \text{ or } \frac{1}{14,000,000} \text{ which reduces to } \frac{1}{28,000}$$

Every seventh grader would have had to visit Quincy Market 28,000 times that year.

2. How many times would each seventh grader in Boston have to visit Quincy Market in order to total 14,000,000 visitors?
3. You may choose to generate some other examples from this chart or add statistics about towns not listed.

Town	Est. Grade 7 Population (1986)
Boston	4500
Cambridge	500
Hingham	275
Chelmsford	425
Lexington	350
Somerville	450
Waltham	450
Lincoln	125
Marblehead	175
Acton	300
Medford	375

After Class:

"One of the Crowd"
"The Crowd According to Portia"

Reinforcement
Extension

ONE OF THE CROWD



HORATIO: There sure are a lot of people here at Faneuil Hall Marketplace!

CROW: About 14,000,000 people visit every year.

HORATIO: Suppose every seventh grader in my school visited Quincy Market.
How many times...

CROW: Poor Horatio. He'll never solve that one. We had better help him!

Town	Est. Grade 7 Population 1986	Town	Est. Grade 7 Population 1986
Boston	4500	Waltham	450
Cambridge	500	Lincoln	125
Hingham	275	Marblehead	175
Chelmsford	425	Acton	300
Lexington	350	Medford	375
Somerville	450		

Suppose your town decides to take every seventh grader in the town to Quincy Market for the day:

1. How many busses would you need if a school bus can carry 50 students? _____

What is the ratio of students to busses in your town? _____

2. How many pizzas will you order if every student eats two pieces of pizza on the trip and each pizza has eight slices? _____

What is the ratio of students to pizzas in your town? _____

3. One of the teachers took a survey on the way home and gathered the following information:

How many students bought

- 1/5 of the students bought T-shirts.
- 1/3 of the students bought jewelry.
- 3/4 of the students bought candy.

T-shirts? _____
Jewelry? _____
Candy? _____

4. Make up your own ratio questions about a trip to Quincy Market.

THE CROWD ACCORDING TO PORTIA



- PORȚIA:** Boy, it's certainly crowded in here!! I can hardly move.
- CROW:** Did you know that between twelve and fourteen million people visited Faneuil Hall Marketplace last year?
- GRASSHOPPER:** No! Come on!! That's more people than visited Disney World last year.
- PORȚIA:** It's perfectly obvious it's a reasonable estimate. In the last 15 seconds, I counted 16 people coming through that door. That's 64 in a minute. Wait a minute!! Where's my calculator?? Sixty-four times...

Did Portia estimate correctly? Check her figures.

(Hint: The market is open every day, 10 hours a day, Monday through Saturday.
On Sunday it's open 6 hours)

SURVEY INTRODUCTION

<u>Topic/Objective</u>	<u>Materials</u>
Survey techniques Ratio, proportion	Overheads of: Bull's Eye View of the Carts Portia's Survey

During class:

1. Discuss cart locations and products sold at Quincy Market.
Locate selected carts on overhead.
Use scale drawing on bulletin board to identify specific locations on overhead (i.e. rotunda, doors, stairs, selected restaurants).
2. (Optional) Use these facts to generate discussion of carts:
More than 1,000 different products are sold.
Only 1% of the carts do not succeed.
Cart rental is \$175 to \$250 per week.
4 to 5 applications for carts are received each week.
There is often a one-year waiting period to get a cart.
New carts have a two-week probation period.
3. Introduce the idea of a survey using overhead of Portia's Survey.
4. Take class surveys on: favorite ice cream, favorite pizza, etc.
5. Explain that we use the ratios determined in a survey (eg. 10 out of 30 students in the class like chocolate ice cream) to make predictions about a larger group using proportions. Explain that in some situations proportions give us a good estimate but only if the sample of students has similar tastes to the larger group.
6. Explain that in other situations our predictions are much more accurate (e.g., on a map, if the scale is 1" = 3 miles and the distance from Cambridge to Lexington is 2", we can accurately predict that the distance will be 6 miles).
7. Discuss "How Will You Make Your Fortune" with students. Have them complete this for homework.

After Class

"How Will You Make Your Fortune"

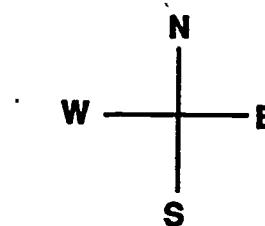
Reinforcement

A BULL'S EYE VIEW OF THE CARTS
(JULY 1986)

Overhead

58

Harbor →



Durgin-Park

1 2 3 4 5 6 7 8 9 10

11 12 13 14 15 16

17 18 19 20 21 22

23 24 25 26 27

28 29 30 31 32 33 34 35

36

37

38

39

40

41

Quincy Market Building

42

43

44

45

46

47 48 49 50 51

52 53 54 55 56 57 58 59 60

Key to a Bull's Eye View (Bull Market Carts, July 1986)

- | | | |
|-----|-----------------------------------|--|
| 1. | T-shirts | "Fanueil Hall" |
| 2. | Sun glasses | |
| 3. | T-shirts | "Boston" |
| 4. | Buttons | make your own |
| 5. | Christmas ornaments | personalized |
| 6. | <u>Just Dreaming</u> | pillows with sayings or names |
| 7. | Wild clothes | jams, dresses, Hawaiian shirts |
| 8. | Earrings | |
| 9. | Embroidery | pillows, scarfs, etc. |
| 10. | <u>Top Deck</u> | beach chairs |
| 11. | T-shirts | "Harvard", "Boston College" |
| 12. | <u>Scribbly Things</u> | color Boston picture (for young children) |
| 14. | <u>Mini Chimes</u> | all kinds of chimes |
| 15. | Hand Painted | welcome signs, thimbles, trinket boxes, refrigerator magnets |
| 16. | T-shirts | "Feed the World" |
| 17. | Personalized name posters | |
| 18. | <u>Sign Maker</u> | made to order |
| 19. | T-shirts | "Boston whale watching" |
| 20. | Posters and note paper | |
| 21. | T-shirts | "Boston Greeting Cod" |
| 22. | Coke hats | straws attached |
| 23. | Shells, plant hangers, and chimes | |
| 24. | <u>Tales and Tails</u> | stuffed animals |
| 25. | <u>Boston Fans</u> | cups, dishes, bumper stickers |
| 26. | T-shirts | "Boston" |
| 27. | Ceramic chimes | butterfly, rainbow |
| 28. | <u>Truly Boston</u> | visor caps, napkins, commuter mugs |
| 29. | T-shirts | Boston Lobsters, "I love Boston", Boston Beach Club |
| 30. | Pocket Book | wallets, bags |
| 31. | Jewelry | gold pins, charms |
| 32. | Glass | window sun catchers |
| 33. | <u>Li'l Lefty Shop</u> | bags, cups, playing cards |
| 34. | Dinosaurs | puzzles, school bags, stuffed animals |
| 35. | <u>Rainbow Connection</u> | belts |
| 36. | <u>Mail a Heart</u> | personalize your heart, earrings, pins |
| 37. | <u>Celebration</u> | clown dolls, door wreaths, bagel magnets |
| 38. | Straw bags | pocket books |
| 39. | Music theme | shopping bags, cups, hats, key chains, note paper, aprons |
| 40. | Cat theme | cups, banners, leashes, figurines, address books, placques |
| 41. | Glass | lanterns, floating candles |
| 42. | <u>Wizard Shop</u> | figurines, note paper, crystals |
| 43. | <u>Marcus and Me</u> | leather bags, belts |
| 44. | <u>Precious Cargo</u> | t-shirts, cups, bags |
| 45. | Leather bags | pocket book |
| 46. | <u>Cape Cod Porcelin</u> | lamps, vases, dishes |

Bull Market Carts (cont)

- | | |
|-----------------------------------|---|
| 47. Hand woven items | dresses, scarves, belts |
| 48. <u>Expressions by Chari</u> | umbrellas (with messages or names) |
| 49. Paintings | framed (Boston, etc.) |
| 50. <u>Calligraphy and Quotes</u> | plaques with quotes |
| 51. <u>Notable Names</u> | visor caps, baby clothes |
| 52. <u>Bagtime</u> | quilted bags, ties |
| 53. <u>Concord Hand Design</u> | pottery, plant pots |
| 54. <u>Salt Marsh Pottery</u> | hand-painted pottery, bells, boxes |
| 55. Ireland | Irish toilet paper, plaques, shirts, hats, etc. |
| 56. Handmade mice | door decorations and stuffed animals |
| 57. <u>Inkidinado</u> | rubber stamps |
| 58. American Cup | "American Cup" t-shirts, shorts, visors, mugs |
| 59. <u>Purple Panache</u> | bags, earrings, scarves, pins |
| 60. Greater Boston Tea Co. | t-shirts |

PORTIA'S SURVEY



PORTIA: It seems perfectly obvious to me that no one would want a Horatio T-shirt.

HORATIO: Well, I like it!

PORTIA: I think we should take a survey.

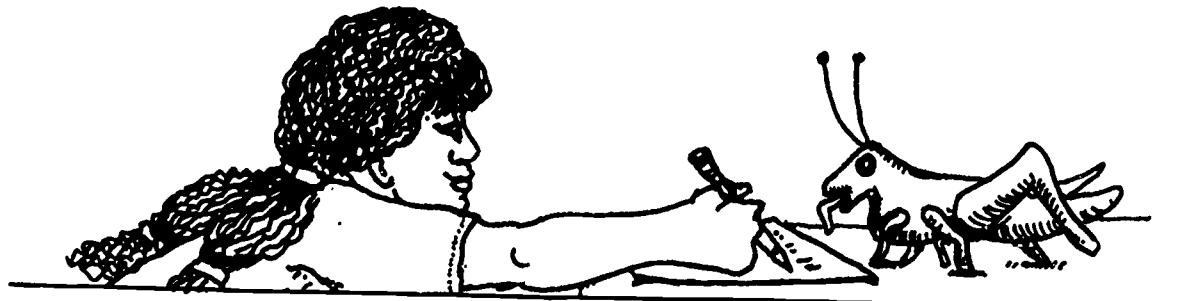
Portia's Survey

T-shirts		60
Jewelry	/	6
School Supplies	//	2
Stuffed Animals		9
Buttons	///	3
Total Survey		80



HOW WILL YOU MAKE YOUR FORTUNE?

Why not follow Portia's example.



Pretend you want to open a Bull Market cart at Quincy Market. Before you make your application you must decide what would be a profitable item to sell!

To do this you must:

- Choose 5 items to include in the survey and poll family and friends.
- Conduct your survey among 25 people of various ages.
- Record your information on the chart below.

's Survey

ITEM	TALLY	ITEM TOTAL	PERCENT
TOTAL			

Make up 5 questions using Your Survey results.

CREATING A BAR GRAPH

<u>Topic/Objective</u>	<u>Materials</u>
Survey techniques Graphing	Overhead of Portia's Survey Overhead of Steve's Ice Cream Bar Graph Large scaled graph paper (included) Construction paper (optional)

During class:

1. Review the techniques for and value of conducting a survey using Portia's Survey from previous lessons. Encourage students to give other examples.
2. Using the results of Steve's Ice Cream Survey, discuss bar graphs and the advantages of depicting information in graphical form. Guidelines for drawing bar graphs are included on Steve's Ice Cream Bar Graph.
3. Work through one of the bar graphs with students in class using Graph Your Stats.
4. (Optional) Discuss License Application which students complete after completing their bar graph.

After Class

"Tally-Ho!"
"Steve's Ice Cream Survey"

Reinforcement
Extension

STEVE'S ICE CREAM SURVEY

On a recent Tuesday afternoon Horatio took a 4 minute survey at Steve's Ice Cream Shop.



Flavor	Number of Cones Sold	Total
Cookie-O	/	12
Vanilla		—
Oatmeal Raisin		—
Maple Walnut	/	—
Chocolate Ripple	/	—
Strawberry	/	—

Total Number of Cones Sold in Four Minutes.

Steve's Ice Cream Bar Graph

Cones Sold in a 4-Minute Interval at STEVE'S

Your bar graph must have:

1. Title that tells what graph is about
2. Labels--on side and bottom of your graph that tell the kinds of facts listed and how many
3. Bars--horizontal or vertical, that are of equal width and equally spaced

Cookie-O

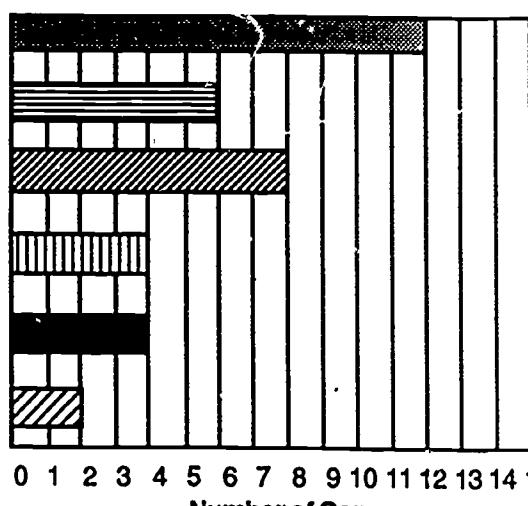
Vanilla

Oatmeal Raisin

Maple Walnut

Chocolate Ripple

Strawberry



GRAPH YOUR STATS

Your bar graph must have:

1. Title--that tells what graph is about
2. Labels--on side and bottom of your graph that tell the kinds of facts listed and the quantities of each
3. Bars--horizontal or vertical that are of equal width and equally spaced

Draw a bar graph for each of these tally sheets.

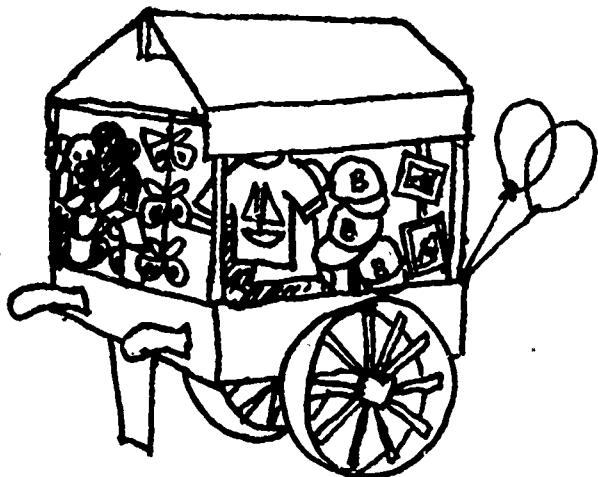
This tally sheet shows pounds of candy sold in one hour at Sweet Tooth in Quincy Market.

TALLY SHEET		
Gummi Bears	### ## /##	14
Licorice	###	5
Jelly Bears	### /##	9
Sweet Tarts	### //	7
M&M's	### ##	10

This sheet shows the results of a survey on adult size T-shirts sold at a T-shirts cart in Quincy Market in one day.

TALLY SHEET		
Small	###	5
Medium	### ##	10
Large	### ## #### ##	25
Extra Large	### ## #### ##	20

TALLY-HO!



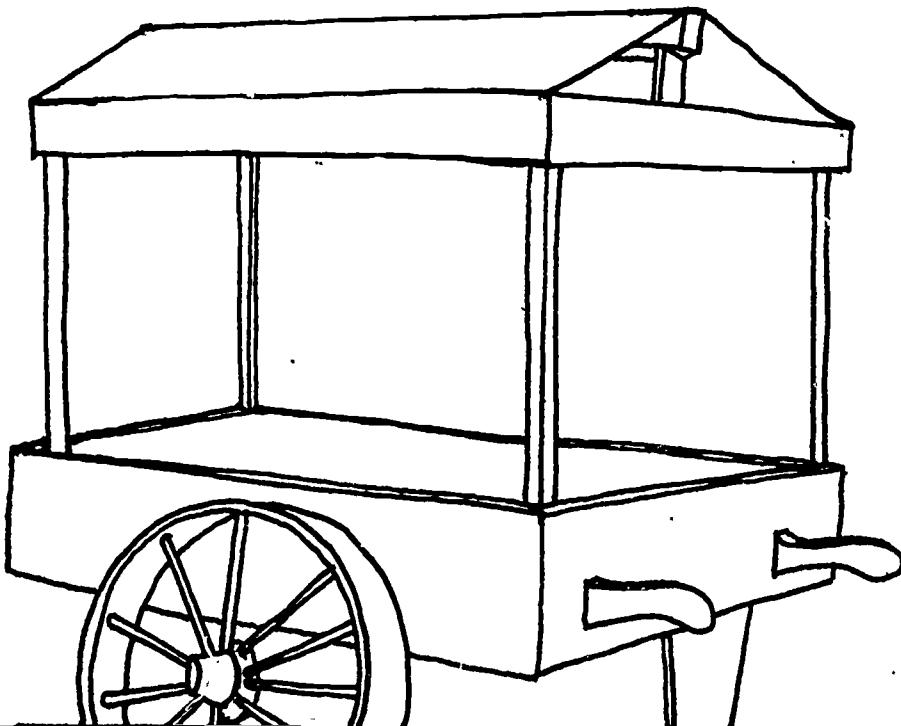
Use the information from your survey to create a bar graph of your information.

- 1. Check your survey tally and bar graph with your Quincy Market representative.**
- 2. When it is approved, ask for an application for a Bull Market License.**
- 3. Complete the license application carefully!**

Good luck!

APPLICATION FOR BULL MARKET LICENSE

Name	Homeroom number
Class Name	Teacher Name
Items to be merchandised	
Reasons for selecting above items	
Color scheme	
Name of cart	
How would the cart add to the festive spirit of the market place?	
Other information which might best describe your product and presentation	
Signature	Date



Please color in this drawing of a Bull Market cart showing the merchandise you would sell, how it would be displayed, any fixtures to be used (boxes, baskets, etc.) the method of hanging or attaching merchandise, the overall color scheme and type of sign, including the name of your cart.

STEVE'S ICE CREAM SURVEY

On a recent Tuesday afternoon Horatio took a 4 minute survey at Steve's Ice Cream Shop.



Flavor	Number of Cones Sold	Total
Cookie-O	/ /	12
Vanilla		—
Oatmeal Raisin	/ /	—
Maple Walnut		—
Chocolate Ripple		—
Strawberry	//	—

Total Number of Cones Sold in Four Minutes.

- What is the ratio of Cookie-O cones to the total number of cones sold? _____
What is the ratio of each of the other flavors to Cookie-O? _____
- If Steve sells this many cones in 4 minutes, how many does he sell in an hour?
In a 10 hour day? _____ In 5 days? _____
- On a weekend day Steve sells twice as many cones as on a weekday. How many cones does he sell on a Saturday? _____ On a weekend?(Sat, and Sunday) _____
How many cones will he sell in a whole week? _____
- If it takes one gallon of ice cream to make 25 cones, how many gallons will Steve need on Tuesday?

- If an ice cream container holds $3\frac{1}{2}$ gallons, how many containers must Steve order for Tuesday?

- If you were going to order ice cream for a week, how many gallons would you need? _____
How many containers would that be? _____
- How many gallons of each flavor per weekday must Steve order? _____
- * If each container has a diameter of 16", how much room does Steve need to store a weekday's supply? _____

PORIA PREDICTS

Reinforcement

Portia watched what foods were being sold at Quincy Market. She learned some interesting things. Can you use her research to answer these questions?

Assume: Quincy Market is open 10 hours every day, 7 days a week.*

- At the Taco Maker, Horatio observed that 20 tacos were sold in 30 minutes. At this rate, how many tacos would be sold in ...

<u>40</u> tacos in 1 hour	<u>50</u> tacos in 1 1/2 hours
<u>200</u> tacos in 5 hours	<u>400</u> tacos in 1 day
<u>2800</u> tacos in 1 week	<u>14,000</u> tacos in 1 year

- Portia was told the Pizzeria Regina sells an average of 600 pizzas per day. At this rate, how many pizzas would be sold in ...

<u>60</u> pizzas in 1 hour	<u>300</u> pizzas in 5 hours
<u>4200</u> pizzas in 1 week	<u>21,000</u> pizzas in 1 year

- Horatio discovered the Boston Brownie sell 5 times as many brownies to adults as to young people, a 5 to 1 ratio. (Warning! This isn't a 1 to 5 ratio)

- If they sell a total of 180 brownies in 1 hour, how many were sold to adults? 150 to young people? 30
- How many brownies are sold in one day to adults? 1500 to young people? 300
- How many brownies are sold in one week to adults? 15,000 to young people? 3000

- Actually, Quincy Market is only open 6 hours on Sunday but for this set of predictions assume it is open 10 hours on Sunday.

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ONE OF THE CROWD

Reinforcement



HORATIO: There sure are a lot of people here at Faneuil Hall Marketplace!

CROW: About 14,000,000 people visit every year.

HORATIO: Suppose every seventh grader in my school visited Quincy Market.

How many bries ...

CROW: Poor Horatio. He'll never solve that one. We had better help him!

Town	Est. Grade 7 Population 1986	Town	Est. Grade 7 Population 1986
Boston	4500	Waltham	450
Cambridge	500	Lincoln	125
Hingham	275	Marblehead	175
Chelmsford	425	Acton	300
Lexington	350	Medford	375
Somerville	450		
TOWN	#1 Busses	#1 Students Busses	#2 Pizzas
Boston	90	50%	1125
Cambridge	10	59%	125
Hingham	6	275%	69
Chelmsford	9	425%	107
Lexington	7	50%	88
Somerville	?	50%	113
Waltham	9	50%	113
Lincoln	3	125%	32
Marblehead	4	175%	44
Acton	6	50%	75
Medford	8	375%	94
	#2 Students	#3 T-Shirts	#3 Jewelry
		900	1500
		100	167
		55	92
		85	142
		70	117
		90	150
		150	338
		42	94
		35	58
		60	100
		75	125
		175	281
	#3 Candy		

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THE CROWD ACCORDING TO PORTIA

Extension



PORIA: Boy, it's certainly crowded in here!! I can hardly move.

CROW: Did you know that between twelve and fourteen million people visited Faneuil Hall Marketplace last year?

GRASSHOPPER: No! Come on!! That's more people than visited Disney World last year.

PORIA: It's perfectly obvious it's a reasonable estimate. In the last 15 seconds, I counted 16 people coming through that door. That's 64 in a minute. Wait a minute!! Where's my calculator?? Sixty-four times...

Did Portia estimate correctly? Check her figures. yes.

$$340 \frac{\text{people}}{\text{hr}} \times 10 \frac{\text{hrs}}{\text{day}} \times 6 \frac{\text{days}}{\text{wk}} \times 52 \frac{\text{wks}}{\text{yr}} = 11,800,800 \text{ mon-sat.}$$

$$340 \frac{\text{people}}{\text{hr}} \times 6 \frac{\text{hrs}}{3\text{days}} \times 52 \frac{\text{wks}}{\text{yr}} = 1,198,080 \text{ sun.}$$

(Hint: The market is open every day, 10 hours a day, Monday through Saturday. On Sunday it's open 6 hours.)

STEVE'S ICE CREAM SURVEY

Extension

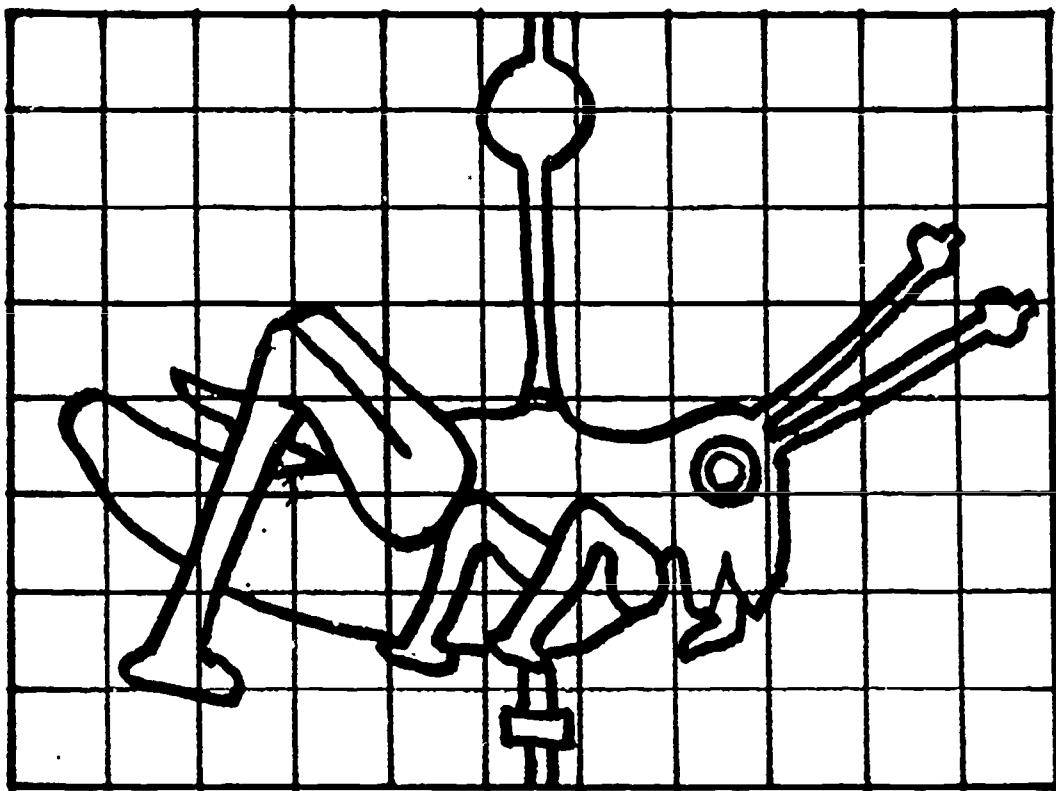
On a recent Tuesday afternoon Horatio took a 4 minute survey at Steve's Ice Cream Shop.



Flavor	Number of Cones Sold	Total
Cookie-O	7777111	12
Vanilla	777	6
Oatmeal Raisin	7777777	9
Maple Walnut	777	4
Chocolate Ripple	777	4
Strawberry	77	2

Total Number of Cones Sold in Four Minutes. 36

- What is the ratio of Cookie-O cones to the total number of cones sold? 1/3
What is the ratio of each of the other flavors to Cookie-O? 1/12, 1/6, 1/9, 1/4, 1/4, 1/2
- If Steve sells this many cones in 4 minutes, how many does he sell in an hour? In a 10 hour day? 5400 cones in 5 days? 27,000 cones
- On a weekend day Steve sells twice as many cones as on a weekday. How many cones does he sell on a Saturday? 10,800. On a weekend? (Sat and Sunday) 31,600
How many cones will he sell in a whole week? 48,600 cones
- If it takes one gallon of ice cream to make 25 cones, how many gallons will Steve need on Tuesday? 216 gallons
- If an ice cream container holds 3 1/2 gallons, how many containers must Steve order for Tuesday? 62 containers
- If you were going to order ice cream for a week, how many gallons would you need? 1944 gallons
How many containers would that be? 555 containers $\frac{C=0}{V=36} \frac{C=24}{V=36} \frac{C=24}{S=12}$
- How many gallons of each flavor per weekday must Steve order? 15.872 sq. inches.
If each container has a diameter of 16", how much room does Steve need to store a weekday's supply? 15,872 sq. inches



SCALE DRAWING

SCALE DRAWING OF SHOPS

<u>Topic/Objective</u>	<u>Materials</u>
Scale drawing Linear measure Perimeter, area	Graph paper, rulers Scissors, paper Direction cards (per store) Construction paper, tape Graph paper - included in packet (6 blocks per inch)

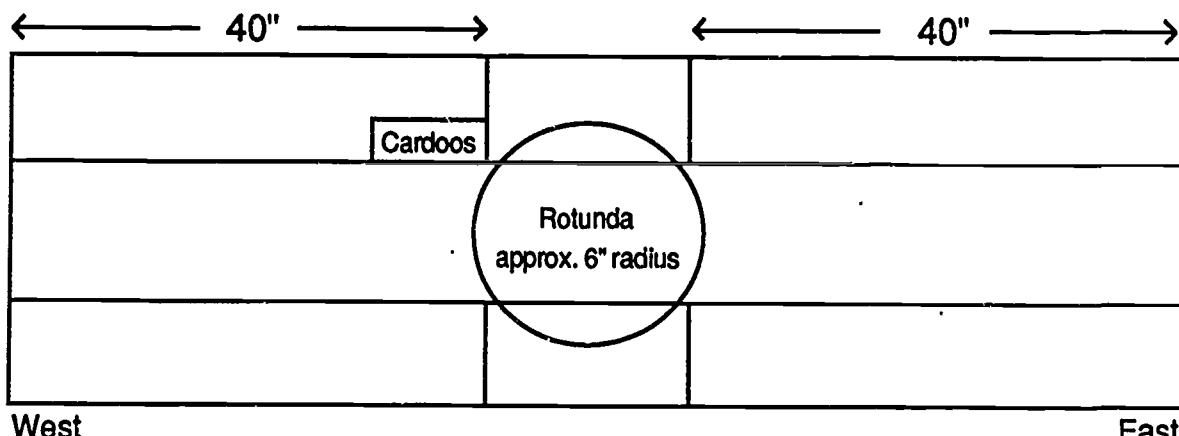
Pre-class preparation:

Review scale drawings of Quincy Market; determine scale appropriate to display area (e.g. if 9' are available, use a 1" = 6' scale); cut up cards and review them; position the outlines of Quincy Market using the dimensions listed below.

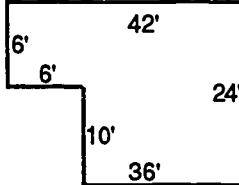
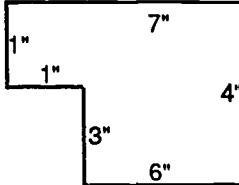
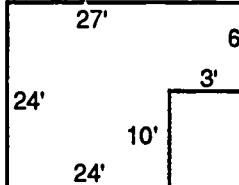
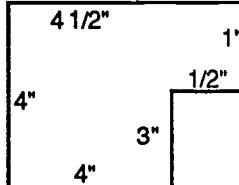
During class:

1. Use a sample card to show students how to determine the correct scaled dimensions for their shop.
Example: Cardoos 6' x 24'
 If 1" = 6', the scaled dimensions of Cardoos would be 1" x 4".
2. Each student selects a card and computes the scaled dimensions for that store.
3. Then, each student draws his/her shop on graph paper using correct dimensions. Using the graph paper as a guide, students then transfer this shape onto construction paper. Each shop should be named and may be decorated if there is time.
4. Discuss the floor plan with the students. Plot the location of the sample shop. Each student locates his/her shop and positions it correctly.

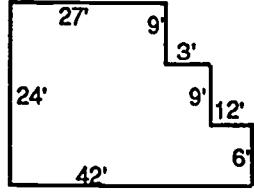
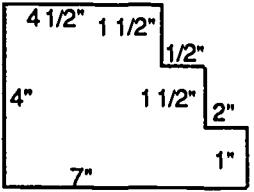
Floor Plan
Quincy Market Building



QUINCY MARKET INFORMATION SHEET

#	Name	Product	Dimensions	1" = 6' Scale
1	Coffee Connection	coffee, etc.	24' x 24'	4" x 4"
2	Beverly's Kitchen	quiches & soups	24' x 24'	4" x 4"
3	Kilvert & Forbes	cookies & brownies	 6' 42' 10' 24' 36'	 1" 7" 1" 4" 3" 6"
4	Paul W. Marks	cheese	24' x 18'	4" x 3"
5	Aegean Fare	Greek specialties	24' x 24'	4" x 4"
6	Pizzeria Regina	pizza	24' x 24'	4" x 4"
7	Peanut Butter Fantasies	peanut butter	24' x 21'	4" x 3 1/2"
8	J.P. Abocdy	fruit cups & salads	 24' 6' 24' 3' 10' 27'	 4" 1" 4" 1/2" 4" 3" 4" 4"
9	Cardoos	candy & nuts	6' x 24'	1" x 4"

QUINCY MARKET INFORMATION SHEET

#	Name	Product	Dimensions	1" = 6' Scale
10	Joey's Gelateria	ice cream	9' x 18'	1 1/2" x 3"
11	Doe, Sullivan & Company	cheese		
12	Jennetta's	subs & Italian specialties	24' x 24'	4" x 4"
13	The Monkey Bar	drinks	24' x 18'	4" x 3"
14	Ming Tree	Chinese food	24' x 24'	4" x 4"
15	Boston & Maine Fish Co.	seafood	24' x 24'	4" x 4"
16	Great Stuff	salads	24' x 36'	4" x 6"
17	Boston Beanery	beans	9' x 9'	1 1/2" x 1 1/2"
18	Freedman's Bakery	bagels & pastries	24' x 48'	4" x 8"

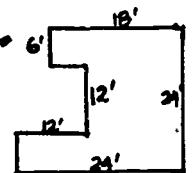
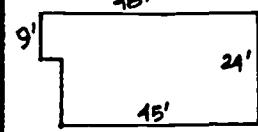
QUINCY MARKET INFORMATION SHEET

#	Name	Product	Dimensions	1" = 6' Scale
19	Steve's Ice Cream	ice cream		
20	Julian's Cheesecake	cheesecake	9' x 9'	1 1/2" x 1 1/2"
21	M. Berenson	meat	24' x 39'	4" x 6 1/2"
22	E.N. West	meat	24' x 18'	4" x 3"
23	Aris Barbecue	chicken & ribs	24' x 24'	4" x 4"
24	Brown Derby Deli	hot dogs & pastrami	24' x 36'	4" x 6"
25	Au Bon Pain	French breads		
26	North End Bakery	Italian pastries	6' x 18'	1" x 3"

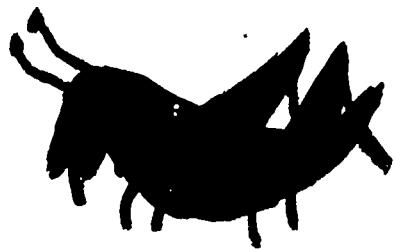
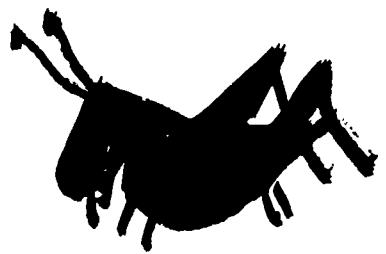
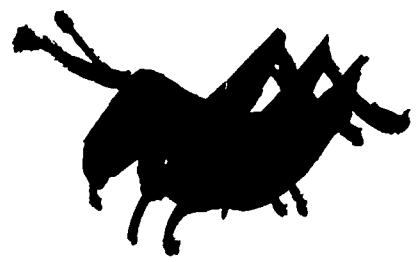
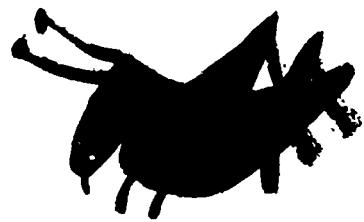
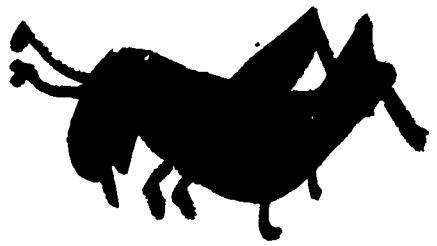
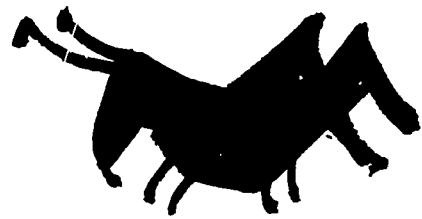
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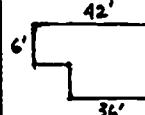
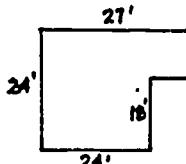
QUINCY MARKET INFORMATION SHEET

#	Name	Product	Dimensions	1" = 6' Scale
27	Aval's Fudge	fudge	6' x 12'	1" x 2"
28	Taco Maker	Mexican specialties		
29	A la Carta	hors d'oevres	24' x 24'	4" x 4"
30	Boston Brownies	brownies	24' x 18'	4" x 3"
31	The Colombo Yogurt Shop	yogurt	24' x 18'	4" x 3"
32	Walrus and the Carpenter	clams & oysters	24' x 18'	4" x 3"
33	Fisherman's Nest	fish & seafood plates	24' x 24'	4" x 4"
34	Cafe Marion	burgers & salads	24' x 39'	4" x 6 1/2"
35	Raging Cajun	gumbo & jambalaya	9' x 9'	1 1/2" x 1 1/2"
36	Carol Ann Bake Shop	Italian pastries		

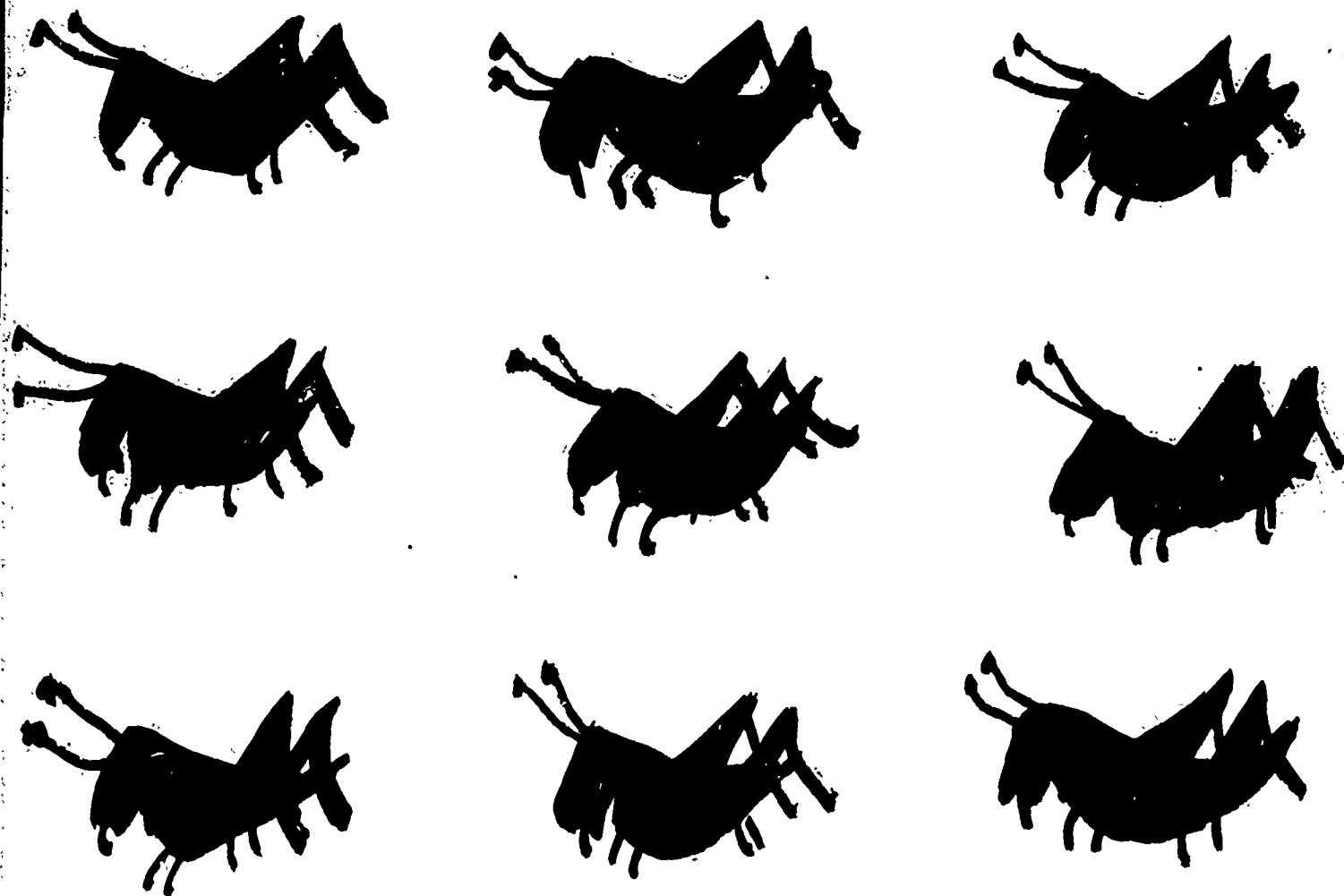
 <p>28</p> <p>Taco Maker</p> <p>YOU MUST FIGURE THE MISSING DIMENSIONS</p> 	 <p>29</p> <p>A la Carte</p> <p>$24' \times 24'$</p>	 <p>30</p> <p>Boston Brownies</p> <p>$24' \times 18'$</p>
 <p>31</p> <p>The Columbo Yogurt Shop</p> <p>$24' \times 18'$</p>	 <p>32</p> <p>Walrus and the Carpenter</p> <p>$24' \times 18'$</p>	 <p>33</p> <p>Fisherman's Net</p> <p>$24' \times 24'$</p>
 <p>34</p> <p>Cafe Marion</p> <p>$24' \times 39'$</p>	 <p>35</p> <p>Raging Cajun</p> <p>$9' \times 9'$</p>	 <p>36</p> <p>Carol Ann Bake Shop</p> <p>YOU MUST FIGURE THE MISSING DIMENSIONS.</p> 

QUINCY MARKET FLOOR PLAN ASSIGNMENT CARDS • EAST WING • TO BE CUT FOR STUDENTS



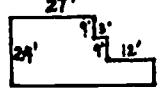
 <p>1</p> <p>The Coffee Connection</p> <p>$24' \times 24'$</p>	 <p>2</p> <p>Beverly's Kitchen</p> <p>$24' \times 24'$</p>	 <p>3</p> <p>Kilvert & Forbes</p> <p></p> <p>YOU MUST FIGURE THE MISSING DIMENSIONS.</p>
 <p>4</p> <p>Paul W. Marks</p> <p>$24' \times 18'$</p>	 <p>5</p> <p>Aegean Fare</p> <p>$24' \times 24'$</p>	 <p>6</p> <p>Pizzeria Regina</p> <p>$24' \times 24'$</p>
 <p>7</p> <p>Peanut Butter Fantasies</p> <p>$24' \times 21'$</p>	 <p>8</p> <p>J.P. Aboody</p> <p></p> <p>YOU MUST FIGURE THE MISSING DIMENSIONS.</p>	 <p>9</p> <p>Cardoos</p> <p>$6' \times 24'$</p>

QUINCY MARKET FLOOR PLAN ASSIGNMENT CARDS • WEST WING • TO BE CUT FOR STUDENTS

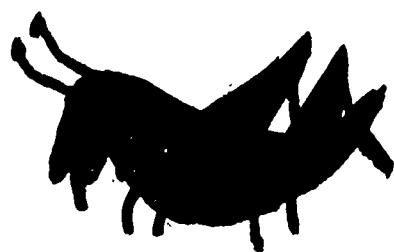
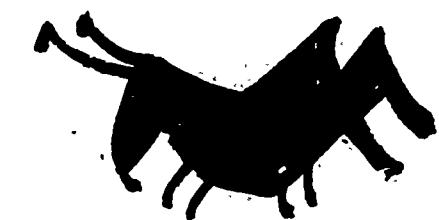


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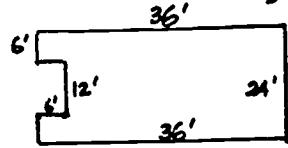
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 <p>10 Joey's Gelateria $9' \times 18'$</p>	 <p>11 Doe, Sullivan & Co.  YOU MUST FIGURE THE MISSING DIMENSIONS.</p>	 <p>12 Jennetta's $24' \times 24'$</p>
 <p>13 The Monkey Bar $24' \times 18'$</p>	 <p>14 Ming Tree $24' \times 24'$</p>	 <p>15 Boston & Maine Fish Co. $24' \times 24'$</p>
 <p>17 Boston Beanery $9' \times 9'$</p>	 <p>16 Great Stuff $24' \times 36'$</p>	 <p>18 Freedman's Bakery $24 \times 48'$</p>

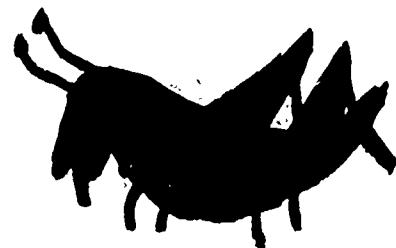
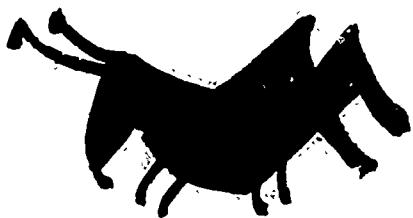
QUINCY MARKET FLOOR PLAN ASSIGNMENT CARDS • WEST WING • TO BE CUT FOR STUDENTS

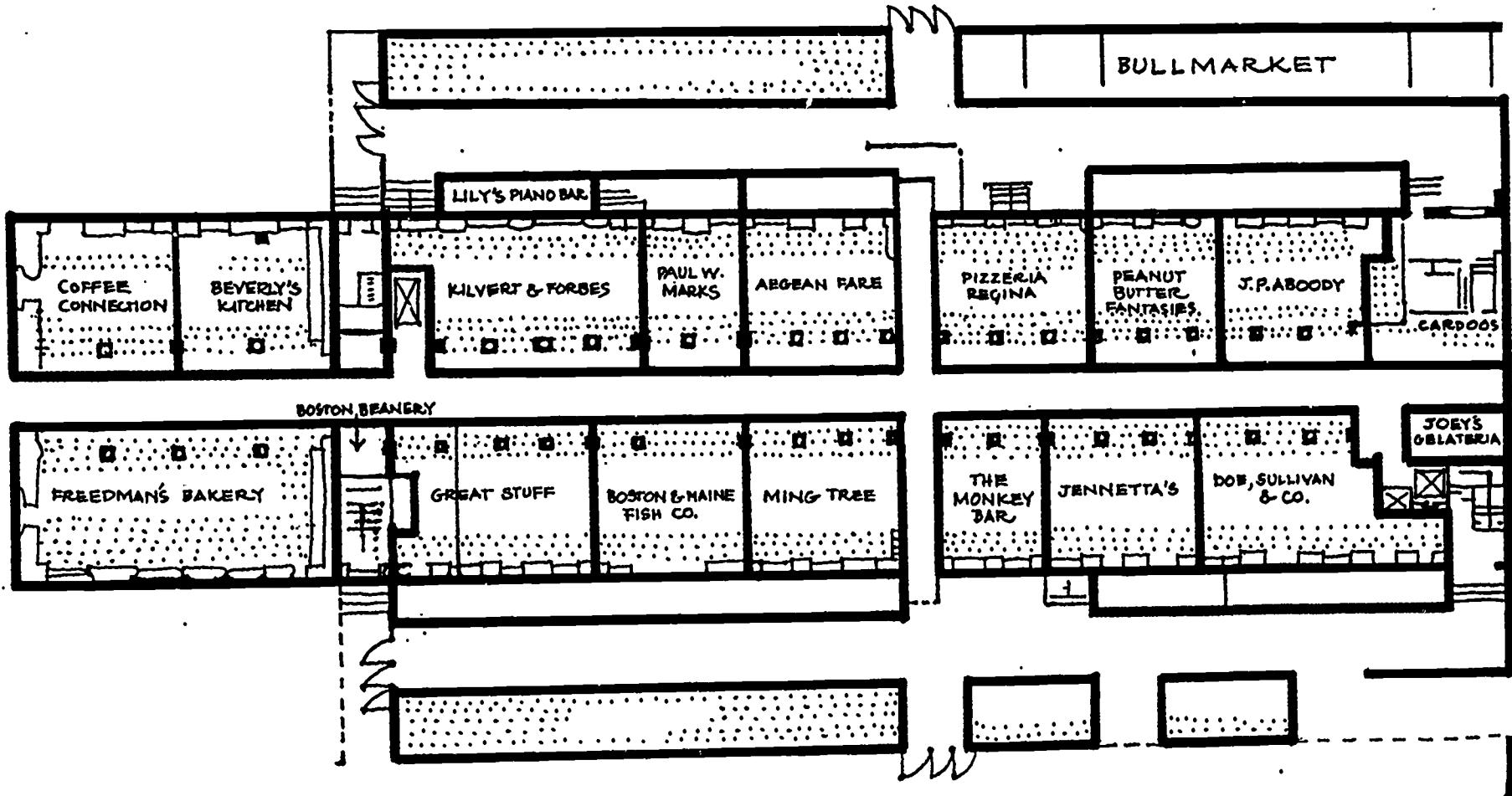


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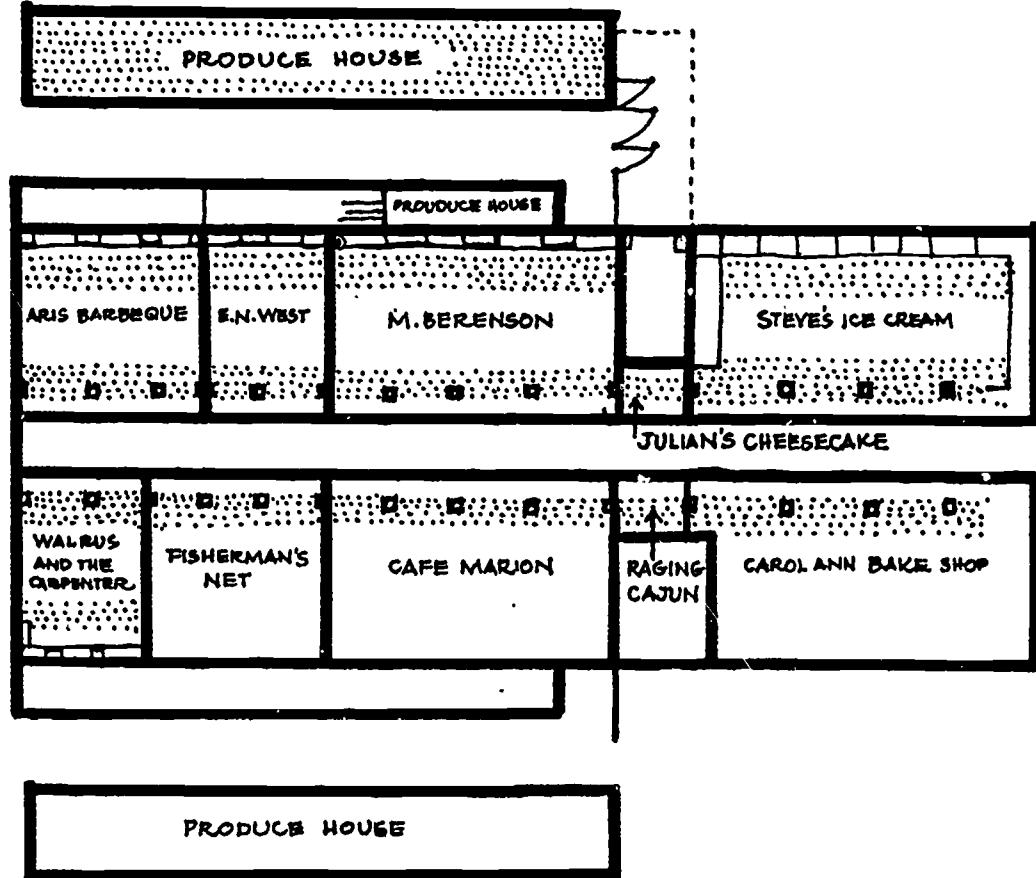
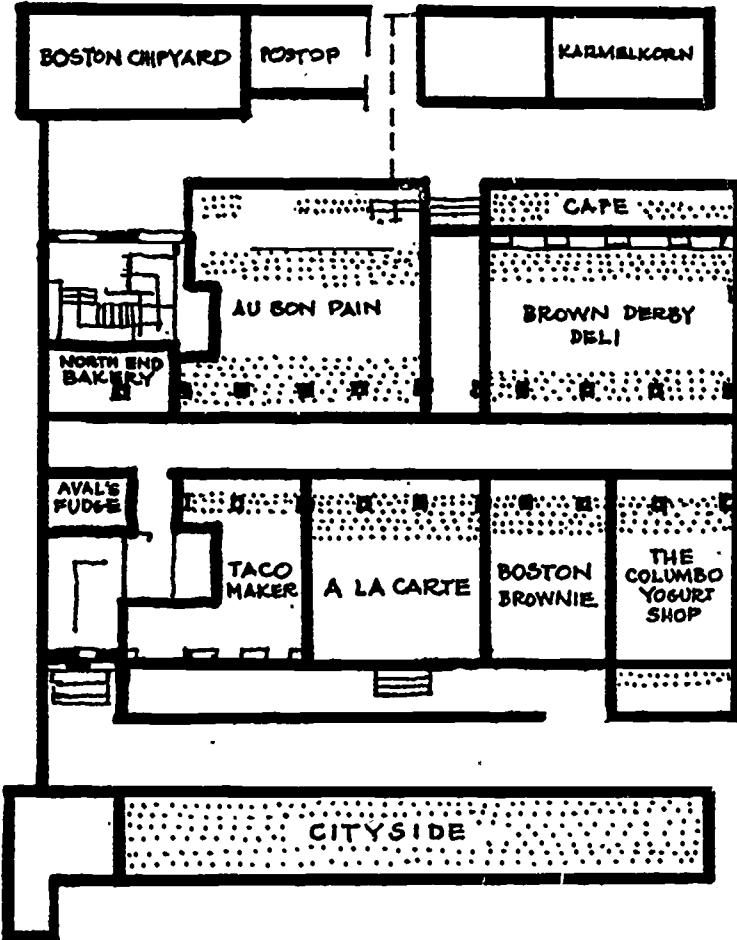
 <p>Steve's Ice Cream</p> <p>21' × 48'</p>	 <p>Julian's Cheesecake</p> <p>9' × 9'</p>	 <p>M. Berenson</p> <p>24' × 39'</p>
 <p>E.N. West</p> <p>24' × 18'</p>	 <p>Aris Barbeque</p> <p>24' × 24'</p>	 <p>Brown Derby Deli</p> <p>24' × 36'</p>
 <p>All Bon Pain</p>  <p>YOU MUST FIGURE THE MISSING DIMENSIONS.</p>	 <p>North End Bakery</p> <p>6' × 18'</p>	 <p>Aval's Fudge</p> <p>6' × 12'</p>

QUINCY MARKET FLOOR PLAN ASSIGNMENT CARDS • EAST WING • TO BE CUT FOR STUDENTS





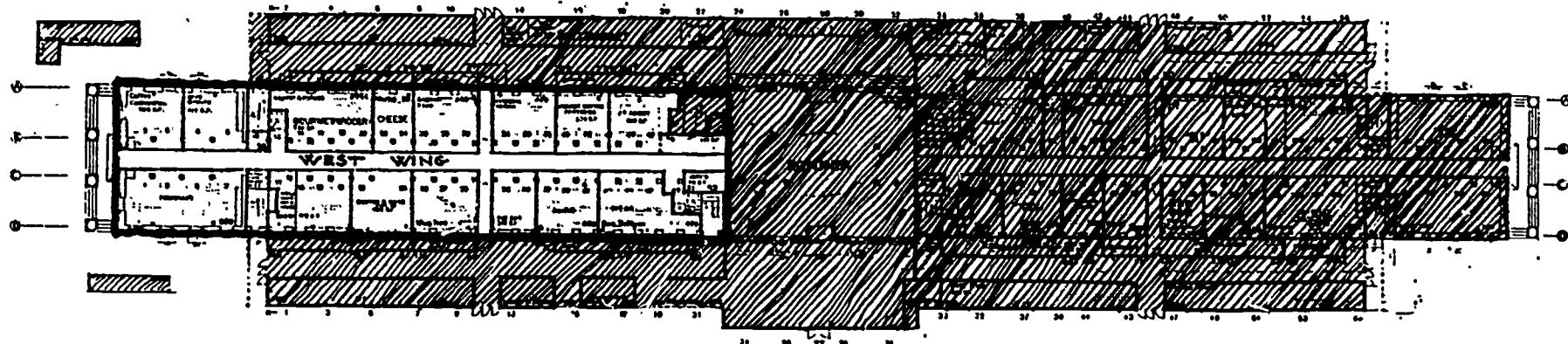
QUINCY MARKET • WEST WING SHOP LOCATIONS



QUINCY MARKET • EAST WING SHOP LOCATIONS

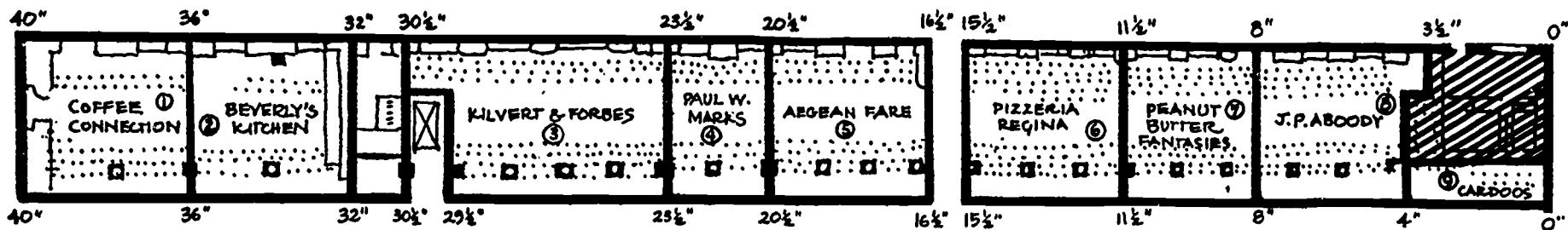
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QUINCY MARKET • WEST WING

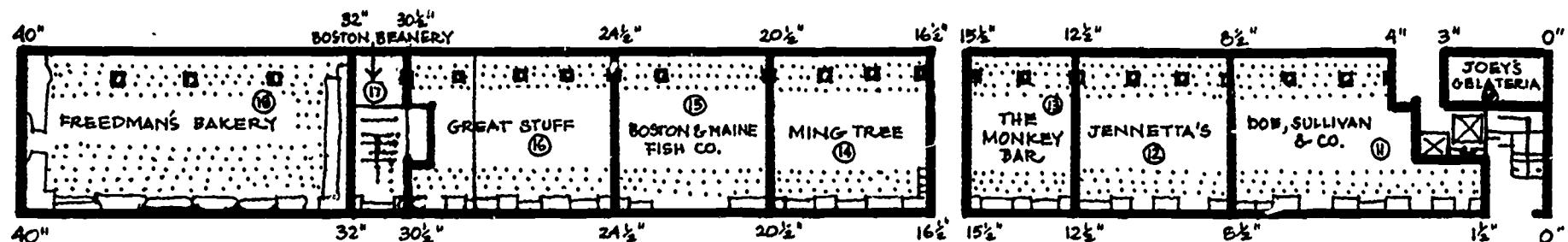


FOR TEACHER USE IN SETTING UP BULLETIN BOARD DISPLAY.
INCH MARKINGS SHOULD BE MADE ON MASKING TAPE OR OTHER GUIDE ON BULLETIN BOARD.

SCALE: 1" = 6'



ROTUNDA →



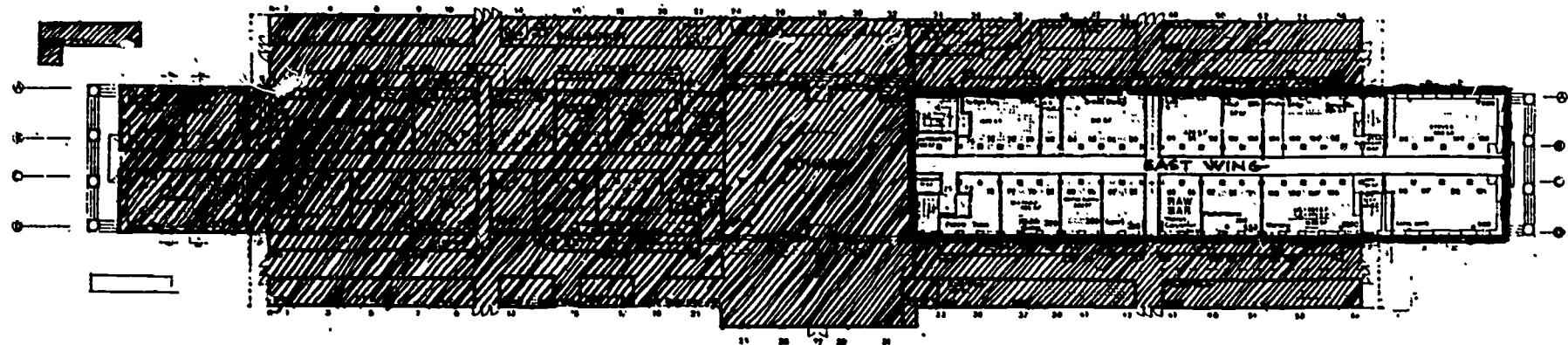
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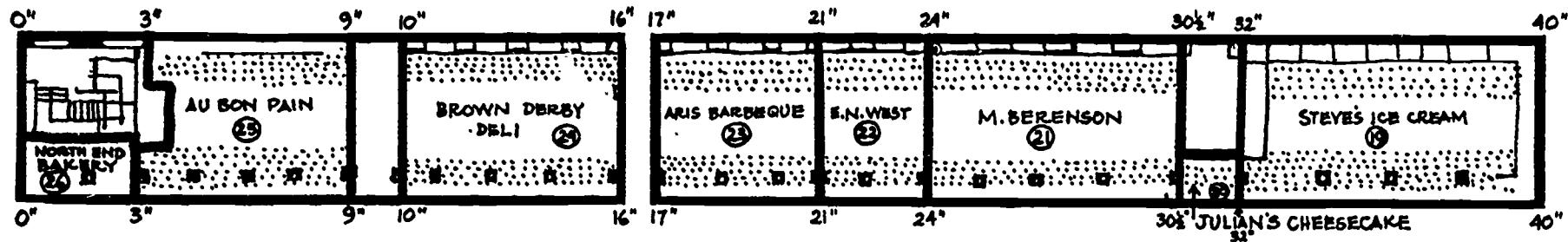
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QUINCY MARKET • EAST WING

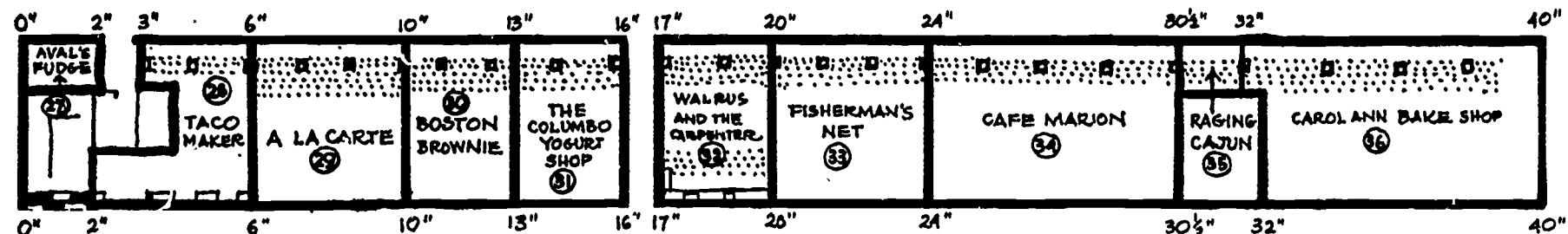


FOR TEACHER USE IN SETTING UP BULLETIN BOARD DISPLAY.
INCH MARKINGS SHOULD BE MADE ON MASKING TAPE OR OTHER GUIDE ON BULLETIN BOARD.

SCALE: 1" = 6'



← ROTUNDA



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THE GRAPH-HOPPER

<u>Topic/Objective</u>	<u>Materials</u>
Scale drawing, linear measure Ratio, proportion Perimeter, area	Construction paper 1/2" and 1" graph paper (included in unit) Rulers

Pre-class preparation:

Prepare a sample crow, and grasshopper.

During class:

1. Ask students to choose the scale they wish to use (1/2" or 1"). Remind them that their drawings will be used as part of the class display and that a variety of sizes are needed.
2. Distribute graph paper according to scale chosen.
3. Begin a sample crow or grasshopper on the board or overhead with the class. Have students continue work on their own or in small groups. Use the coordinate system to help complete your drawings.
4. Discuss with the class the effect of scale on both the area and perimeter of a design.

Extensions:

If your classroom has floor tiles, have students complete one design on the floor using colored chalk.

If a pantograph is available, ask a group of students to learn how to use it and present a class demonstration.

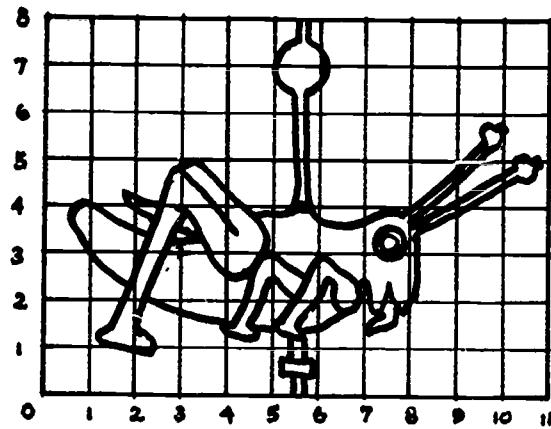
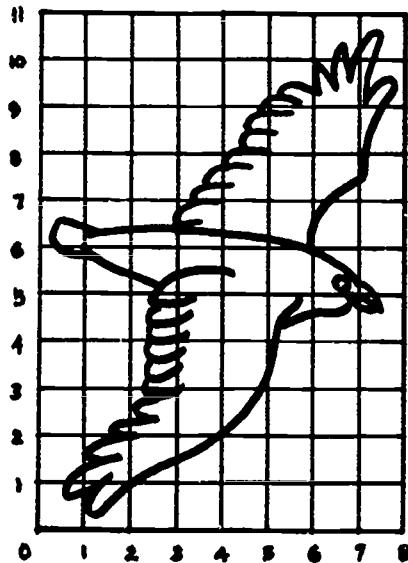
Prepare overhead transparencies from some of the designs. Project them on the wall at different distances and examine the effect on area and perimeter.

THE GRAPH-HOPPER



HORATIO: I'm trying to enlarge drawings of the crow and the grasshopper and it's not working.

PORTIA: Well, it's perfectly obvious to me that you gotta use graph paper.



The crow and grasshopper have been drawn on 1/4" graph paper.

Enlarge the pictures by using 1/2" or 1" graph paper.

Now answer the following questions:

- 1) What size are the squares on your graph paper? How much larger are your squares than the squares on this page? What is the perimeter of your square? Of the one above? What is the area of your square? Of the one above?
- 2) What do you think this enlargement will do to the length of the grasshopper or the wing span of the crow? Measure corresponding parts to check your guess.
- 3) What do you think this enlargement will do to the area of the paper covered by the grasshopper or the crow?

List some other questions you might ask and give their solutions.

CONSTRUCTION OF BULL MARKET CART

<u>Topic/Objective</u>	<u>Materials</u>
Scale drawing Linear measure Perimeter, Area	Posterboard or oak tag (1 1/3 pieces of 8 1/2 x 11 per cart) 1/4" metal fasteners Glue, compass, scissors

Pre-class preparation:

Construct sample cart; gather materials (posterboard or oak tag); duplicate cart design on oak tag (optional)

During class:

1. Oak tag: If oak tag is used and cart design has been duplicated on oak tag, students will be ready to cut and assemble their carts immediately.

Posterboard: Instruct students to paste their designs onto the posterboard before cutting and assembling carts.

(Students may be encouraged to work in pairs so they can assist one another)

2. After the students have assembled their carts, have them compare the dimensions of their model to those of a real cart (scale: 1" = 1')

Suggested questions:

- What is the length of the rectangular display part of your cart?
- What will the length be on the real cart?
- What is the width of this display on your cart? On a real cart?
- What is the diameter of the model cart wheel? Of the real cart wheel?
- What is the ratio of these dimensions?
- What is the area of the model cart wheel? Of the real cart wheel?
- What is the area of the rectangular display on your cart?
- What is the area of the rectangular display on the real cart?
- What is the ratio of these two areas? Why is it different from the ratio of the length of the display areas? (the square factor is introduced)

After class

- * Compare the volume of the top tray of the model cart to that of the real cart. What is the ratio of these volumes? Extension
- * Choose an item to sell from your cart. Name your cart appropriately and decorate it. You may even stock the cart. Draw all items to scale. Extension
- * Construct a full-size cart. The full-size cart is 3' by 6' (use the scale drawing to construct it). Appliance boxes (e.g. refrigerator box) would be useful. Double wheels will give added support. A roof might even be added. (Note: this introduces square and cubic factors) Extension

CONSTRUCT YOUR OWN BULL MARKET CART

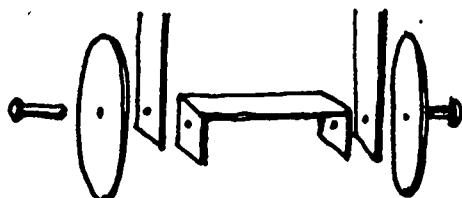
Use the design which your teacher gives you. Follow directions for oak tag or posterboard depending on the material you are using.

OAK TAG: Skip to step 1 below.

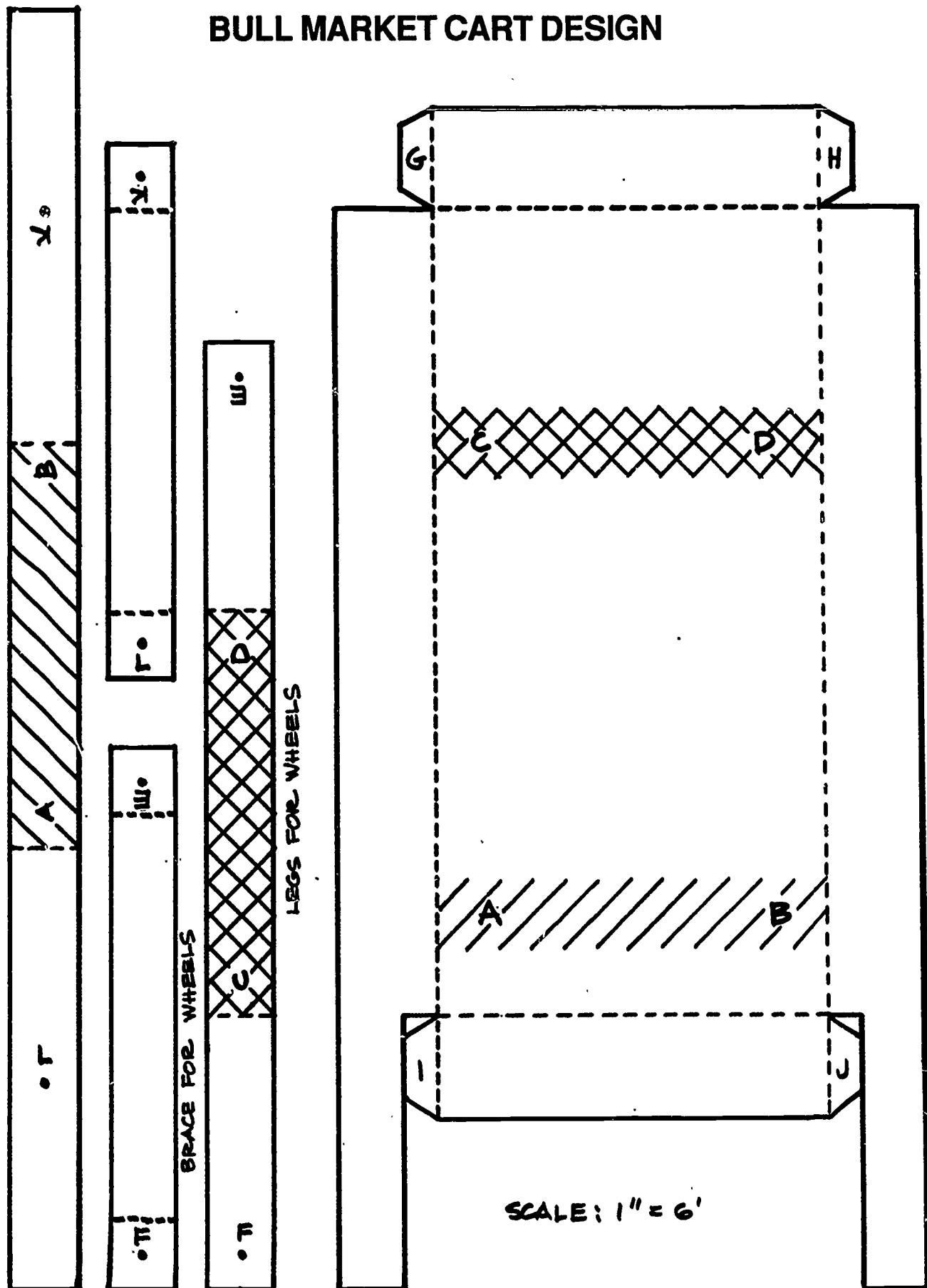
POSTERBOARD: Using a ruler and ball point pen, trace the design from the paper onto the posterboard. Press hard. Now go to step 1 below.

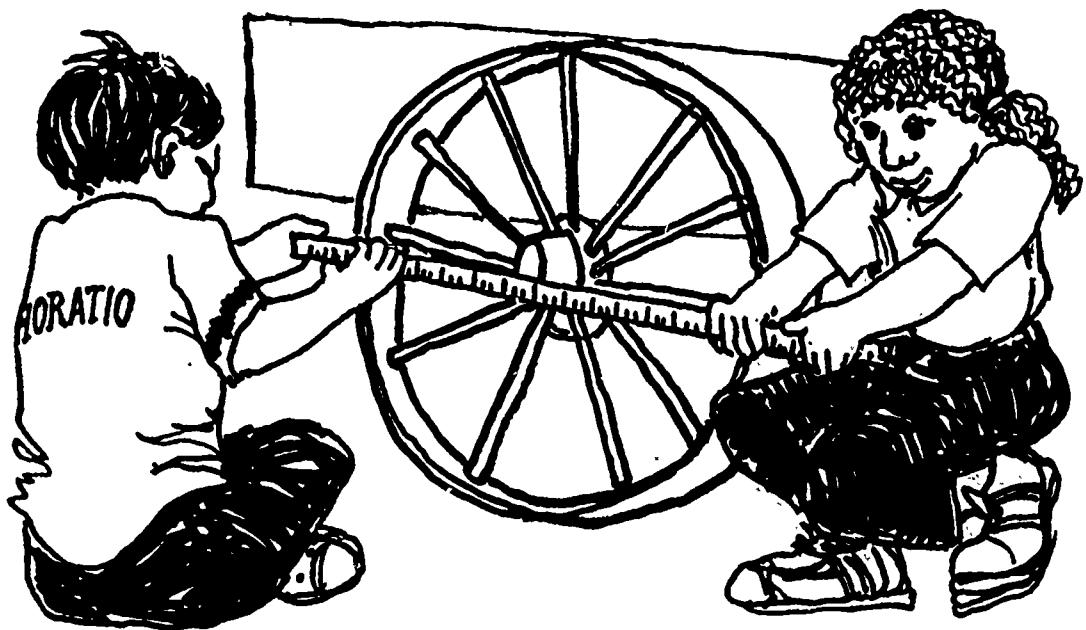


1. Carefully cut all pieces along solid lines.
2. Use a compass to construct two circles with diameters of 3" on your plain piece of oak tag. Cut out these circles for cart wheels.
3. Fold carefully on dotted lines. Dots should be on the outside of the fold.
4. Glue AB to AB and CD to CD.
5. Fold in tabs G, H, I and J and glue to form the top of the cart.
6. Insert a small metal fastener into the center of one wheel, then through point F on the cart leg and point F on the brace, and fasten. (Be sure that the brace tab is inside the leg cart with the tab facing down.)
7. Insert another fastener through the center of the other wheel, then through point E on the other leg and finally through point E on the brace.
8. With glue, attach the other leg brace, matching K's and L's.



BULL MARKET CART DESIGN





PERIMETER AND AREA

PERIMETER

<u>Topic/Objective</u>	<u>Materials Needed</u>
Concept of perimeter	12.5 feet of yarn knotted at 12 feet, graph paper, 2 yardsticks, dot paper for all students

During class:

1. Ask four students to hold the yarn and be prepared to create different shapes. Ask two students to check measurements with yardstick. All other students should record figures on dot paper or graph paper. Use scale $1'' = 1'$ or $1/4'' = 1'$.
2. Ask the students to form the following using the yarn (all of the perimeters will be the same since the length of the yarn never changes):
 - a triangle
 - an equilateral triangle--discuss the meaning of congruence
 - a right triangle--how many different right triangles can be formed? Does one of the right triangles have sides 3, 4, and 5? (remind students that the perimeter is constant)
 - a square
 - a rectangle--how many different rectangles can you form? What is the perimeter of each? What is the area of each? What rectangle appears to have the largest area?
 - What does perimeter mean? If I know the perimeter of a figure, can I always predict the area?

After Class**"I Counted My Hops!"**

Use textbook for supplementary problems

Reinforcement

I COUNTED MY HOPS



Horatio: How far is it around the Quincy Market building?

Grasshopper: I didn't really measure, but I counted my 242 hops.

If every grasshopper hop is 60 inches long, what is the perimeter of the Quincy Market Building in feet?

perimeter

Horatio: I didn't really measure, but I took 24 steps when I walked along the width of the building.

If every step Horatio took was 25" long, what was the width of the building in feet?

width

Using the information from the Grasshopper and Horatio, find the dimensions of the Quincy Market Building.

(Hint: Draw a diagram of a rectangle to help you solve the puzzle.)

HANDS AROUND THE SCHOOL

<u>Topic/Objective</u>	<u>Materials Needed</u>
Concept of perimeter	Town Map (optional)

During class:

1. Ask students to stand around the perimeter of the room (or the lunchroom or gymnasium--wherever there is blank wall space).
 - Can they enclose the entire perimeter?
 - Can they enclose the perimeter with fewer people?
 - Estimate and agree upon the length for which each person is responsible
 - Estimate the largest perimeter that this class could form
2. Can you predict whether all of the students in the school could surround the school building? The gym? The football field? Your town?
3. Did you know that most people are "squares"? ("squares" means that the ratio of their arm spread to their height is close to 1).

Check this with:

- Members of your class
- Small children
- Adults

4. Using an enlarged map of your town have students use yarn to measure the perimeter and convert this answer to feet. Calculate the number of people required to surround the town. Could your town's population do this?
5. (Challenge Project) "Hands Across America" tried to create a human chain from New York to Los Angeles. If it is 2825 miles, how many students would be necessary for the chain.

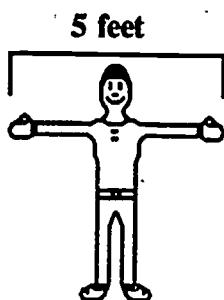
After Class

"Quincy Market, We've Got You Surrounded"
 "Portia's Dilemma"

Extension
 Extension

QUINCY MARKET: WE'VE GOT YOU SURROUNDED!

Fact: The Quincy Market building is 555' long and 50' wide. The average person has an arm spread of 5 feet.



Question: How many visitors would it take to surround Quincy Market?

Fact: Approximately 35,000 people visit Quincy Market every day.

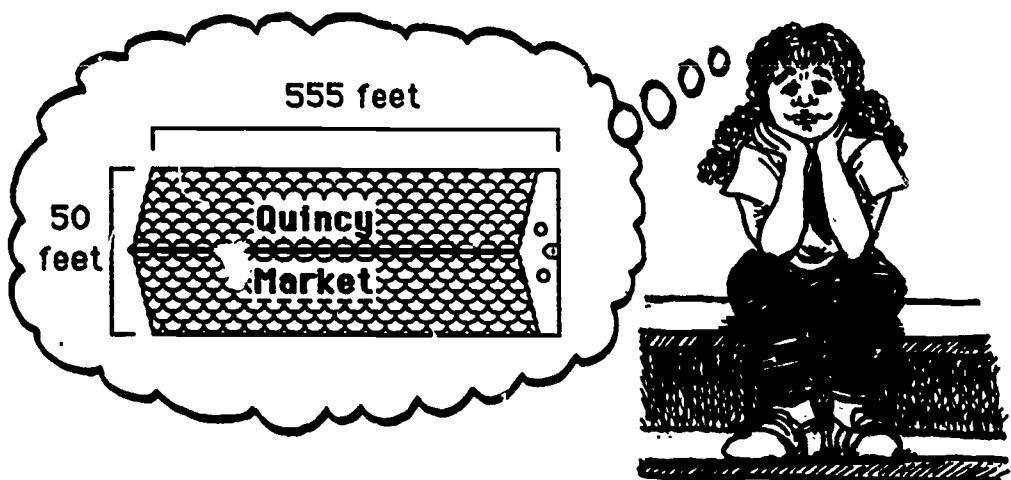
Question: If all of the visitors on Tuesday held hands, how many times would Quincy Market be surrounded?



132

94

PORTIA'S DILEMMA



Fact: One day Quincy Market had 34,364 visitors. Every visitor had a 5' arm spread. Suppose every visitor was there at the same time, and they all joined hands around the outside of Quincy Market.

Question: What is the largest (in area) rectangle that can be formed that uses every visitor and has dimensions proportional to those of Quincy Market?

AREA: SQUARES AND RECTANGLES

<u>Topic/Objective</u>	<u>Materials</u>
Develop concept of area	Use Masking tape to mark 4 square feet and 1 square yard on the floor. Place the tape so that one square is 2 feet on a side and the other is 3 feet on a side

During Class:

1. Ask one student to stand in the 4 square-foot box. Can another student fit? How many can fit? (Rule: Both feet must be on the floor)
2. Have students stand in the square yard box. How many can fit?
3. What is the ratio of the number of students in the 4 square-foot box to the number of students in the square yard box?

Use these numbers for the following problems and the homework assignment.

4. Have students estimate the number of students who could fit in
-the classroom
-the gym, etc.
5. How many square feet (yards) would hold the entire class?
6. How many square feet (yards) would hold the entire school?

After Class

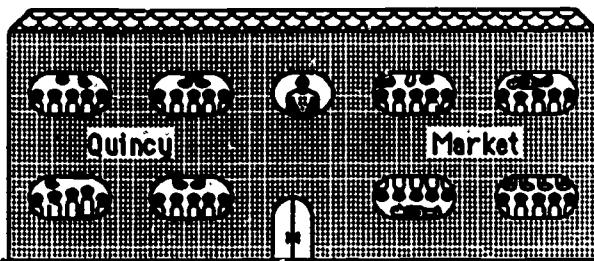
"How Many Visitors Can Fit in Quincy Market?"

"Bull Market Cart Storage"

Use textbook for supplementary problems

Reinforcement
Extension

HOW MANY VISITORS CAN FIT INTO THE QUINCY MARKET BUILDING?

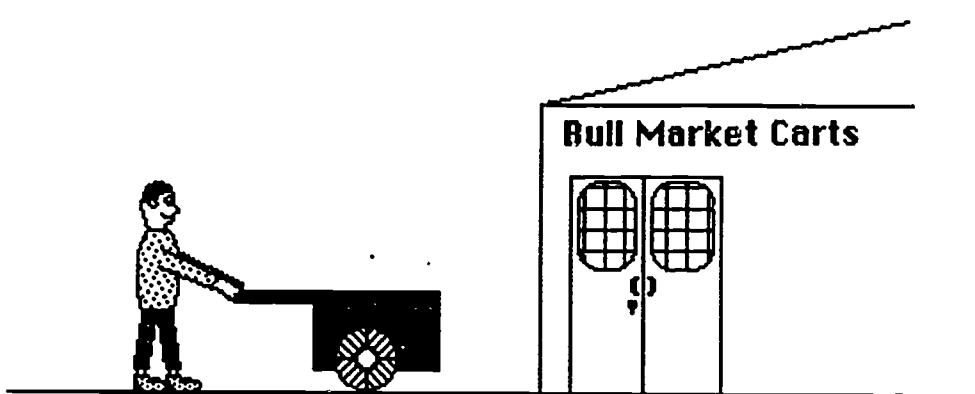


The dimensions of the Quincy Market Building are 50' by 555'. If we assume there are no obstacles in the building, how many people can fit inside the building at one time? First floor only, please! (HINT: Use the results from your class experiment and think about the number of people that fit into a square yard).

Find out about the fire regulations for your town and what limits there are on building capacity. How many people could legally fit into Quincy Market if it were in your town?

Use the results of your class experiment to determine how many people could fit into an elevator 5' x 6'. If the average weight of each person is 130 lbs., how much weight is that elevator carrying?

BULL MARKET CART STORAGE



Bull Market carts are 3' wide and 6' long. If there are 50 carts that must be stored in a room, find the dimensions of the smallest room that will hold all 50 carts. The room should only have one door (which opens out). You decide where that door should be. The carts must be placed so that any cart can get out without moving other carts.

Show the arrangement of the carts in the room.

HINTS: Graph paper might help. You may choose to use the carts you have constructed and start with a smaller number of carts.

SPOT ON THE WHEEL

<u>Topic/Objective</u>	<u>Materials</u>
Circumference of a circle Concept of π	String, Rulers, Calculator, Chart on blackboard (optional), Tape Measure (optional)

Pre-Class Preparation: Cut-out cardboard circles with diameters of 3", 4", 5", 10", and 12". Put chart below on blackboard.

Diameter of Wheel	Measure of Circumference	$\frac{C}{D}$
3 inches		
4 inches		
5 inches		
10 inches		
12 inches		

During Class:

1. Explain that the word circumference is used to designate the perimeter of a circle.
2. Ask students to find a diameter (by folding circle in half) and to measure and record the diameter and circumference (using string or rolling circle on a flat surface).
3. Have students make a visual comparison of circumference and its relationship to diameter.
4. Encourage them to verbalize that for any circle the circumference is approximately three times the diameter.
5. Use the chart on the blackboard and a calculator to develop $C/D \approx 3.14$ and introduce the symbol π . Stress that 3.14 is an approximation and that the formula $C = \pi D$ may be used to find the circumference of a circle with known diameter.
6. Have students make up several examples using the formula and "Spot on the Wheel" in class. Have students share the examples with each other.

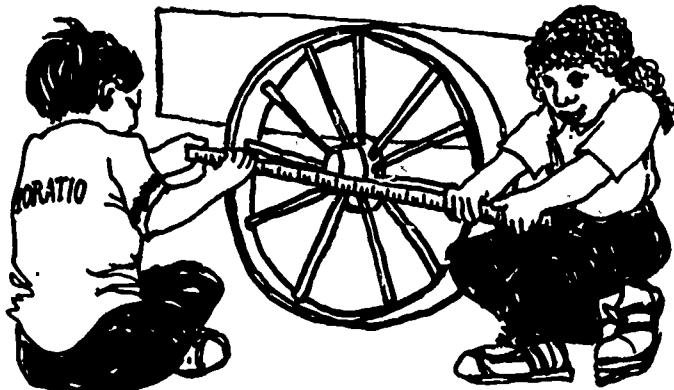
After Class

"Spot on the Wheel"
 "Pi for Horatio"
 "How Many Rotations"
 Use textbook for supplementary examples

Reinforcement
 Reinforcement
 Extension

THE SPOT ON THE WHEEL

Horatio observes a nick on the edge of the wheel as one of the vendors pushed a bull market cart into position.



HORATIO: I wonder how far the cart moves when the wheel turns exactly once?

PORTIA: It's perfectly obvious to me that we need to measure the circumference of the wheel and compare our measure, in some way, to the diameter of the wheel.

HORATIO: Circumference! What's that?

PORTIA: Circumference is the perimeter of the wheel.

Portia and Horatio did some measurement and put the results on a chart. Complete the chart by finding the indicated measurements and doing the necessary calculations.
(HINT: A calculator could make this easier).

Find 5 other circular objects to measure and complete the chart.

OBJECT	DIAMETER	DISTANCE AROUND OUTSIDE OF CIRCLE (circumference)	Divide circumference by diameter and round answer to nearest hundredth
WHEEL	3 feet	9.5 feet	3.17
PIZZA			
CHOCOLATE CHIP COOKIE			

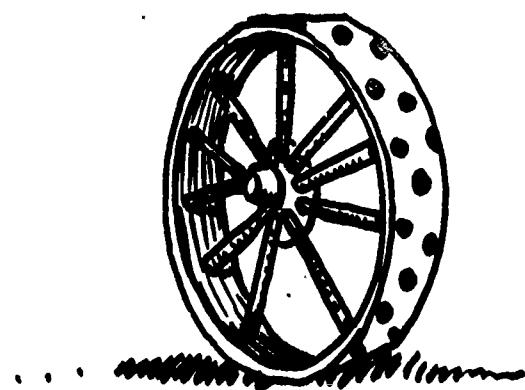
What do you observe in the last column? What are your conclusions?

MORE SPOTS ON THE WHEEL

OBJECT	DIAMETER	DISTANCE AROUND OUTSIDE OF CIRCLE (CIRCUMFERENCE)	<u>CIRCUMFERENCE</u> DIAMETER ROUND ANSWER TO NEAREST HUNDREDTH
WHEEL	5 FEET	15.9 FEET	3.18

What do you observe in the last column?

What are your conclusions?





PI FOR HORATIO

PORTIA: Horatio, it's perfectly obvious to me you don't need to measure the circumference, just multiply the diameter by π !

HORATIO: Apple or blueberry?

Poor Horatio! He still thinks $\pi = \text{apple}$, but you know $\pi = 3.14$ (well, almost!). Find the circumference of the following using the formula $C = \pi d$.

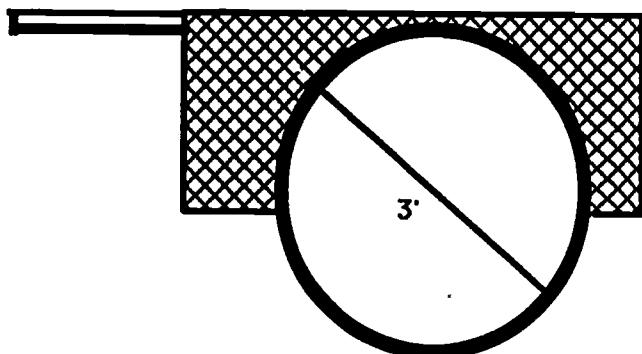
1. A cup with a diameter 4". _____
2. The top rim of a flower pot with diameter 6". _____
3. The bottom rim of a lampshade with diameter 12". What is your answer in inches? _____ In feet? _____
4. A circular rug with diameter 54". What is your answer in inches? _____ In feet? _____ In yards? _____
5. A circular swimming pool with diameter 18'. What is your answer in feet? _____ In yards? _____
6. A button with diameter 1/2". What is your answer in inches? _____
7. A bicycle wheel with radius 13". How many inches have you travelled when the wheel makes one rotation? _____
8. Estimate the diameter of a pipe with circumference 9 1/2". _____

Measure the circumference of 3 circular objects and use the formula $C = \pi d$ to estimate the diameter of these objects.

OBJECT	CIRCUMFERENCE	DIAMETER
1.		
2.		
3.		

HOW MANY ROTATIONS, HORATIO?

- HORATIO:** I think I'll push this cart around Quincy Market and count the number of times the wheel turns.
- CROW:** Remember, Horatio, the Quincy Market building is 50 feet wide and 555 feet long.
- GRASSHOPPER:** An estimation is good enough for me!
- PORTIA:** Does anybody have a calculator?



Find out how many times the wheel turns when the bullmarket cart is pushed around the perimeter of the Quincy Market building.

Why might Horatio's answer be different from Portia's?

Are there any accuracy problems here?

A BIG SLICE IN THE LIFE OF HORATIO

<u>Topic/Objective</u>	<u>Materials</u>
Area of circle (estimation)	Graph chalkboard, 1" graph paper (3 pieces per student), Compasses, String (2 feet)

During Class:

1. Distribute graph paper and compasses to each student.
2. Brainstorm with students to generate methods for approximating the area of a circle.
3. Have students draw a circle with radius 3" on their graph paper and count the squares. (Approximate partially covered squares.)
4. Repeat same procedure with circles of 1" and 2" radius.
5. Draw circles of radius 4" on chalkboard. Ask students to brainstorm how they would use their graph paper to find the area of this circle. (Hint: students should draw semicircle on graph paper.)
6. Introduce "A Big Slice in the Life of Horatio".

Discuss meaning of a 16" pizza. (Hint: radius = 8").

Show students how to draw a circle using string. Suggest that students draw their circles on newspaper or a brown paper bag. Have students use their graph paper for estimating area.

After Class

"A Big Slice in the Life of Horatio"

Reinforcement

A BIG SLICE IN THE LIFE OF HORATIO

HORATIO: I'm starved! I want a large 16" pizza.

PORȚIA : That's more than twice the size of the 10" pizza! You'll never finish all that, Horatio!

HORATIO: It's only 6" bigger!

Portia and Horatio are not using the same type of comparison. **BOTH ARE RIGHT!** Can you explain why?



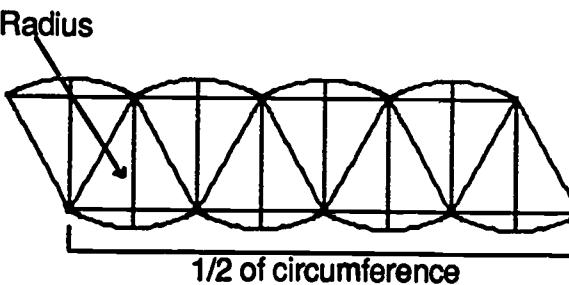
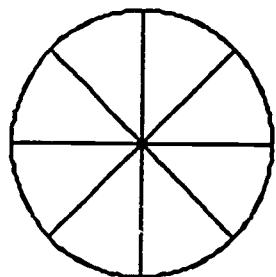
Construct circles of diameter 10" and 16" and estimate carefully the area of each circle. Bring your circles to class and be prepared to explain your method of estimation.

PIZZA PI

<u>Topic/Objective</u>	<u>Materials</u>
Area of Circle (formula)	Scissors Rulers

During Class:

1. Discuss methods used by students to approximate the area in "A Big Slice in the Life of Horatio".
2. Use the parallelogram method to help students visualize the area of a circle.



For a parallelogram:

$$\text{Area} = (\text{base}) \times (\text{height})$$

$$\text{Area} = (1/2)Cr$$

$$\text{Area} = (1/2)(\pi d)r$$

$$\text{Area} = (1/2)\pi(2r)r$$

$$\text{Area} = \pi r^2$$

3. Have the students cut the circle into eight equal slices and form a parallelogram. This intuitive approach leads to the actual formula.
4. Use the formula to calculate the area of the 10 and 16 inch pizzas. Compare the results with previous estimations.
5. Have students solve additional examples. Stress the meaning of r^2 .

After Class

Textbook examples using formula

Reinforcement

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ROOM UNDER THE UMBRELLA

<u>Topic/Objective</u>	<u>Materials</u>
Area of Circle	Square yard marked on floor 36" diameter circle on floor (use masking tape to outline shapes on floor)

During Class:

1. Determine how many students can stand in a square yard or in a 36" circle.
2. Have students form groups to solve "Room Under the Umbrella". (Teacher may have to brainstorm or suggest possible approaches, diagram, etc.)
3. Ask students why we used a square yard and a 36" circle in our comparison.

After Class:

"All Wet"	Reinforcement
Text book problems using πr^2	Reinforcement
"Room Under the Umbrella"	Extension

ROOM UNDER THE UMBRELLA

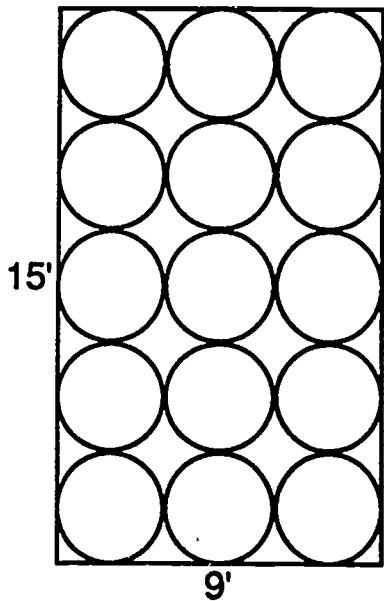
Horatio: Even in that crowd of people with umbrellas, I GOT WET!

Crow: Look at the facts, Horatio.

1. How many people can stand in a square yard?
2. How many people can stand under an umbrella that is 36" in diameter?



Use a rectangle 15' by 9' as an example and estimate the number of people that get wet.



Think! What happens if we change the size of the rectangle to 8' by 5' or the diameter of the umbrella to 40"?

Make up some other umbrella problems.



I COUNTED MY HOPS

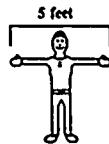
Reinforcement



Reinforcement

QUINCY MARKET: WE'VE GOT YOU SURROUNDED!

Fact: The Quincy Market building is 555' long and 50' wide. The average person has an arm spread of 5 feet.



Horatio: How far is it around the Quincy Market building?

Grasshopper: I didn't really measure, but I counted my 242 hops.

If every grasshopper hop is 60 inches long, what is the perimeter of the Quincy Market Building in feet?

1210 feet

perimeter

Horatio: I didn't really measure, but I took 24 steps when I walked along the width of the building.

If every step Horatio took was 25" long, what was the width of the building in feet?

600 inches = 50 feet
width

Using the information from the Grasshopper and Horatio, find the dimensions of the Quincy Market Building.

(Hint: Draw a diagram of a rectangle to help you solve the puzzle.)

555 feet X 50 feet

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Question: How many visitors would it take to surround Quincy Market?

242 people

Fact: Approximately 35,000 people visit Quincy Market every day.

Question: If all of the visitors on Tuesday held hands, how many times would Quincy Market be surrounded?

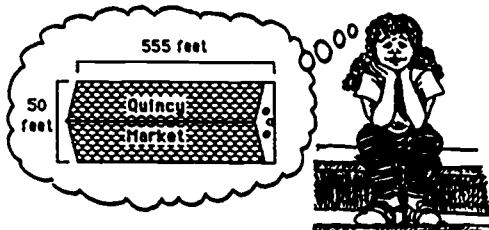
145 times



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PORTIA'S DILEMMA

Extension



Fact: One day Quincy Market had 34,364 visitors. Every visitor had a 5' arm spread. Suppose every visitor was there at the same time, and they all joined hands around the outside of Quincy Market.

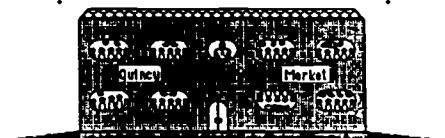
Question: What is the largest (in area) rectangle that can be formed that uses every visitor and has dimensions proportional to those of Quincy Market?

$$\text{length of human wall} = 78,810 \text{ ft.}$$

$$\text{width of human wall} = 7100 \text{ ft.}$$

$$\text{Area} = 559,551,000 \text{ sq. ft.} \approx 560,000,000$$

HOW MANY VISITORS CAN FIT INTO THE QUINCY MARKET BUILDING?



The dimensions of the Quincy Market Building are 50' by 555'. If we assume there are no obstacles in the building, how many people can fit inside the building at one time? First floor only, please! (HINT: Use the results from your class experiment and think about the number of people that fit into a square yard).

$$3083 \text{ sq. yds.} \times \frac{\text{people}}{\text{sq. yard}} = \text{people}$$

Find out about the fire regulations for your town and what limits there are on building capacity. How many people could legally fit into Quincy Market if it were in your town?

Use the results of your class experiment to determine how many people could fit into an elevator 5' x 6'. If the average weight of each person is 130 lbs., how much weight is that elevator carrying?

$$3.3 \text{ sq. yds.} \times \frac{\text{people}}{\text{sq. yard}} \times 130 \text{ lbs.} = \text{lbs.}$$

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PI FOR HORATIO

Reinforcement

Extension

PORTIA: Horatio, it's perfectly obvious to me you don't need to measure the circumference, just multiply the diameter by π !

HORATIO: Apple or blueberry?

Poor Horatio! He still thinks $\pi = \text{apple}$, but you know $\pi = 3.14$ (well, almost!). Find the circumference of the following using the formula $C = \pi d$.

1. A cup with a diameter 4". 12.56"
2. The top rim of a flower pot with diameter 6". 18.84"
3. The bottom rim of a lampshade with diameter 12". What is your answer in inches? 37.68" In feet? 3.14'
4. A circular rug with diameter 54". What is your answer in inches? 169.56" In feet? 14.13' In yards? 4.71 yds.
5. A circular swimming pool with diameter 18'. What is your answer in feet? 56.52' In yards? 19.17 yds.
6. A button with diameter 1/2". What is your answer in inches? .157"
7. A bicycle wheel with radius 13". How many inches have you travelled when the wheel makes one rotation? 87.64"
8. Estimate the diameter of a pipe with circumference 9 1/2". 3"

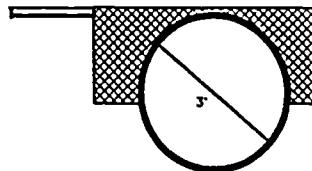
Measure the circumference of 3 circular objects and use the formula $C = \pi d$ to estimate the diameter of these objects.

OBJECT	CIRCUMFERENCE	DIAMETER
1.		
2.		
3.		

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HOW MANY ROTATIONS, HORATIO?

- HORATIO:** I think I'll push this cart around Quincy Market and count the number of times the wheel turns.
- CROW:** Remember, Horatio, the Quincy Market building is 50 feet wide and 555 feet long.
- GRASSHOPPER:** An estimation is good enough for me!
- PORTIA:** Does anybody have a calculator?



Find out how many times the wheel turns when the bullmarket cart is pushed around the perimeter of the Quincy Market building.

128.5 rotations

Why might Horatio's answer be different from Portia's?

Are there any accuracy problems here?

VARIATIONS FROM THE
PATH HORATIO TAKES, IR.
HOW CLOSE TO THE BUILDING.

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ROOM UNDER THE UMBRELLA

Extension

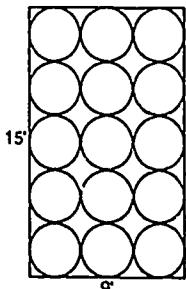
Horatio: Even in that crowd of people with umbrellas, I GOT WE!

Crow: Look at the facts, Horatio.

1. How many people can stand in a square yard?
2. How many people can stand under an umbrella that is 36" in diameter?



Use a rectangle 15' by 9' as an example and estimate the number of people that get wet.



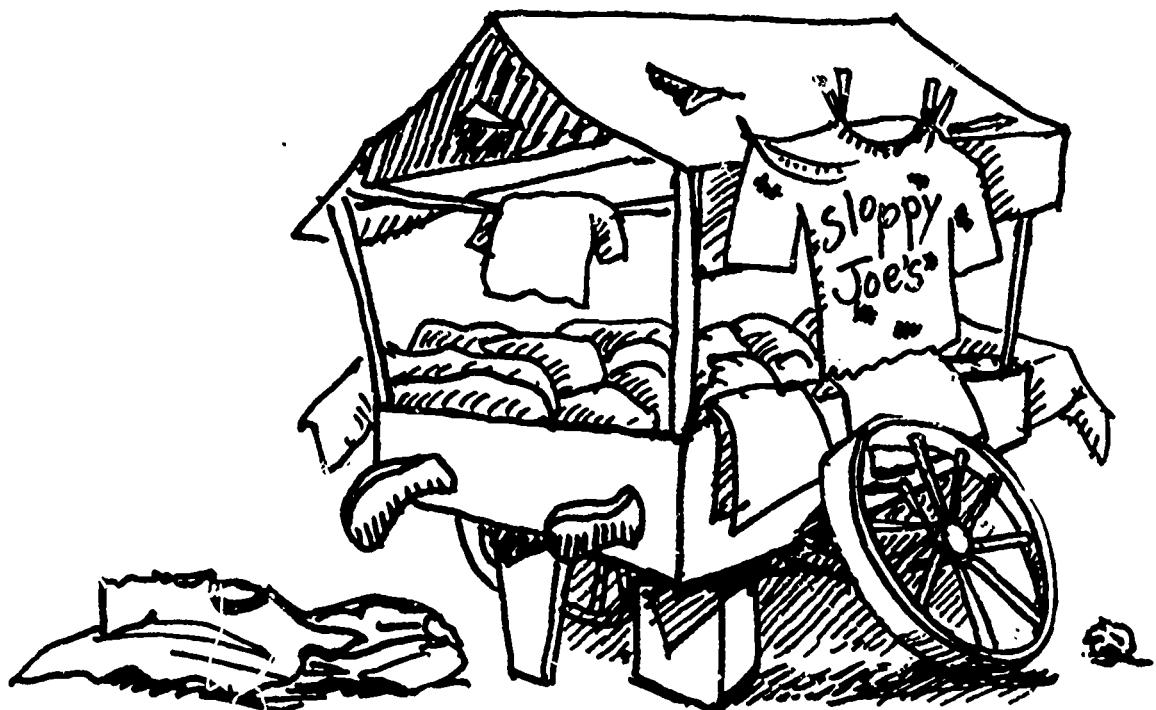
15 people get wet assuming
5 people per sq. yd. and
4 people per umbrella.

Think! What happens if we change the size of the rectangle to 8' by 5' or the diameter of the umbrella to 40"?

Make up some other umbrella problems.



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SIMULATION

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BUSINESS SIMULATIONS

<u>Topic/Objective</u>	<u>Materials Needed</u>
Problem Solving Percent of a number	<u>For Bull Market Game</u> Bull Market Cards Bull Market Score Sheets (6 per student) <u>For Computer Simulation</u> Any Apple II Computer T-Stop Saleogram Disk (included in unit)

Before Class:

Decide whether to use the Bull Market Game or the Computer Simulation or both.

The Bull Market Game is a simplified simulation of running a T-Stop cart. Each student maintains his/her own records and performs the calculations as the teacher presents each card. Students may also work in small groups. This activity can be used for two or more class periods.

T-Stop Sales is a computer simulation which will run on any Apple II computer. Students can work in small groups to run a cart and try to beat Sloppy Joe, a lazy but successful business person. This activity also can be used for two or more class periods.

BULL MARKET GAME

Materials Needed: Green Bull Market cards 5 1/2" x 4 1/4", Bull Market scoresheet

DIRECTIONS: This game is based on the BULL MARKET at Quincy market. The score sheet presents a one week simplified simulation of a T-shirt cart. The game may be used by an entire class, small groups or individually. Since directions on some cards vary, based on the price of T-shirts and the placement of the cart inside or outside, several students could use the same five cards for a week but have different profits.

1. Shuffle the deck of cards and put them face down.
2. Fill in your name on the score sheet and fill in the starting amount. This should be \$3,000 at the beginning of WEEK #1 and the profit or loss carried over for any other week. Also, note all carts pay a \$20.00 storage fee each week.
3. Choose inside or outside position for your cart for the week and enter the appropriate amount.
4. Order the number of T-shirts to keep the stock at 600. Your price per T-shirt is \$4.00.
5. Choose a selling price from \$10.00 to \$15.00 for the T-shirts for the first day of the week.
6. Take the top card in the pack and write the % (up or down) in the appropriate column. Calculate the number of T-shirts sold based on a normal day of 60 shirts sold.

e.g., Sales up 10%	60 + 6	Sales down 85%
10% of 60 is 6	66	85% of 60 is 45
		60 - 45
		15

7. Put the number of T-shirts sold for the day in the appropriate blank and calculate the total sales for the day.
8. Choose a price for T-shirts for the next day. Continue the same process for the week.
9. At the end of the week find the total number of shirts sold for the week.
10. Find the total sales for the week.
11. To calculate total profit for the first week subtract the \$3,000 you started with from the total sales. Carry this amount to the start of the next week.

NOTE: Don't forget at the beginning of each week to readjust your T-shirt order to keep inventory at 600.

BULL MARKET SCORESHEET

WEEK# _____

NAME _____

STARTING AMOUNT(This should be \$3,000
for the first week.)

\$ _____

Inside (\$275) or Outside (\$150)

-\$ _____

Storage (\$20.00)

-\$ _____

Order _____ T-shirts at \$4.00 each

-\$ _____

CASH ON HAND

\$ _____

	PRICE OF T-SHIRTS	TAKE CARD % UP OR DOWN	T-SHIRTS SOLD	TOTAL SALES FOR DAY
SUNDAY				
MONDAY				
TUESDAY				
WEDNESDAY				
THURSDAY				
FRIDAY				
SATURDAY				
TOTALS FOR WEEK				

Balance \$ _____

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T - STOP SALES Computer Simulation

Extension



T-Stop Sales is a computer simulation which will run on any Apple II computer. The program simulates the sale of T-shirts at a Bull Market cart for 1 month. Students run their cart in competition with Sloppy Joe's T-shirts. Sloppy Joe is a lazy businessperson who always orders the same number of T-shirts and never changes his prices.

The goal of the game is to beat Sloppy Joe by ordering and pricing carefully. Students use problem solving strategies and accurate math calculations to win the game.



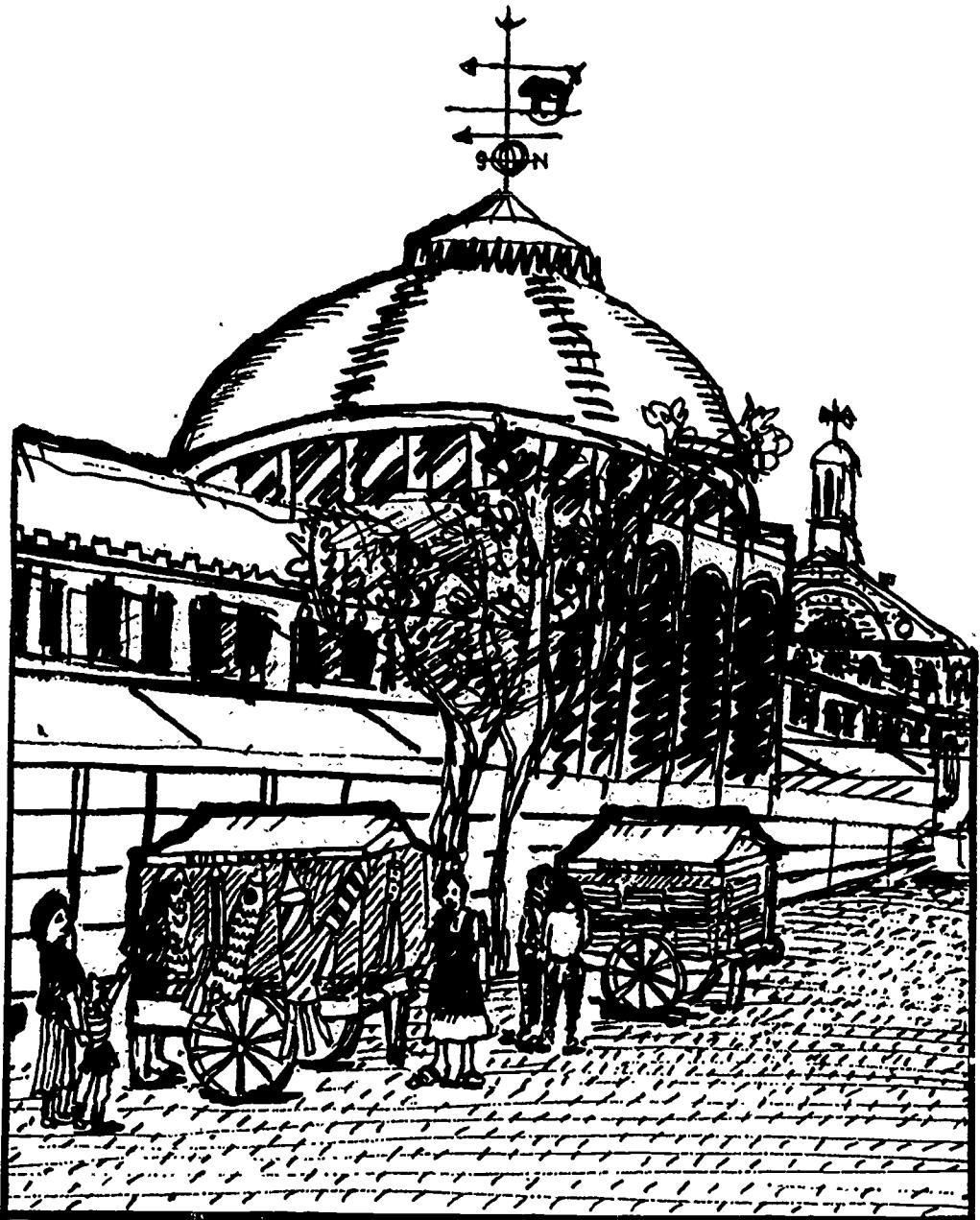
GRAND FINALE

Finish Horatio and Portia's story.



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TEACHER RESOURCES

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RESOURCES

MATERIAL	ADDRESS	TELEPHONE NUMBER
T-Aid Map	MBTA Customer Service 10 Park Plaza Boston, MA 02116	617-722-3200
Official Massachusetts Transportation Map	Public Information Office Mass. Dept. of Public Works 10 Park Plaza Boston, MA 02116-3973	617-973-7500
Teachers' Guide to Faneuil Hall (People and Places)	Boston National Historic Parks 15 State Street Boston, MA 02109	617-223-2982
History of Measurement	Ford Motor Company The American Road PO Box 1899 Dearborn, MI 48121	
Brochure on Quincy Market	Faneuil Hall	617-223-6098

CITY/TOWN STATISTICS

Town/City	1985 Population	Sq. Miles Land and Water Area	Median Family Income	Means of Transportation	Grade 7 Population	Grade 8 Population
Acton	17,431	10.14	\$31,607	Lowell RTA	300	309
Boston	625,000 (est)	45.40	\$16,062	MBTA Hudson	4,489	4,397
Cambridge	95,362	7.14	\$17,845	MBTA	515	559
Chelmsford	30,684	22.96	\$28,174	Lowell RTA	414	453
Hingham	20,648	22.59	\$30,157	MBTA P and B	273	307
Lexington	29,224	16.63	\$34,989	MBTA Grayline	347	376
Lincoln	6,902	14.92	\$31,543	MBTA	120	95
Malden	52,474	5.13	\$19,814	MBTA	431	483
Marblehead	19,403	4.42	\$29,167	MBTA	167	203
Medford		8.76	\$21,441	MBTA Hudson	373	357
Newton	82,925	18.33	\$30,436	MBTA Suburban	651	736
Revere	39,512	6.32	\$19,004	MBTA	403	413
Somerville	71,134	4.32	\$18,220	MBTA	465	483
Waltham	57,955	13.52	\$22,335	MBTA	462	458
Weymouth	53,735	17.72	\$22,693	MBTA	593	608

QUINCY MARKET DATA

Steve's Ice Cream

Most popular flavors:

1. Cookie-O
2. Oatmeal Raisin
3. Vanilla and Chocolate

Least popular:

1. Nuts
2. Butter Pecan

The most popular flavors sell at a 5 to 1 ratio to the least popular flavors.

They sell 110 pieces (3 1/2 gallons each) on weekends vs. 60 pieces on weekdays.

Raging Cajun

- | | |
|--------------|--------------------------|
| 1. Jambalaya | (\$4.50 lg., \$2.50 sm.) |
| 2. Gumbo | (least popular) |

Jamalaya to Gumbo 60 to 20

Aris Barbecue

- | | |
|--|--------|
| 1. 1/4 pounder cheesesburgers to jumbo hotdogs | 4 to 1 |
| 2. Fried onion rings to jumbo hot dogs | 5 to 1 |

Boston Brownies

Adult preferences:

- | | | | |
|------------------|-----|---------------|--------|
| German Chocolate | vs. | Butterscotch | 5 to 1 |
| | | Boston's Best | 4 to 3 |

Young people:

- | | | | |
|--------------|-----|-------------|------|
| M&M Brownies | vs. | Double Deck | Even |
|--------------|-----|-------------|------|

Adult customers outnumber youngsters 5 to 1, and about 1000 brownies are sold per day.

The Taco Maker

- | | |
|------------|-------------|
| 1. Taco | 400 per day |
| 2. Burrito | 250 per day |
| 3. Tostado | 50 per day |

Root Beer to Diet Coke 10 to 1

QUINCY MARKET DATA

Cardoos (candy and nuts)

Gummi "bears", "worms", "strawberries", "fish", "shells"	vs. Gumballs	3 to 1
	vs. Sugar Daddy's	20 to 1
	vs. Shoelace Licorice	3 to 1

Pizzeria Regina

Cheese vs. Pepperoni 3 to 1

Whole Pizzas:

Pepperoni	to Mushroom	4 to 1
	to Anchovy	20 to 1

They sell about 600 pizzas per day.

Ming Tree

#10 Combination Plate vs. #3 (chow mein, fr. rice & chicken fingers) 3 to 1

Appetizers:

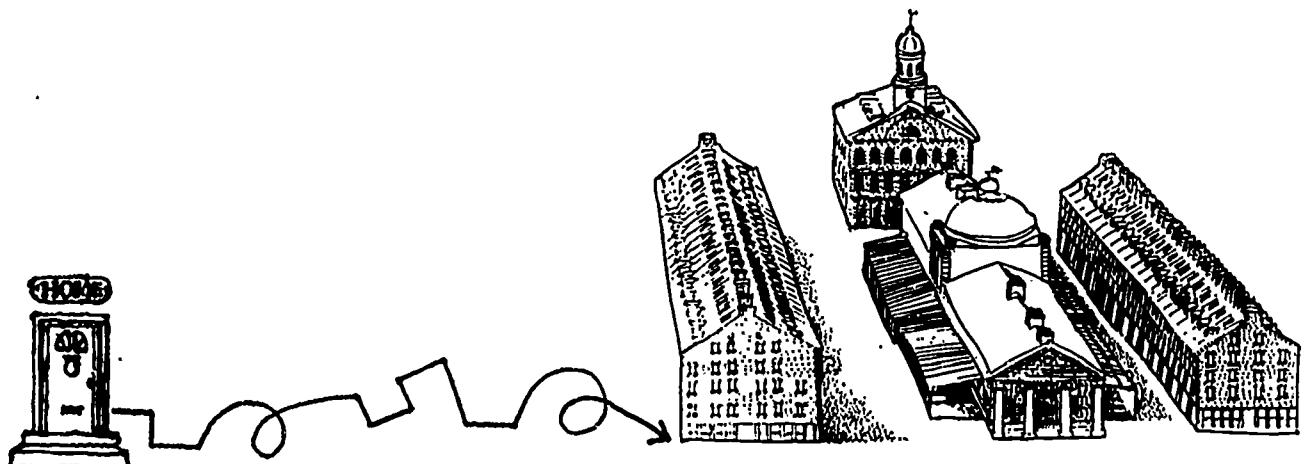
1. Teryaki sticks
2. Chicken Wings
3. Shrimp and Egg Rolls (less popular)

Teryaki to Egg Rolls 2 to 1

160

SUPER CHALLENGES!!

1. How big is 1,000,000? How can you communicate this to someone else?
2. You run a T-shirt cart and must make some decisions concerning staffing, pricing, etc. How can you gain maximum profit?
 - What are the patterns of sales--when are they heavy, light?
 - When does the line of customers require a second salesperson?
 - What should the price of T-shirts be to minimize change and maximize a desirable sounding price?
3. What is the "best" route from your home to Quincy Market? How do you define "best"? (Some ideas: minimum average time, most reasonably consistent time, traffic patterns, etc.)
4. Design a parking garage for Quincy Market.
5. What is the best location for a T-shirt cart in Quincy Market?
 - Should it be inside or outside?
 - How crowded should the area be?
 - What other stands should it be near?

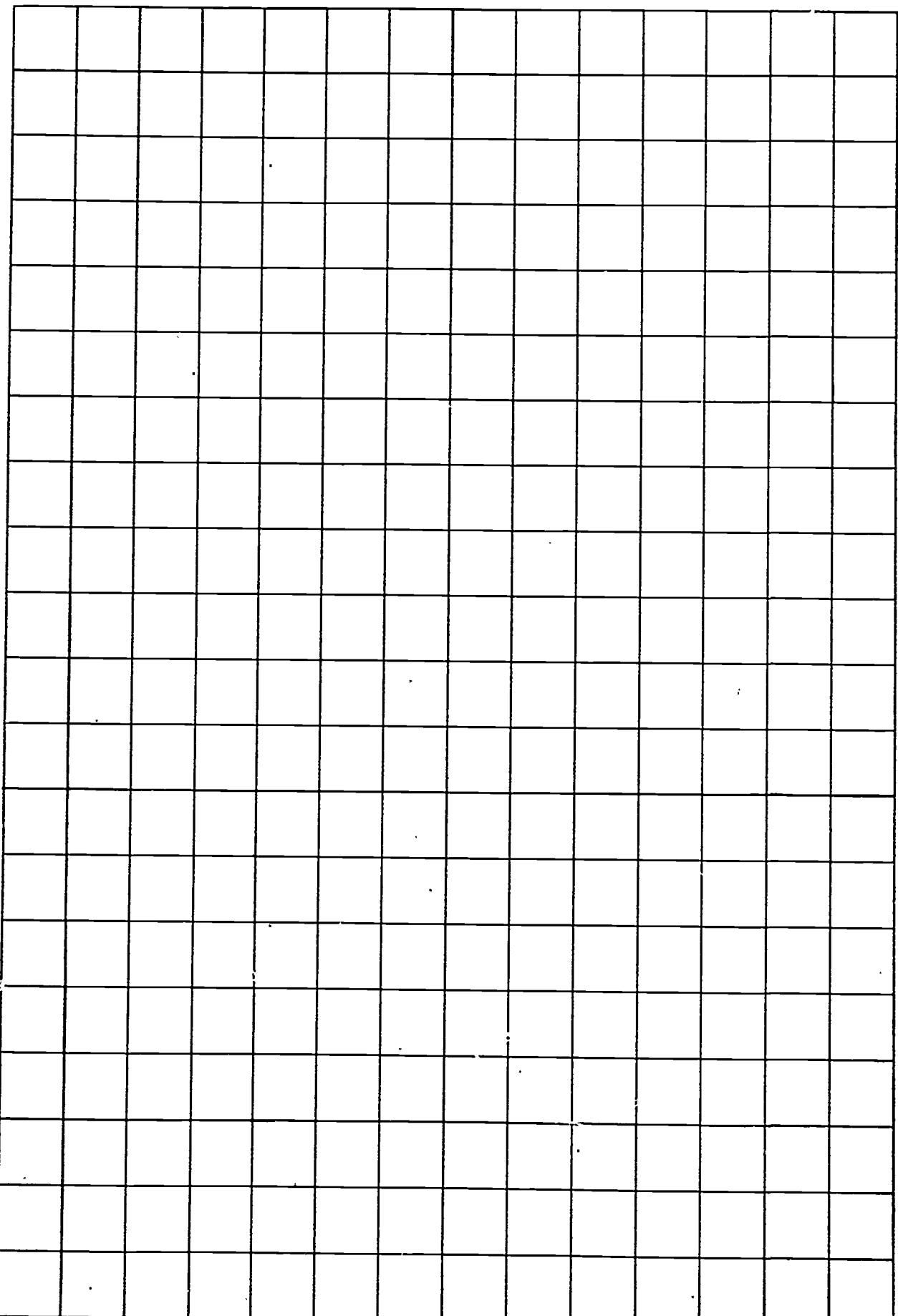


1 Division/Inch

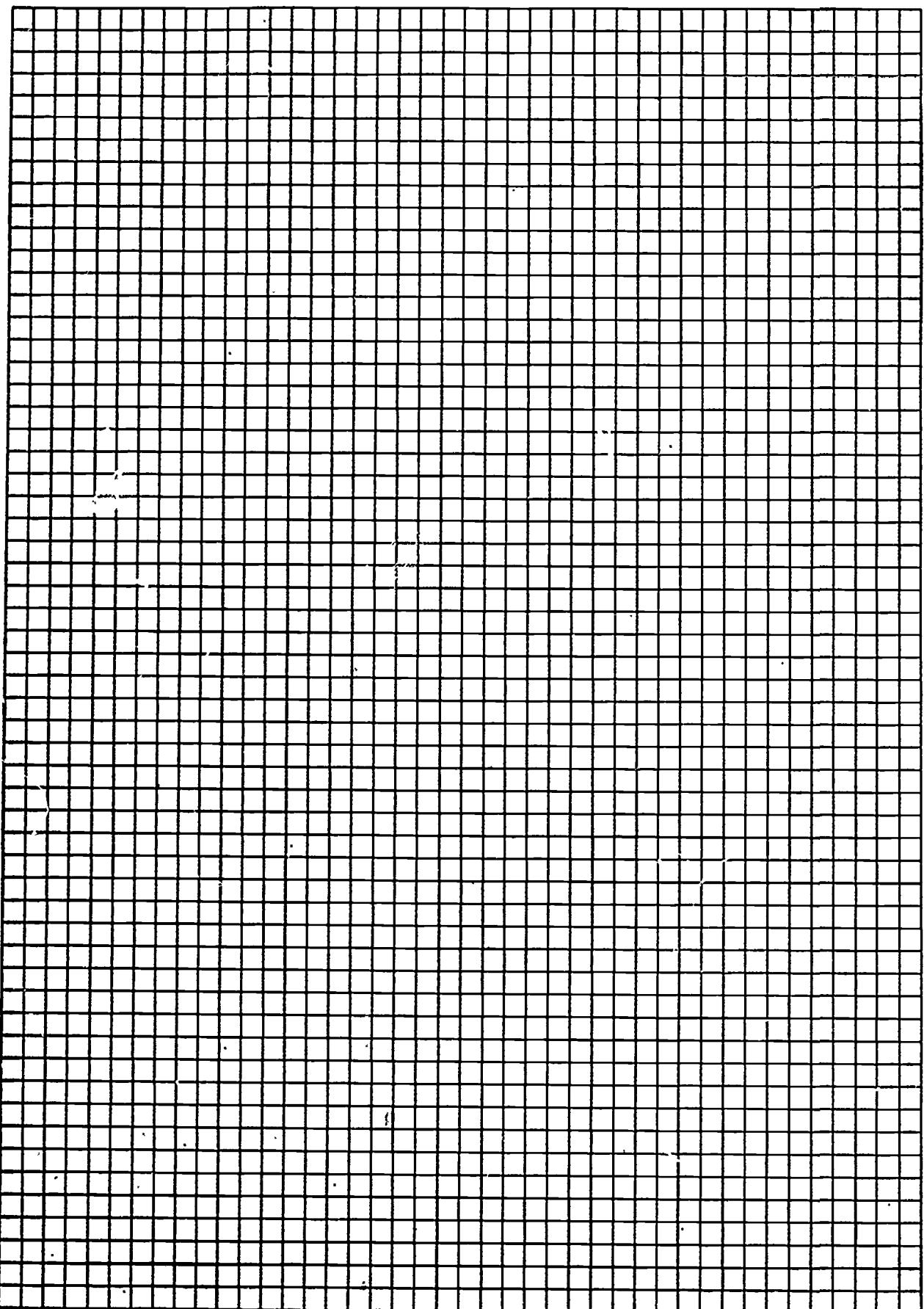
HPBooks—GRAPH PAPER From Your COPIER

A blank 8x6 grid of 48 empty cells, arranged in 8 rows and 6 columns. The grid is defined by thick black lines.

2 Divisions/inch



6 Divisions/inch



**IF SHIRTS ARE
\$12.50 SALES ARE
DOWN 10%**

**IF SHIRTS ARE
MORE THAN \$12.50
SALES ARE DOWN 90%**

**IF SHIRTS ARE
LESS THAN \$12.50
SALES ARE NORMAL**

BUSINESS IS BOOMING!

**SALES ARE UP
75% IF YOUR SHIRTS
ARE \$10.00**

**SALES ARE UP
50% IF YOUR SHIRTS
ARE MORE THAN \$10.00**

**WEATHER
IS BAD!**

**SALES ARE DOWN
50% IF YOU ARE INSIDE**

**SALES ARE DOWN
95% IF YOU ARE OUTSIDE**

**SALES
DOWN
10%**

168

SENIOR CITIZEN TRIP

**SALES ARE UP
20% IF YOUR SHIRTS
ARE LESS THAN \$11.00**

**SALES ARE DOWN
30% IF YOUR SHIRTS
ARE \$11.00 OR MORE**

169

SALES

UP

40%

170

SALE

**IF YOUR SHIRTS ARE
\$10.00 YOU SELL 20%
OF YOUR REMAINING
STOCK
(ROUND TO THE NEAREST
WHOLE NUMBER)**

**IF YOUR SHIRTS ARE MORE
THAN \$10.00 YOU SELL
5% OF YOUR REMAINING
STOCK**

**SALES
UP
30%**

172

SCHOOLS ON FIELDTRIPS!

**SALES ARE UP
10% IF YOUR SHIRTS
ARE LESS THAN \$13.00**

**SALES ARE DOWN
80% IF YOUR SHIRTS
ARE \$13.00 OR MORE**

**SALES
DOWN
50%**

174

**NICE
WEATHER
AND MOST PEOPLE
ARE OUTSIDE**

**SALES ARE UP
15% IF YOU ARE OUTSIDE**

**SALES ARE DOWN
60% IF YOU ARE INSIDE**

**SALES
DOWN
45%**

176

**STORM...
NATIONAL
DISASTER
DECLARED BY
GOVERNOR**

NO SALES TODAY

BUSINESS AS USUAL

178

**SALES
DOWN
25%**

179

GREAT WEATHER!

**SALES ARE UP
80% IF YOU ARE OUTSIDE**

**SALES ARE UP
10% IF YOU ARE INSIDE**

180

SPECIAL ORDER

**150 SHIRTS
SOLD**

181

CONVENTION IN TOWN

**SALES ARE UP
100%**

182

SCHOOLS ON FIELDTRIPS!

**SALES ARE UP
80% IF YOUR SHIRTS
ARE LESS THAN \$12.00**

**SALES ARE UP
30% IF YOUR SHIRTS
ARE \$12.00 OR MORE**
183

**WEATHER
IS GREAT!**

**SALES ARE UP
10% IF YOU ARE INSIDE**

**SALES ARE UP
25% IF YOU ARE OUTSIDE**

STORM TODAY

**SALES ARE DOWN
30% IF YOU ARE INSIDE**

**SALES ARE DOWN
90% IF YOU ARE OUTSIDE**

**NO SALES
IF YOU ARE OUTSIDE**

**IF YOU ARE INSIDE
SALES ARE DOWN 70%**

186

SALES

UP

25%

187

**SALES
DOWN
30%**

188

**SALES
DOWN
15%**

189

SALES

UP

15%

190

**ADVERTISEMENT
PAYS OFF**

**SALES UP
5%**

191

**SALES
UP
20%**

192

**NO
SALES
IF YOUR SHIRTS ARE
\$15.00
IF YOUR SHIRTS ARE
LESS THAN \$15.00
SALES ARE UP 35%**

193

SALES

UP

45%

194

TOURIST SEASON

**ALL SALES ARE UP
25%**

195

**SALES
DOWN
40%**

196

**SALES
DOWN
35%**

197

SALES

UP

5%

198

**SALES
DOWN
20%**

199

BULLMARKET

BULLMARKET

BULLMARKET

BULLMARKET

BULLMARKET

BULLMARKET

BULLMARKET

BULLMARKET

BULLMARKET

**SALES
UP
10%**

201

**SALES
ARE UP
33 1/3 %
IF YOU ARE OUTSIDE
SALES
ARE DOWN
66 2/3 %
IF YOU ARE INSIDE**

202

SALES

UP

50%

203

CONVENTION IN TOWN

**SALES ARE UP
60% IF YOUR SHIRTS
ARE LESS THAN \$12.00**

**SALES ARE DOWN
50% IF YOUR SHIRTS
ARE \$12.00 OR MORE**

SALES

UP

35%

205